

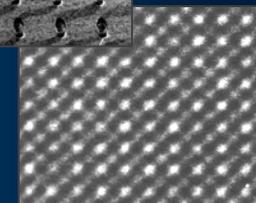
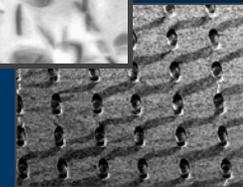
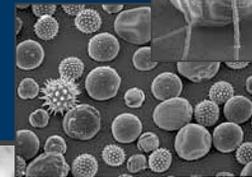
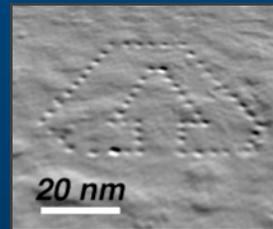
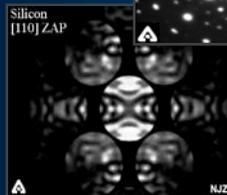
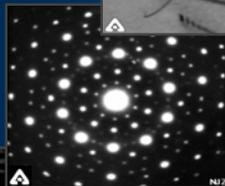
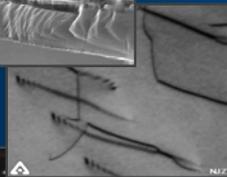
Introduction to Transmission/Scanning Transmission Electron Microscopy and Microanalysis

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Newbury, O'keefe, numerous text books, and
apologies to all those from whom I can't remember
collecting images/figures over the years.



A Few References:

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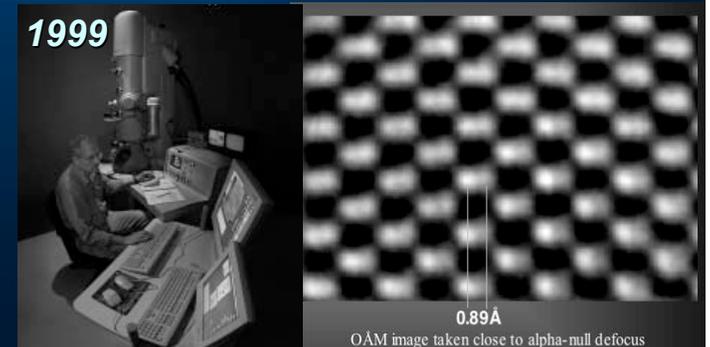
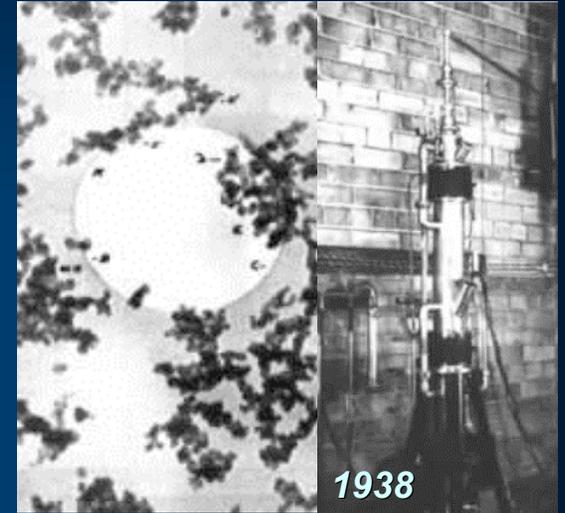
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Hren, Goldstein, Joy Plenum Press 1979

A Historical Time Line in Electron Optical Instrumentation

- 1897 JJ Thompson - Discovery of the Electron
- 1926 H. Bush Magnetic/Electric Fields as Lenses
- 1929 E. Ruska PhD Thesis Magnetic lenses
- 1931** Knoll and Ruska 1st EM built
- 1932 Davisson and Calbrick - Electrostatic Lenses
- 1934 Driest & Muller - EM surpasses LM
- 1939** von Borries & Ruska - 1st Commercial EM
~ 10 nm resolution
- 1945** ~ 1.0 nm resolution (Multiple Organizations)
- 1965 ~ 0.2 nm resolution (Multiple Organizations)
- 1968** A. Crewe - U.of Chicago - Scanning Transmission Electron Microscope
~ 0.3 nm resolution probe - practical Field Emission Gun
- 1986 Ruska et al - Nobel Prize
- 1999 < 0.1 nm resolution achieved (OAM)
- 2009 0.05 nm (TEAM)



Tutorial Outline

Introductory Remarks

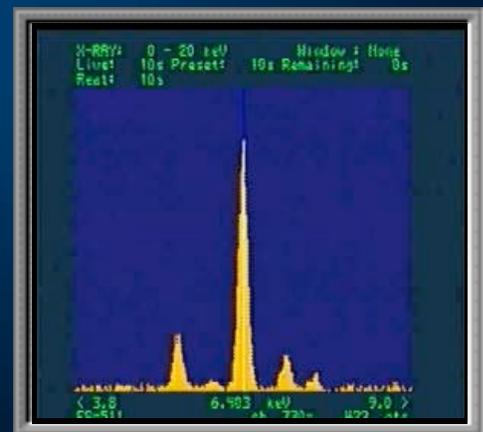
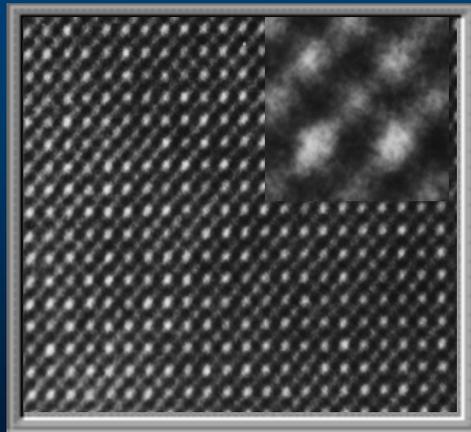
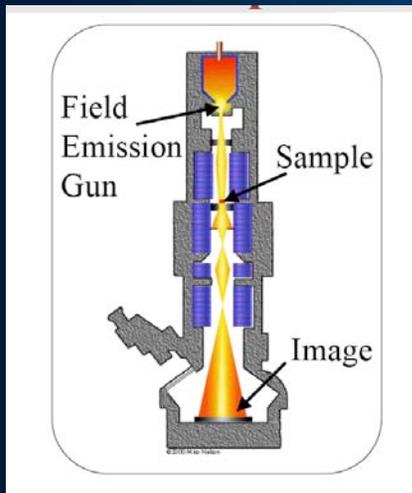
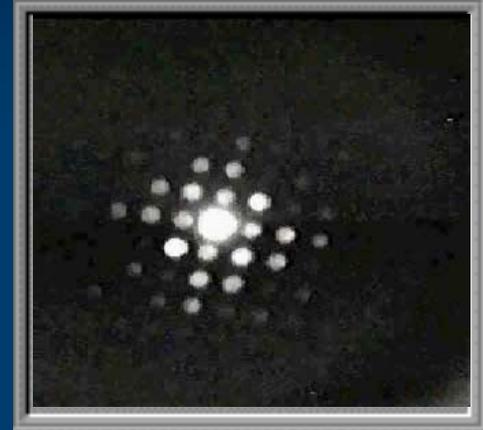
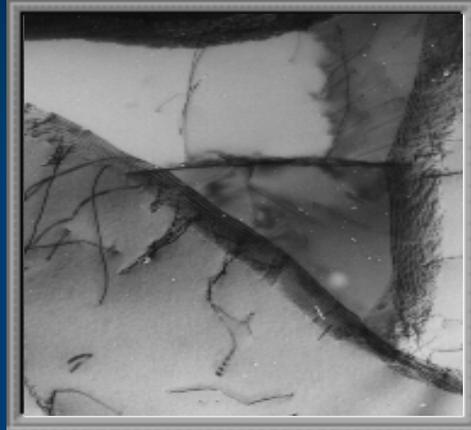
Instrumentation

- Electron Sources
- Electron Optics
- Electron Detectors

Electron Beam Interactions ->Operating Modes

- Electron Scattering
- Diffraction
- Imaging
- Other Modes
 - STEM
 - HREM
 - ? Others ?
- X-ray Energy Dispersive Spectroscopy
- Electron Loss Spectroscopy

Transmission Electron Microscopy

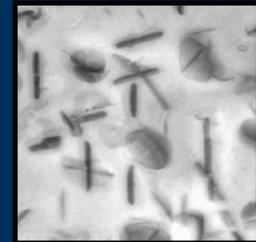


Microscopy & Microanalysis

Experimental methodologies which employ (electron-optical) instrumentation to spatially characterize matter on scales which range from tenths of a millimeter to tenths of a nanometer. The principle modalities employed are:

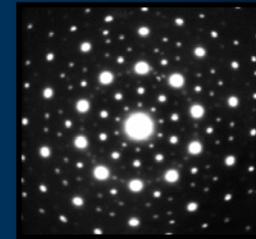
Imaging

- Scanning Electron Microscopy
- Transmission Electron Microscopy
- Scanning Transmission Electron Microscopy
- Focussed Ion Beam



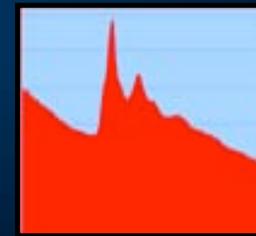
Diffraction

- Electron Backscattered Diffraction
- Selected Area Electron Diffraction
- Convergent Beam Electron Diffraction
- Reflection High Energy Electron Diffraction



Spectroscopy

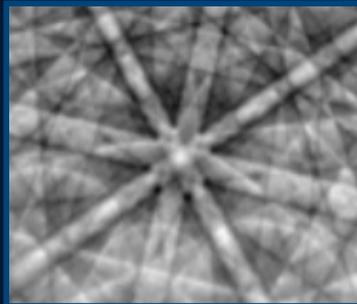
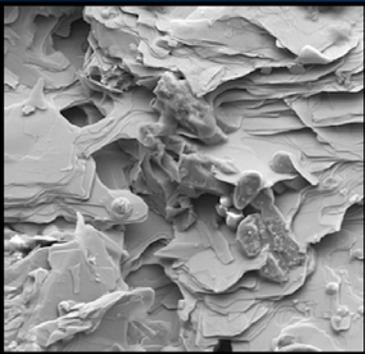
- X-ray Energy Dispersive
- Electron Energy Loss
- Auger Electron



Role of Traditional Electron Microscopy

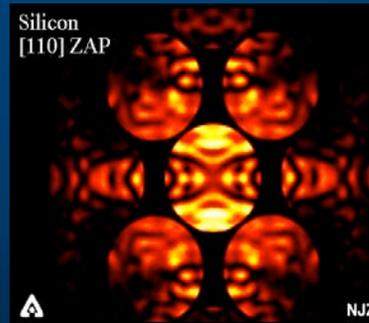
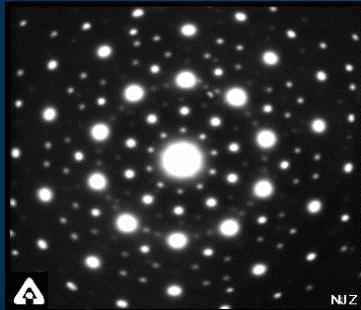
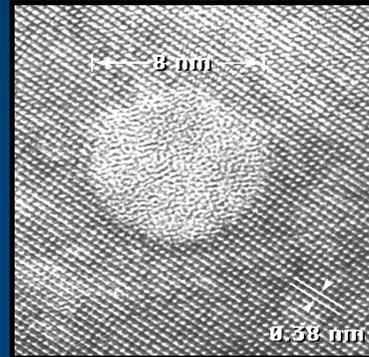
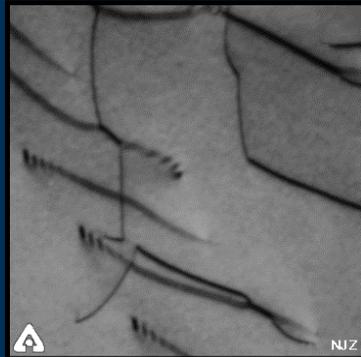
SEM

Scanning Electron Microscopy



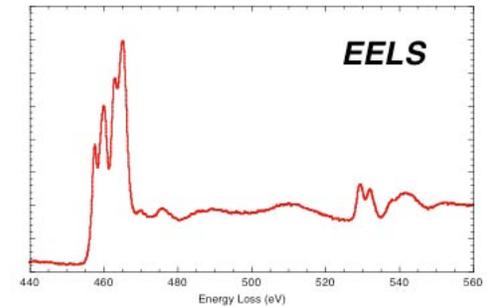
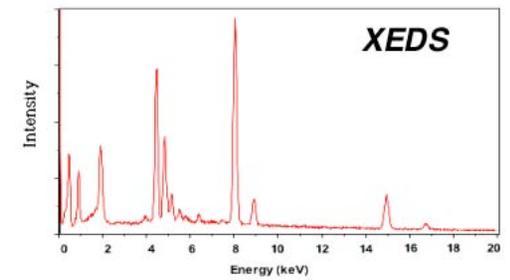
TEM - STEM - HREM

Transmission - Scanning Transmission -
High Resolution Electron Microscopy



AEM

Analytical Electron
Microscopy



Morphology, Crystallography, Elemental, Chemical, Electronic Structure

Elastic Scattering Spectroscopies

Electron Microscopy (EM),

Scanning Electron Microscopy (SEM),

SEM-based Electron Channeling Patterns (ECP),

Transmission Electron Microscopy (TEM),

Transmission Electron Diffraction (TED),

Convergent Beam Electron Diffraction (CBED)

Selected Area Electron Diffraction (SAED)

Scanning Transmission Electron Microscopy (STEM),

Reflection High Energy Electron Diffraction (RHEED)

Low Energy Electron Diffraction (LEED)

X-ray Diffraction (XRD),

Scanning Transmission X-ray Microscopy (STXM)

Neutron Diffraction (ND).

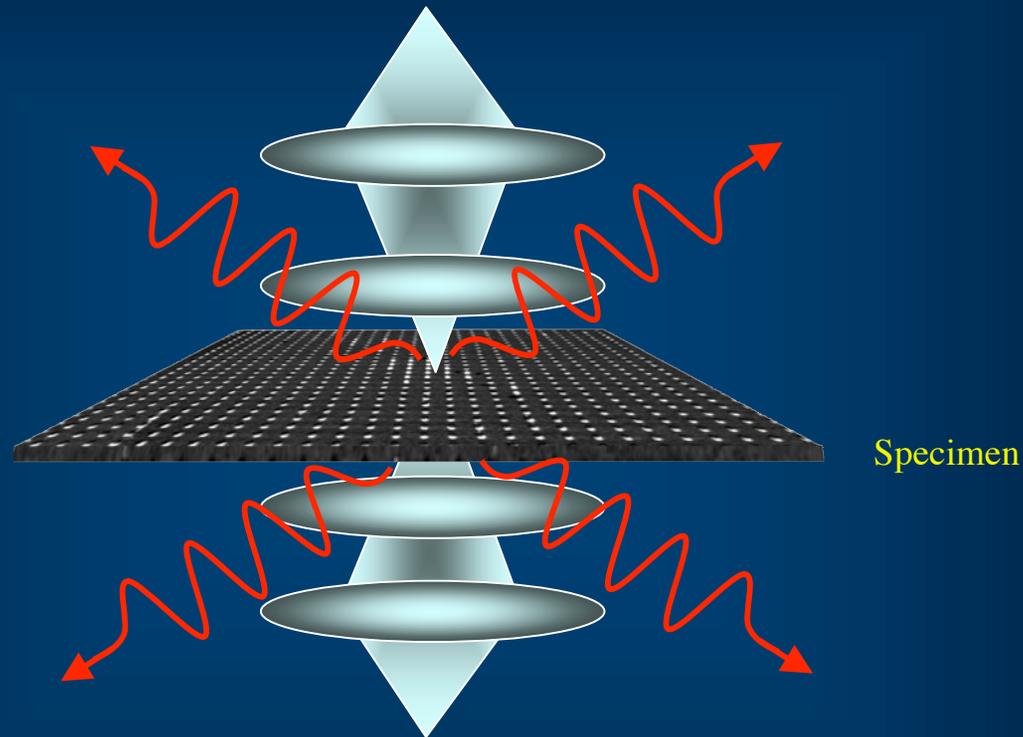
Inelastic Scattering Spectroscopies

	<u>Type</u>
<i>Secondary Electron Imaging (SEI)</i> <i>Backscattered Electron Imaging (BEI/BSI)</i> <i>Auger Electron Spectroscopy (AES),</i> <i>Electron Energy Loss Spectroscopy (EELS),</i> <i>EXtended Energy Loss Fine Structure (EXELFS),</i> <i>Energy Loss Near Edge Fine Structure (ELNES),</i>	$e^- \Rightarrow e^-$
<i>X-ray Emission Spectroscopy (XES),</i> <i>X-ray Energy Dispersive Spectroscopy (XEDS),</i> <i>Wavelength Dispersive Spectroscopy (WDS),</i> <i>Cathodoluminescence (CL)</i>	$e^- \Rightarrow \lambda$
<i>X-ray Photoelectron Spectroscopy (XPS),</i> <i>X-ray Photoelectron Microscopy (XPM),</i> <i>Ultraviolet Photoelectron Spectroscopy (UPS),</i>	$\lambda \Rightarrow e^-$
<i>X-ray Absorption Spectroscopy (XAS),</i> <i>EXtended X-ray Absorption Fine Structure (EXAFS),</i> <i>X-ray Absorption Near Edge Fine Structure (XANES)</i> <i>X-Ray Fluorescence (XRF).</i>	$\lambda \Rightarrow \lambda$

Comparison Source Characteristics

<i>Source</i>	<i>Brightness (particles/cm²/sR/eV)</i>	<i>Elastic Mean Free Path (nm)</i>	<i>Absorption Pathlength (nm)</i>	<i>Attainable Probe Size (nm)</i>
<i>Neutrons</i>	10^{14}	10^7	10^8	10^6
<i>X-rays</i>	10^{26}	10^3	10^5	~ 30
<i>Electrons</i>	10^{29}	10^1	10^2	< 0.1

Reflection / Scanning Microscopy
Deals Mainly with Near Surface Region



Transmission Microscopy
Deals Mainly with Internal Structure

Modern EM's can depending upon the specimen operate in both modes

What are the limits of Resolution?

Abbe (Diffraction) Limit:

Defines the minimum resolvable distance between the image of two point objects using a perfect lens.

In any magnifying system a point object (i.e. zero dimension) cannot be imaged as a point but is imaged as a distribution of intensity having a finite width.

Resolution of an imaging system

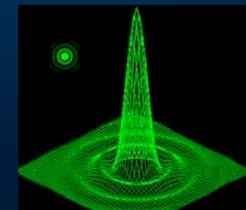
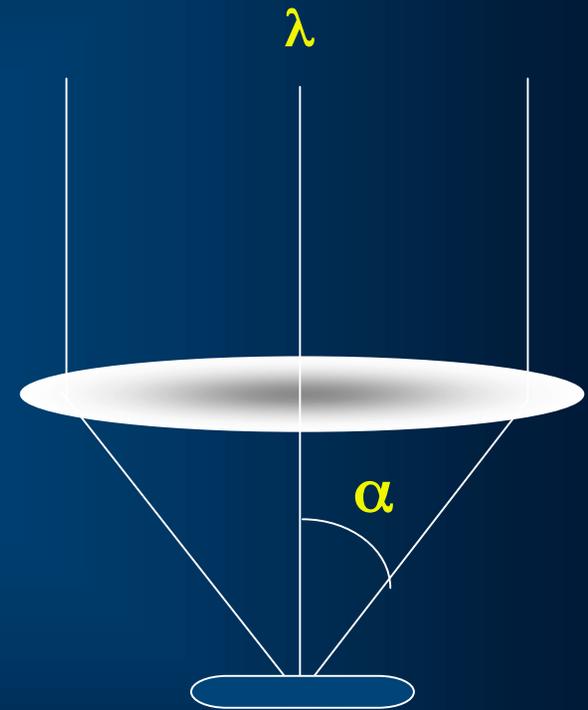
$$\rho = \frac{0.6\lambda}{\eta \sin(\alpha)}$$

λ = wavelength of the imaging radiation

η = index of refraction of the lens

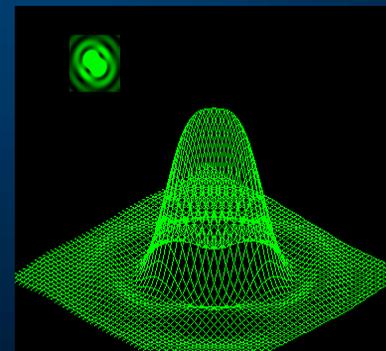
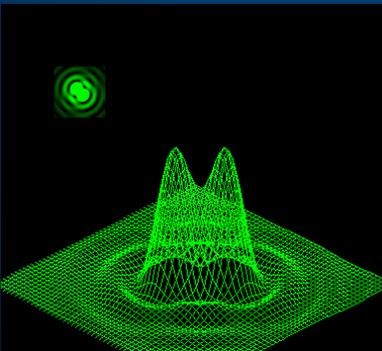
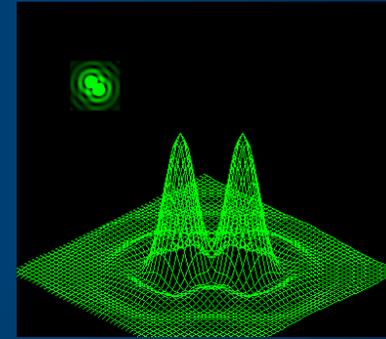
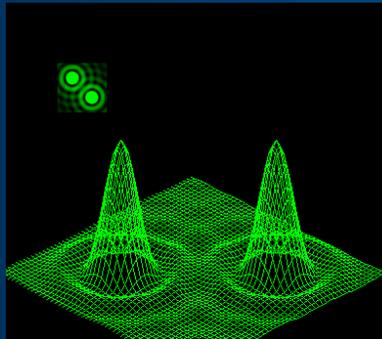
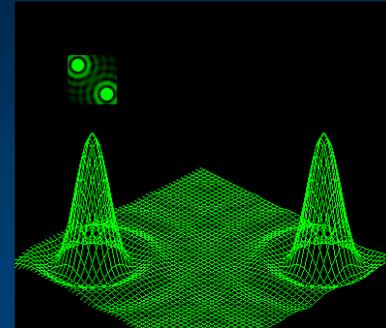
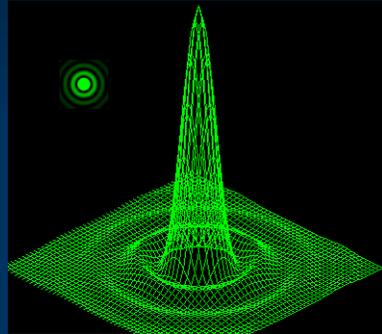
α = illumination semi-angle

NA = numerical aperture = $\eta \sin(\alpha)$



Resolution vs. Magnification

$$\rho = \frac{0.6\lambda}{\eta \sin(\alpha)}$$



Magnification in these images is constant ! Do not confuse the two concepts.

Some Fundamental Properties of Electrons

- Electron wavelength: based on de Broglie's ideas of wave-particle duality we know $\lambda = h/p$, where p is the electron momentum, h is Planck's constant, and λ is corresponding wavelength of the electron.
- In the TEM we impart momentum to the electron by accelerating it through a potential drop, V , giving it a kinetic energy eV . This potential energy must equal the kinetic energy:

$$eV = \frac{m_0 v^2}{2}$$

For nonrelativistic electron wavelength

$$p = mv = \sqrt{2m_0 eV}$$

$$\lambda(\text{\AA}) = \frac{h}{p} = \frac{h}{\sqrt{2m_0 eV}} \approx \frac{12.27}{\sqrt{V(\text{volts})}}$$

- However, for electron microscopy, relativistic effect cannot be ignored at 100-keV energies and above because the velocity of the electron become greater than half the speed of light. So the corrected (relativistic effect is considered) electron wavelength is:

$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2m_0 eV \left(1 + \frac{eV}{2m_0 c^2}\right)}} \approx \frac{12.27}{\sqrt{V(1 + 0.978 \times 10^{-6} V)}}$$

Electron Properties as a Function of Accelerating Voltage

Table 1.2. Electron Properties as a Function of Accelerating Voltage

Accelerating voltage (kV)	Nonrelativistic wavelength (nm)	Relativistic wavelength (nm)	Mass ($\times m_0$)	Velocity ($\times 10^8$ m/s)
100	0.00386	0.00370	1.196	1.644
120	0.00352	0.00335	1.235	1.759
200	0.00273	0.00251	1.391	2.086
300	0.00223	0.00197	1.587	2.330
400	0.00193	0.00164	1.783	2.484
1000	0.00122	0.00087	2.957	2.823

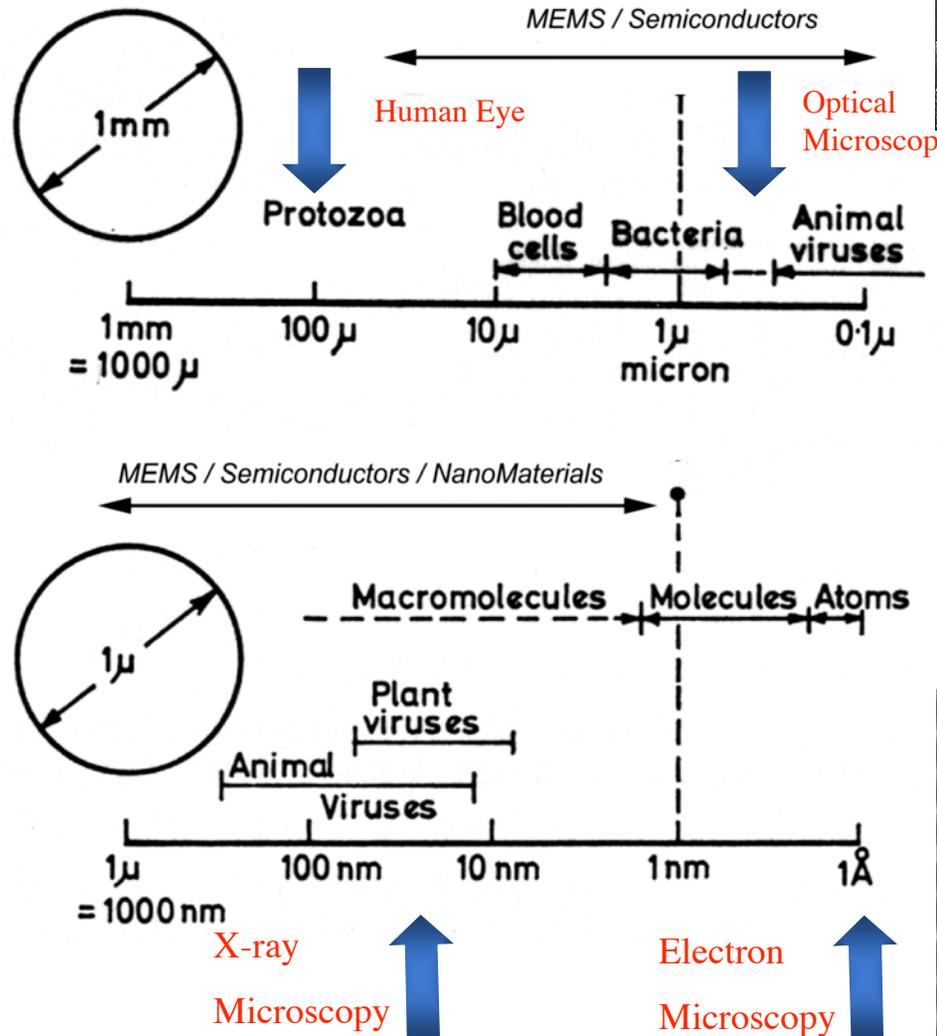
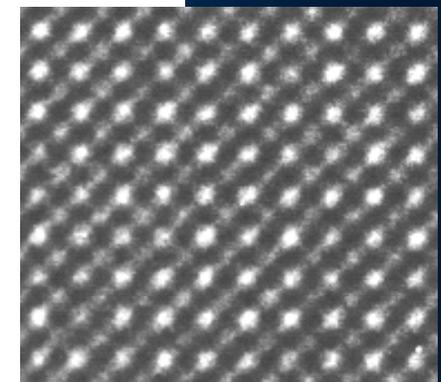
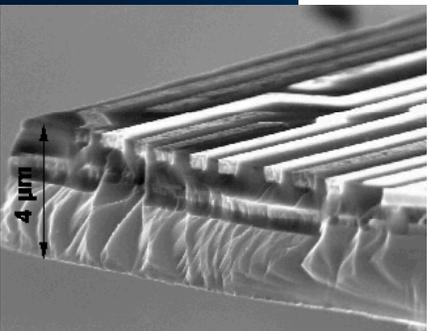
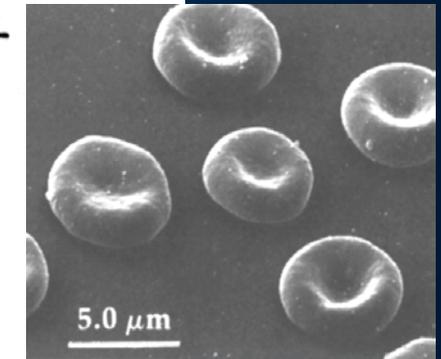
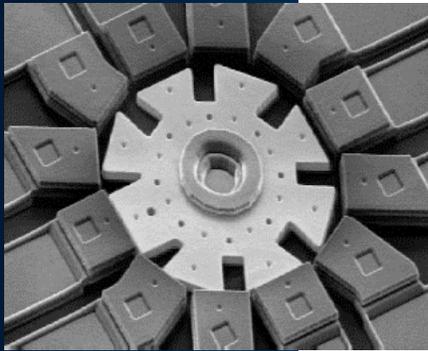
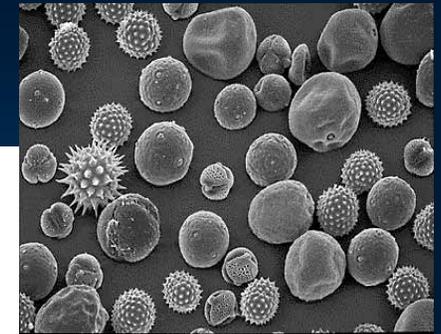
Light vs Electrons

Light Microscope	Electron Microscope
$\lambda \sim 0.5 \mu\text{m}$	$\lambda = \frac{h}{\sqrt{2m_0eV_0}} = 0.068 \text{ \AA} (30 \text{ kV})$
$\eta = 1.5$ (glass)	$\eta = 1.0$ (Vacuum)
$\alpha \sim 70^\circ$	$\alpha \leq 1^\circ$
$\rho \sim 0.21 \mu\text{m} = 2100 \text{ \AA}$	$\rho \sim 4.1 \text{ \AA}$

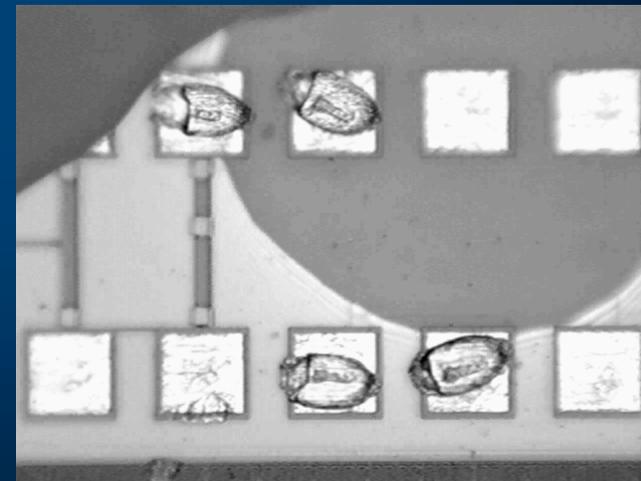
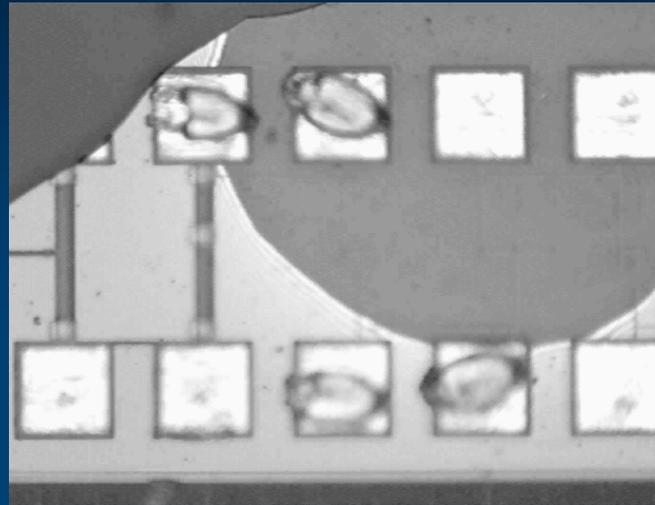
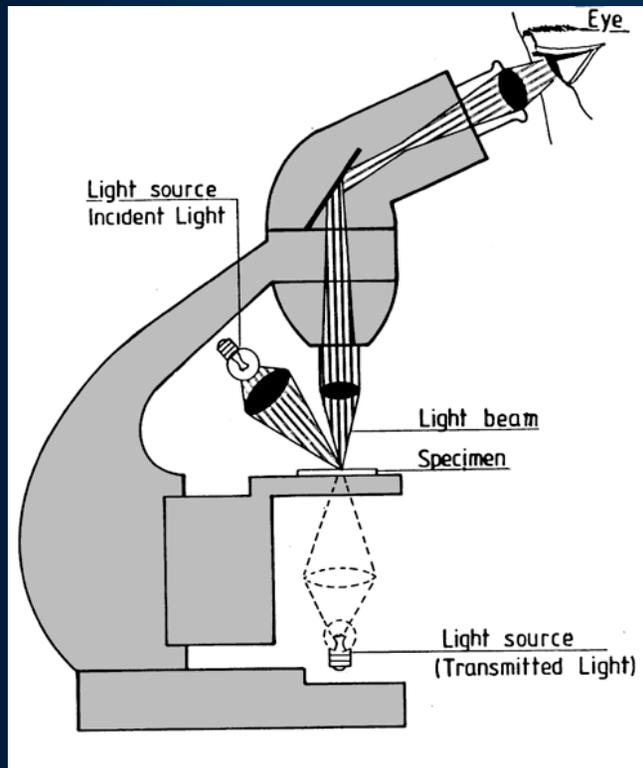
$$\rho = \frac{0.6\lambda}{\eta \sin(\alpha)}$$

From Ants to Atoms

Microscopy is needed nearly everywhere



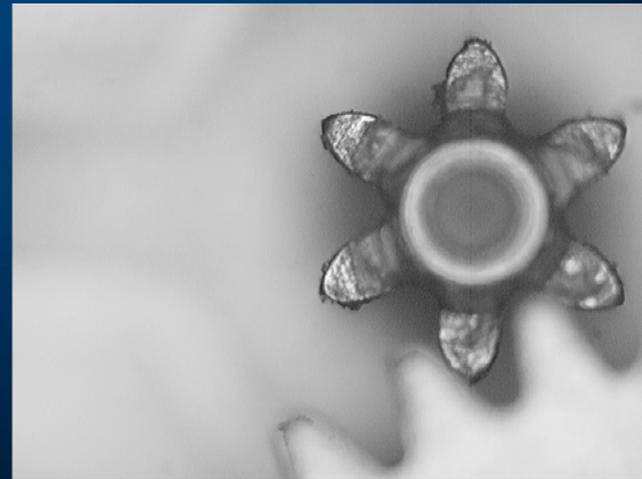
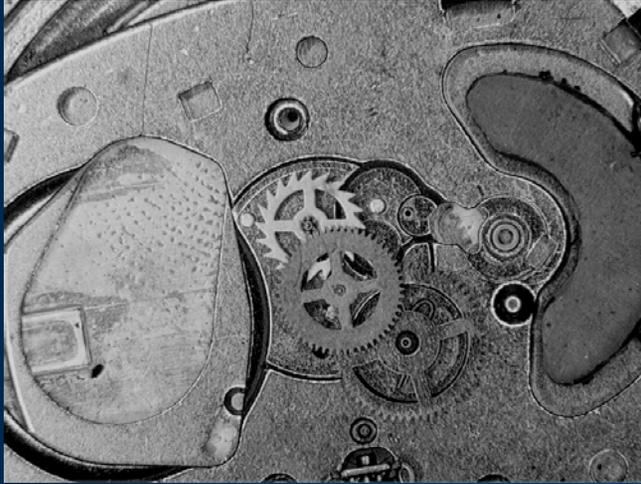
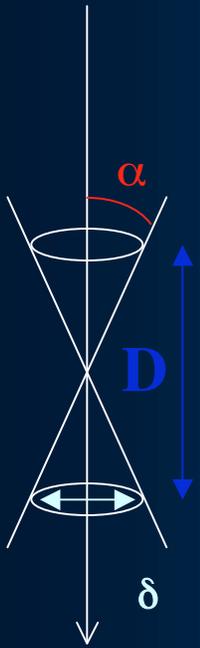
Depth of Field



The distance parallel to the optical axis of the microscope that a feature on the specimen can be displaced without loss of resolution

Depth of Field

Varies with Magnification



Depth of Focus/Field

The distance parallel to the optical axis of the microscope that a feature on the specimen can be displaced without loss of resolution

Optical Microscope

$$d = \frac{\lambda \sqrt{\eta^2 - (NA)^2}}{(NA)^2} + \frac{250}{M^2}$$

Electron Microscope

$$d = \frac{0.1 \text{ mm}}{M \alpha}$$

λ = wavelength

η = refractive index

α = semi angle

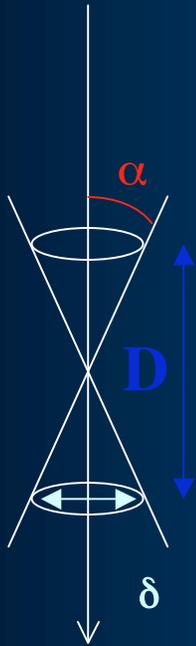
M = total magnification

NA = Numerical Aperture of lens

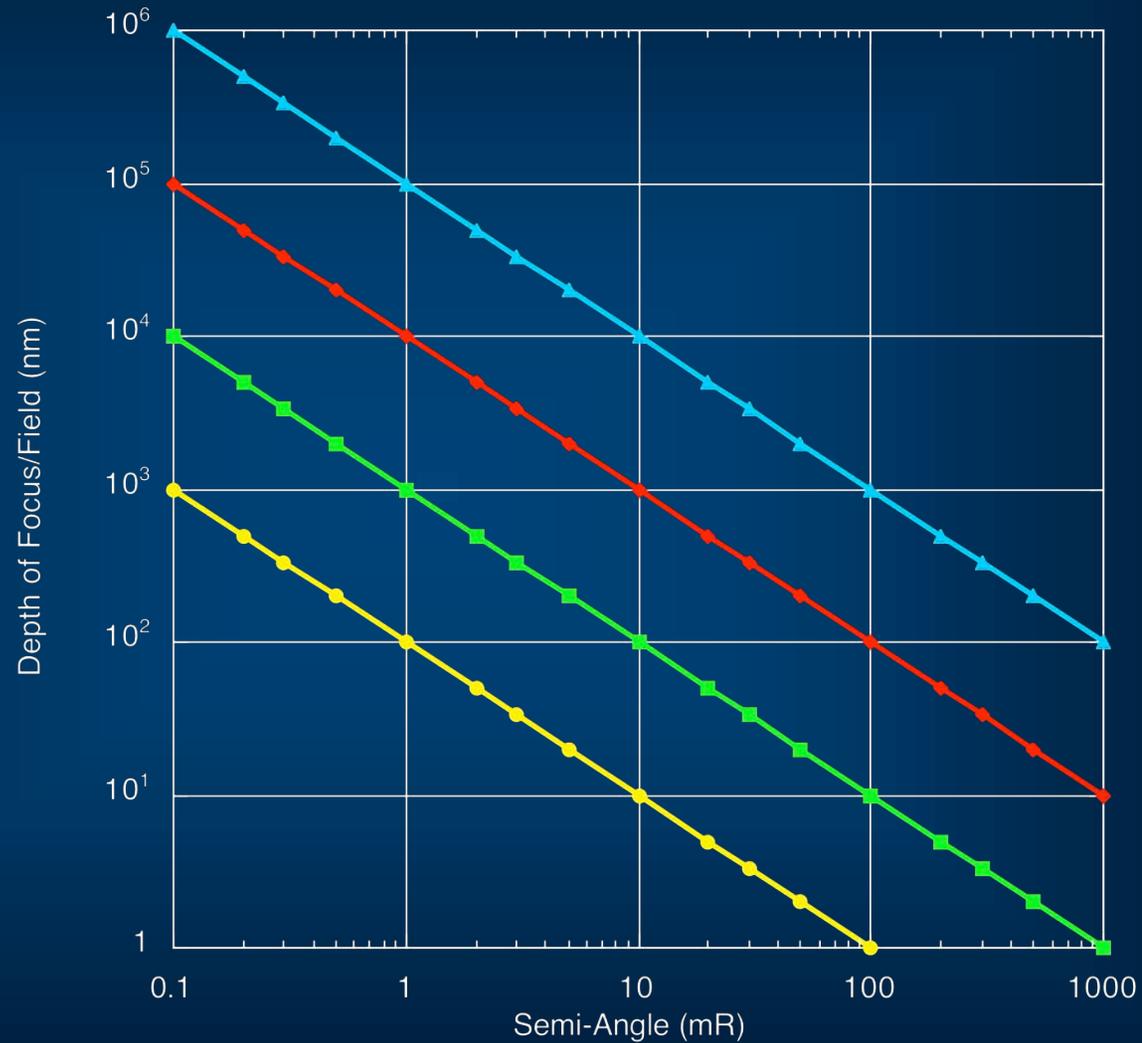
Depth of Focus

Magnification	Depth of Focus	
	Optical	SEM
10	60 μm	1000 μm
100	8 μm	100 μm
1,000	0.2 μm	10 μm
10,000	-	1 μm

Depth of Focus (Specimen Plane) Pre Specimen Semi-Angles

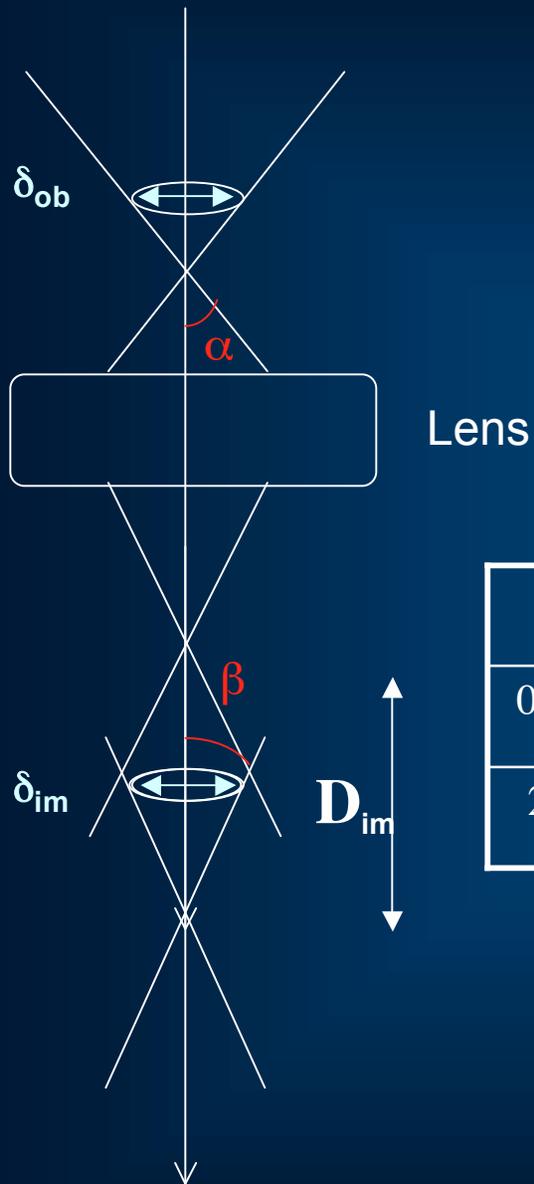


$$D = \frac{\delta}{\alpha}$$



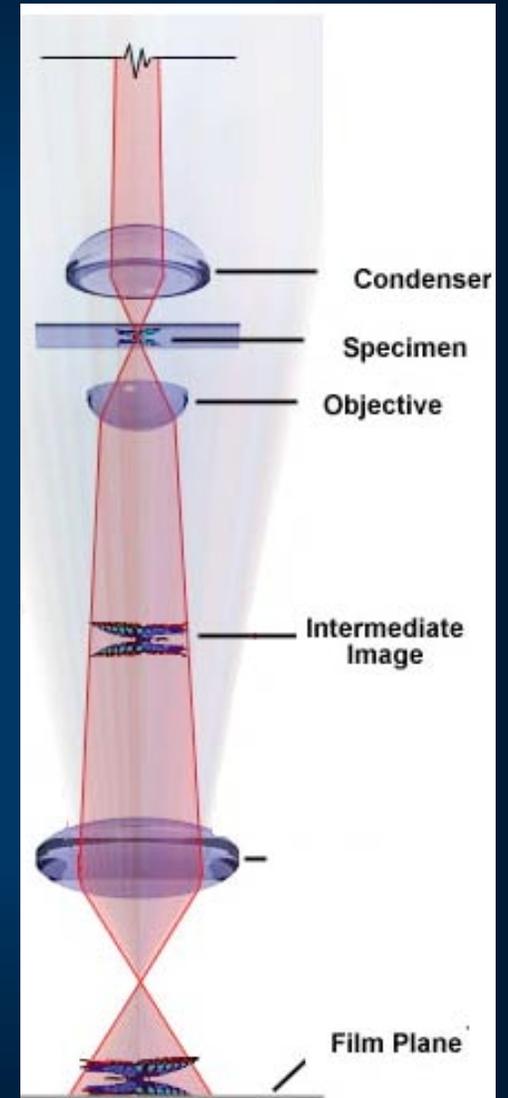
In an EM α is controlled by both Apertures & the Lens Magnification

Depth of Field (Image Plane) Post Specimen Semi-Angles



$$D_{im} = \frac{\delta_{im}}{\beta} = \frac{\delta_{ob}}{\alpha} M^2$$

δ_{ob}	α	M	D_{im}
0.2 nm	10 mR	500kX	5 km
2 nm	10 mR	50kX	5 m



Basic Components of All Microscopes That Use Lenses

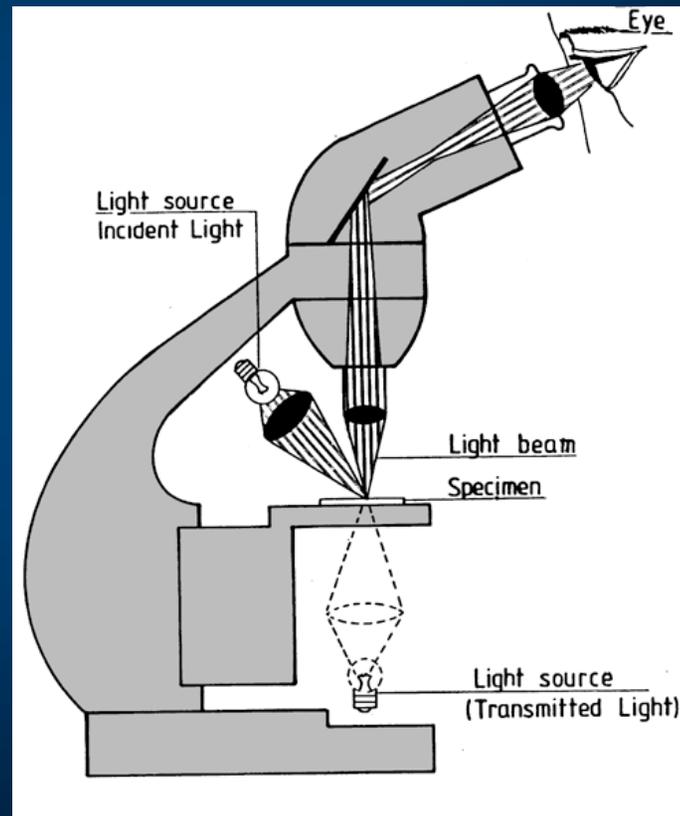
Illumination Source

Illumination Lens

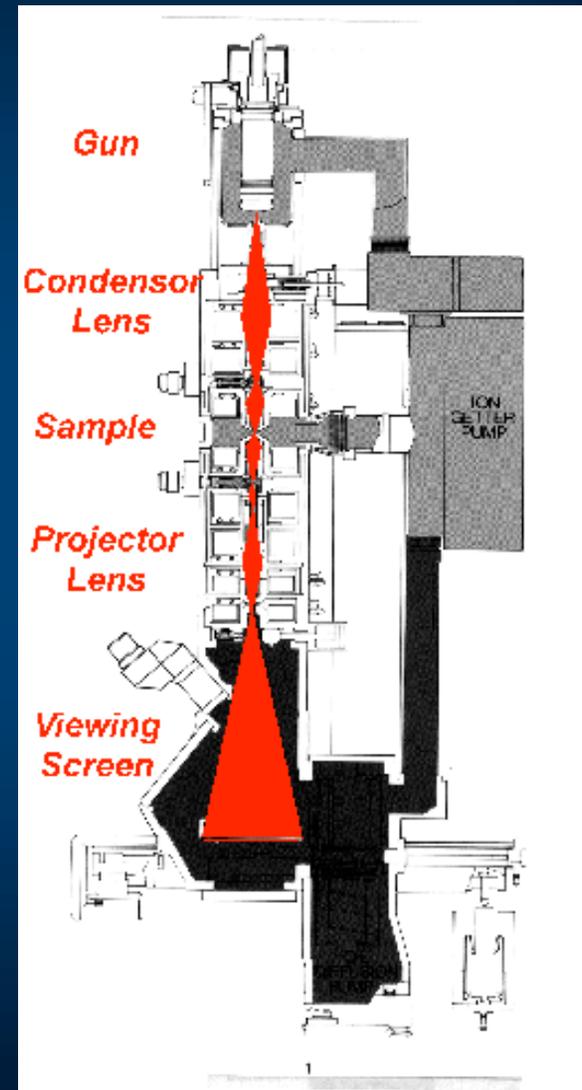
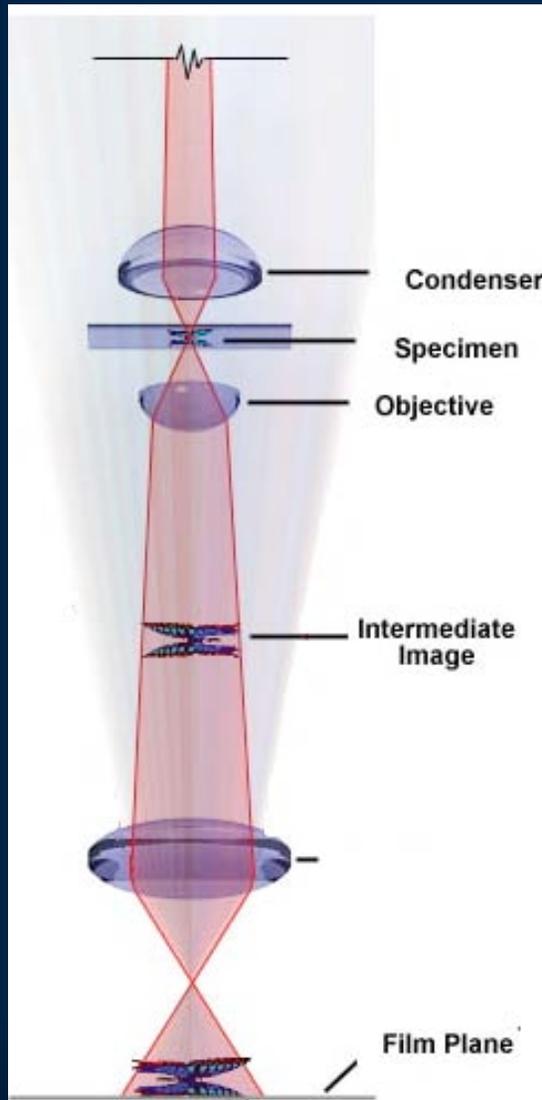
Specimen

Magnifying Lens

Detector/Viewer



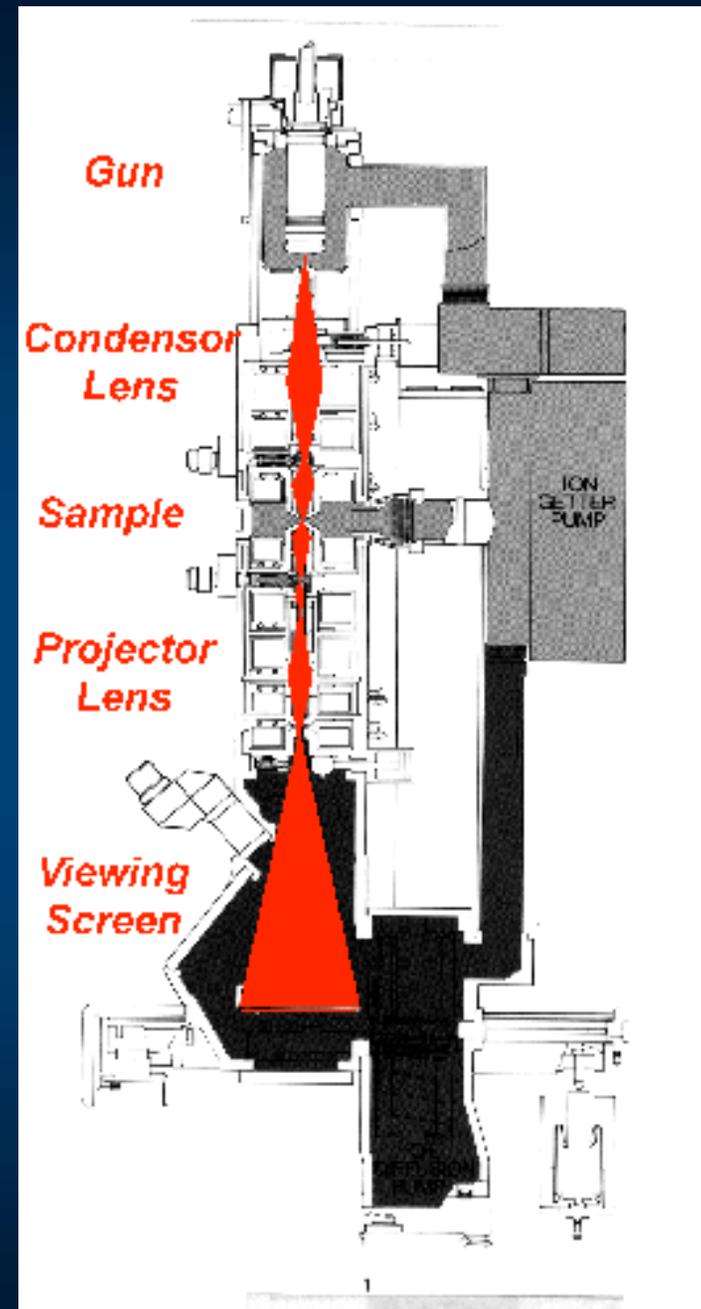
Transmission Electron Microscope



Basic Components of an Electron Microscope



Transmission Electron Microscope



Basic Components of All Microscopes That Use Lenses

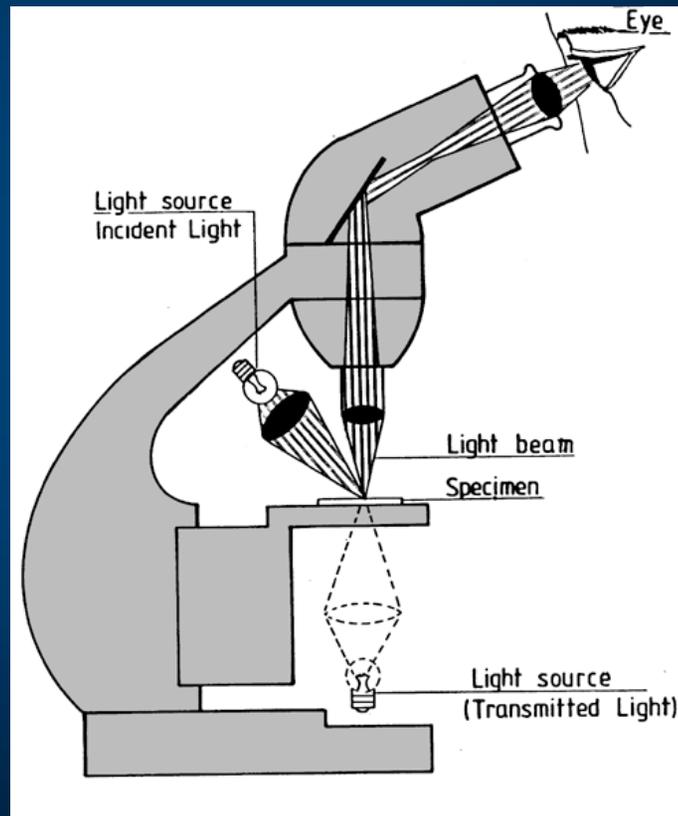
Illumination Source

Illumination Lens

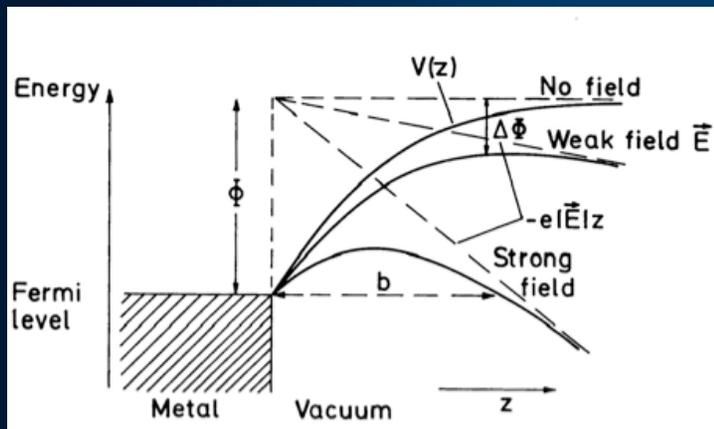
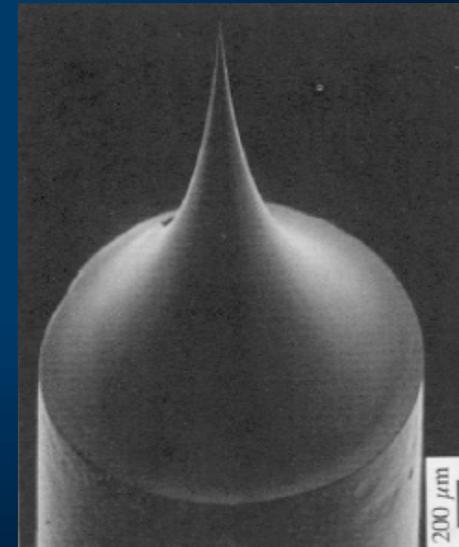
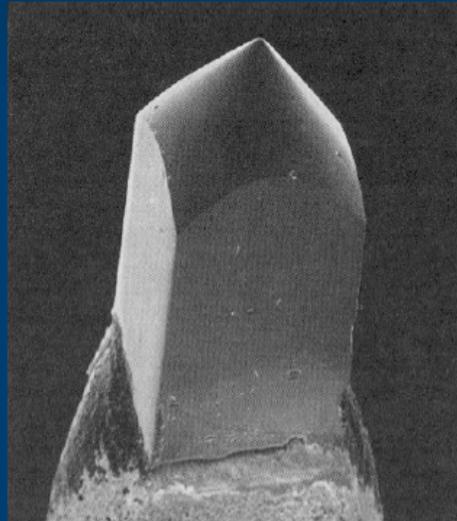
Specimen

Magnifying Lens

Detector/Viewer



Sources for Electron Microscopy Thermionic, Thermally Assisted, and Field Emission



Conduction electrons must overcome the work function ϕ if they are to be emitted from the cathode into the vacuum.

Thermionic sources

Richardson law gives the current density :

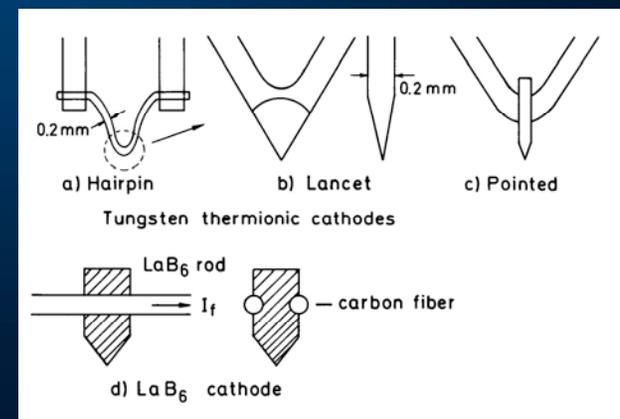
$$j_c = AT_C^2 \exp(-\phi / kT_C)$$

k is Boltzmann's constant, T_C is the cathode temperature and A and ϕ are constants depending on material. Note that $j_c \propto T$.

W has T_C of 2500-3000 K (melting point 3650 K)

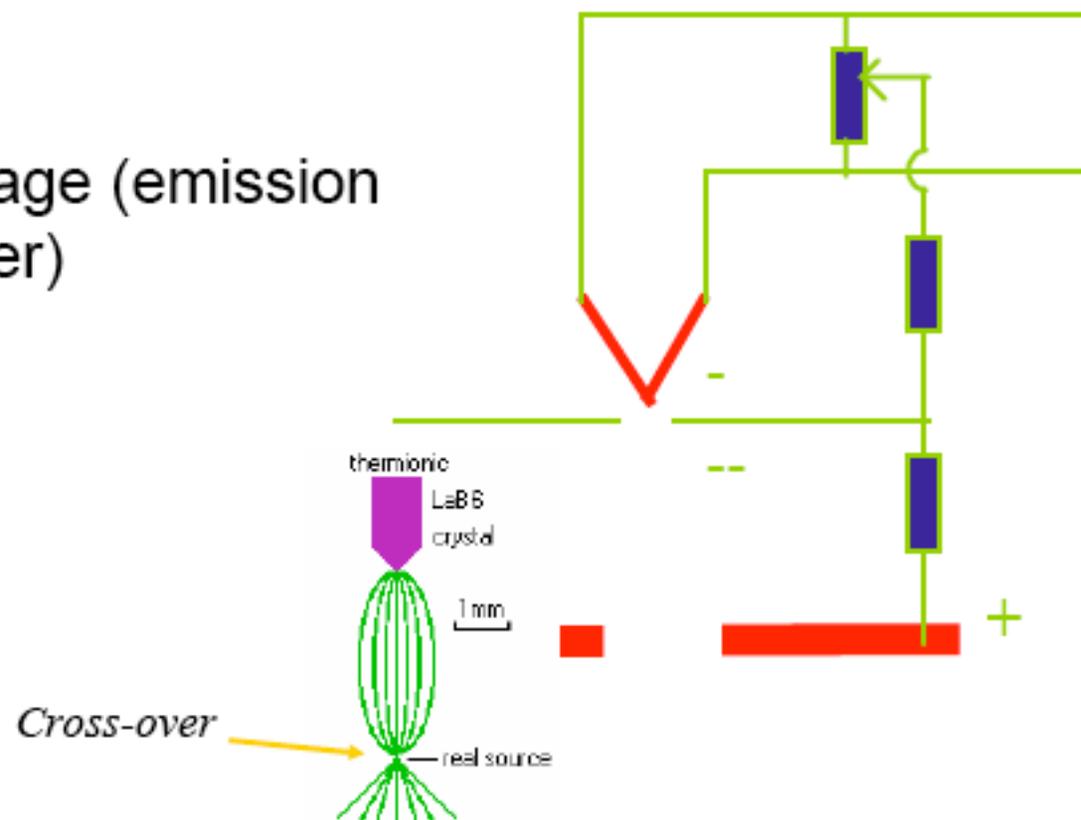
LaB_6 has a T_C of 1400-2000 K

Heating usually produced by running a current through the material!



Electron Source Thermionic Gun

- Filament
- Wehnelt
 - bias voltage (emission parameter)
- Anode

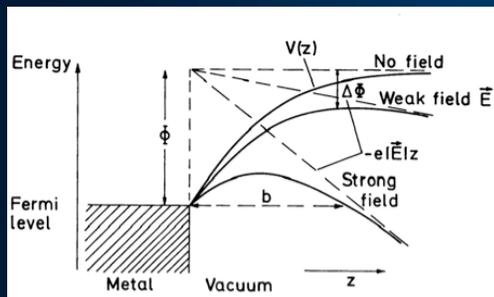


Field emission and Schottky sources

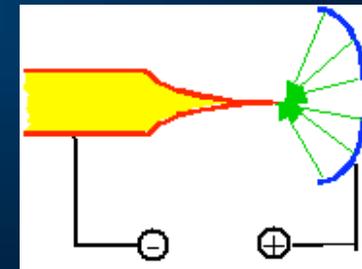
The width b of the potential barrier at the metal-vacuum boundary decreases with increasing electric field \mathbf{E} .

For $|\mathbf{E}| > 10^7$ V/cm the width $b < 10$ nm and electrons can penetrate the potential barrier by the wave mechanical tunneling effect.

The current density of field emission can be estimated from the Fowler-Nordheim formula:

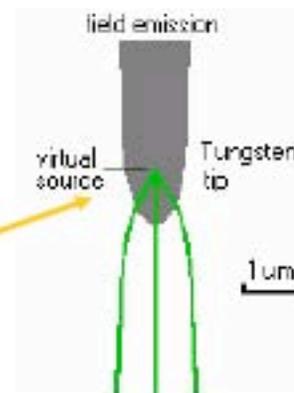
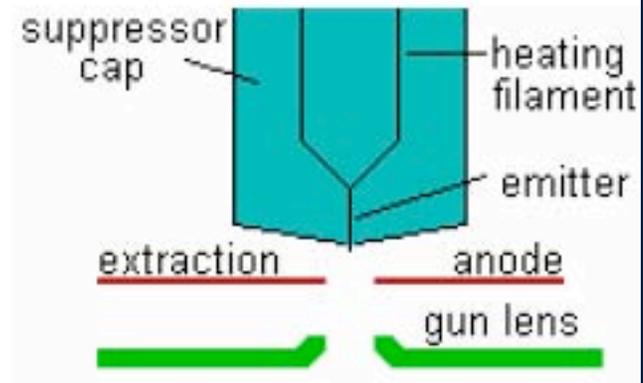


$$j = \frac{k_1 |\mathbf{E}|}{\phi} \exp\left(\frac{k_2 \phi^{3/2}}{|\mathbf{E}|}\right)$$

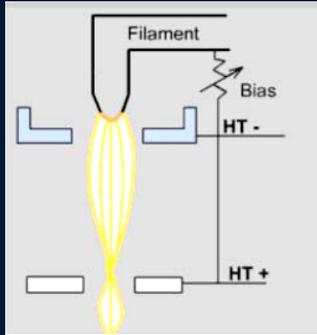


Field Emission Gun (FEG)

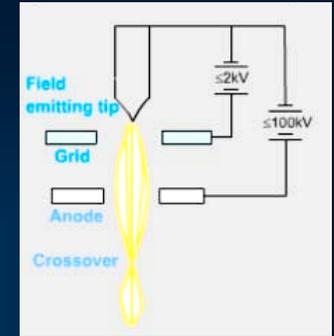
- Heating Filament
- Single Crystal Emitter
- Suppressor Cap
- Extraction Anode
- Electrostatic lens



Electron seemingly originating from tip itself



Sources for Electron Microscopy: Thermionic, Thermally Assisted, and Field Emission



Comparison of Electron Sources

Type		Brightness β/V_0 A/cm ² /sr/eV	Source Size (μm)	Energy Spread (eV)	Temporal Coherence (μm)	Shot Noise	Current Stability	Spatial Coherence	Vacuum (Torr)
Thermionic	Hairpin	1	50	2-3	0.4	Low	Good	Low	$<10^{-4}$
	Pointed	5	10				Fair	Moderate	$<10^{-5}$

$$\text{Temporal Coherence} = 2 E \lambda / \Delta E$$

$$\text{Spatial Coherence} = \lambda / 2\alpha$$

Comparison of Electron Sources

	W	LaB₆	FEG (Schottky)
Maximum Current (nA)	1000	500	300
Normalised Brightness (-)	1	10-30	2500
Energy spread (eV)	3-4	1.5-3	0.6-1.2
Source spotsize	30-100 μm	5-50 μm	15-30 nm
Required Vacuum (Pa)	10^{-3}	10^{-5}	10^{-7}
Temperature (K)	2700	2000	1800
Life time (hr)	60-200	1000	>2000
Normalised Price (-)	1	10	100

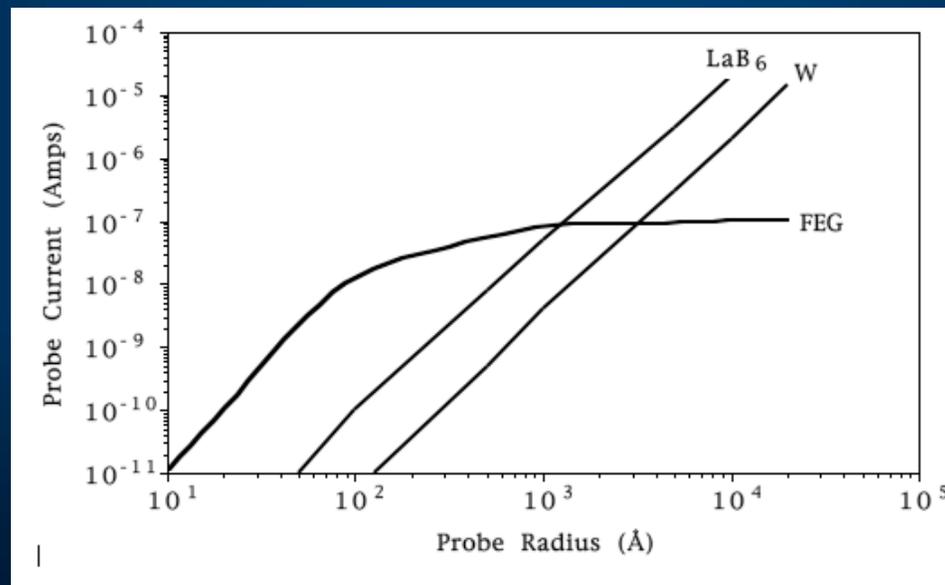
Probe Current Related Parameters

$$J = \text{Probe current} = \frac{(\pi d_0 \alpha_0)^2 \mathcal{B}}{4}$$

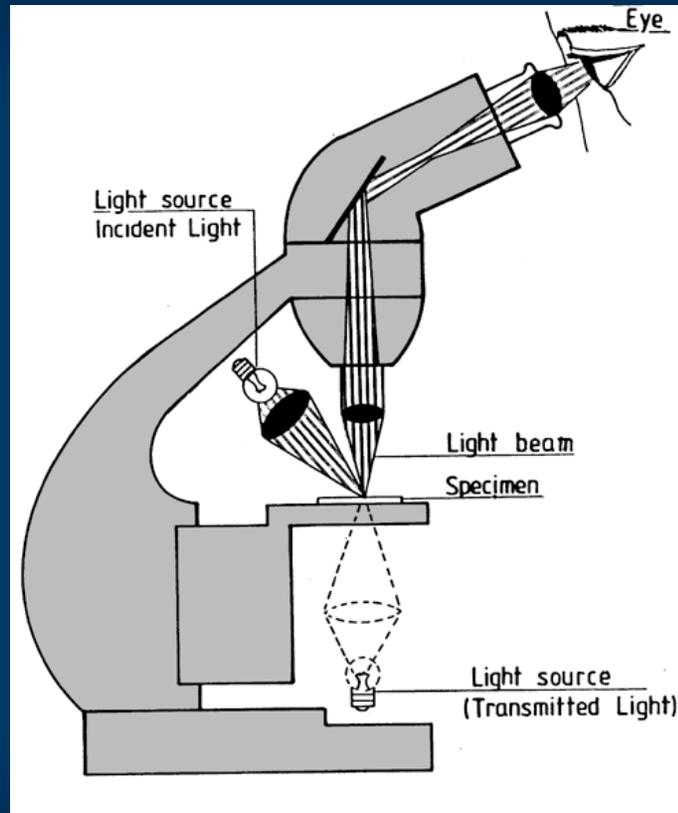
$$\mathcal{B} = \text{Brightness} = \left(\frac{J_c}{\pi k T} \right) e V_r$$

$$V_r = \text{Relativistic Voltage} = V_0 \left(1 + \frac{e V_0}{2 m_0 c^2} \right)$$

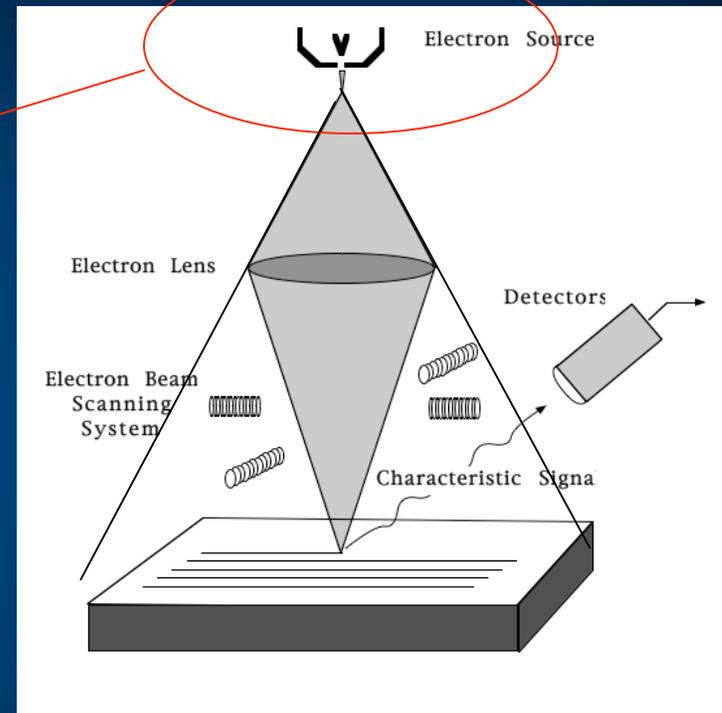
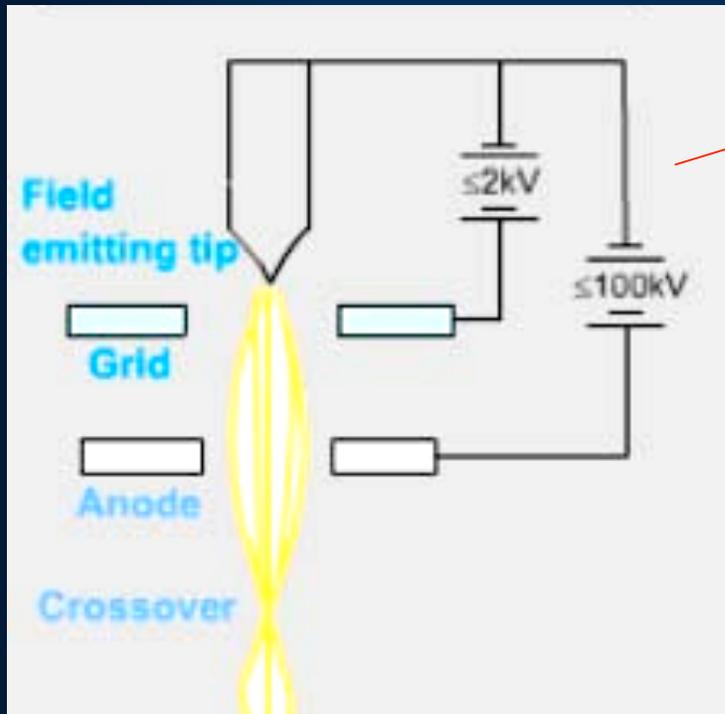
$$V_0 (1 + 9.785 \times 10^{-7} V_0)$$



Why do we need a lens?



Why do we need a lens?



Because all electron sources generally produce a diverging beam of electrons. This beam must be "focussed" onto the specimen, to increase the intensity and thus to making the probe "smaller".

Basic Components of All Microscopes That Use Lenses

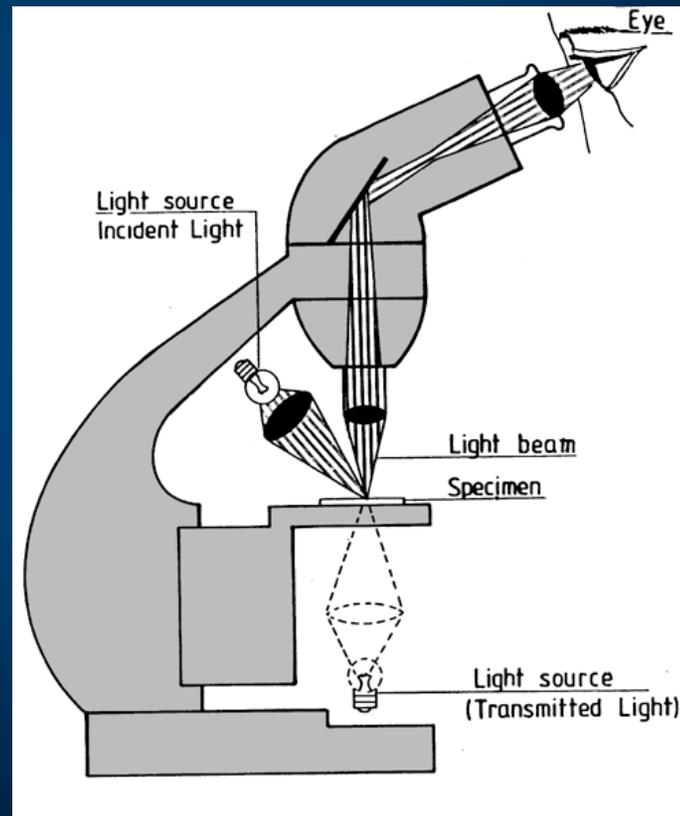
Illumination Source

Illumination Lens

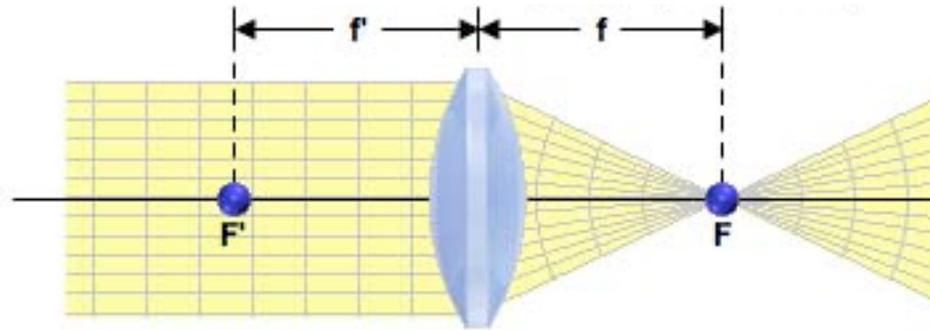
Specimen

Magnifying Lens

Detector/Viewer



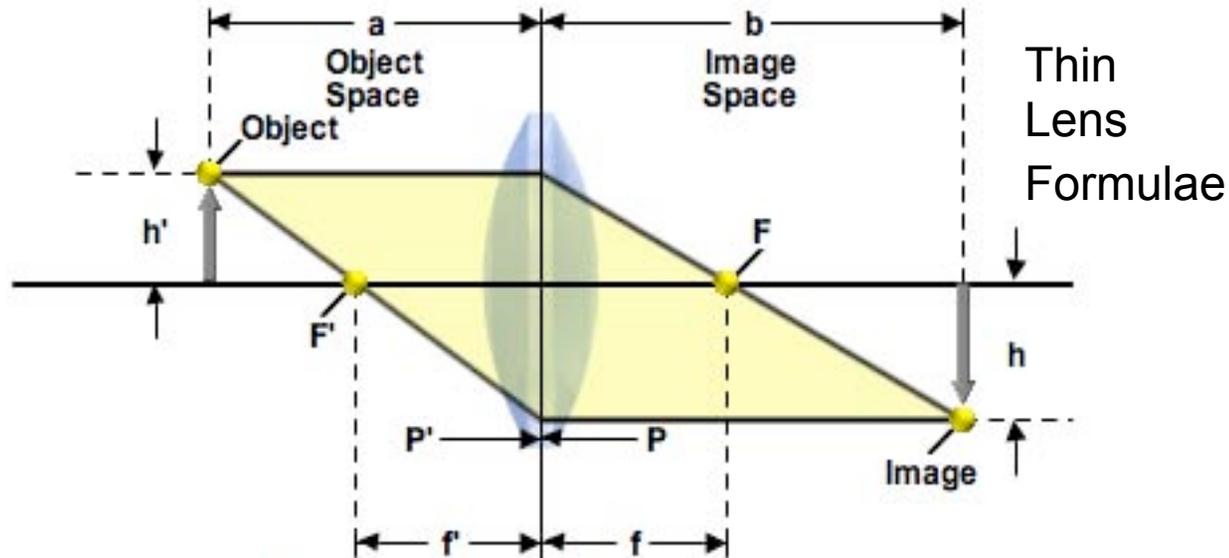
What is a Lens?



It is a device which focuses radiation.

f = focal length of the lens

How Does a Converging Lens Work as a Magnifier?



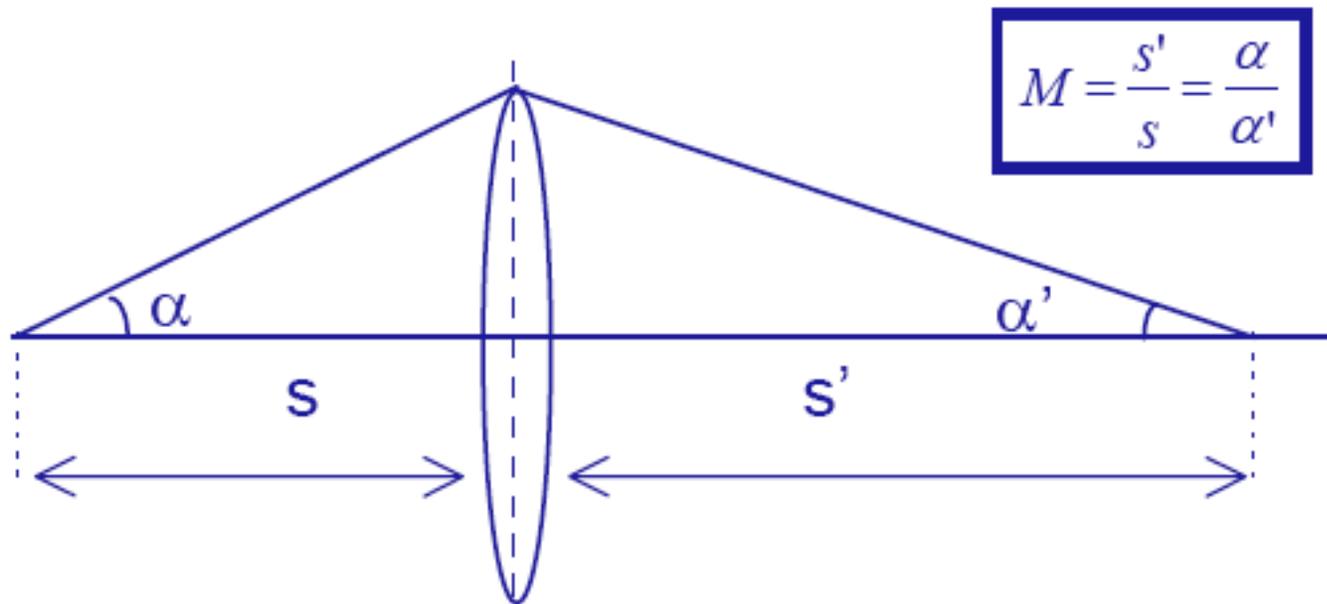
$$\frac{1}{f} = \frac{1}{a} + \frac{1}{b}$$

$$M = \frac{h}{h'} = -\frac{b}{a}$$

In a TEM the function of lens are to either demagnify the probe from the source point to the sample. This means that $b < a$ resulting in a smaller electron probe. It's 2nd role as a post specimen lens is magnify an image hence $b > a$

Lenses

- Gaussian Law

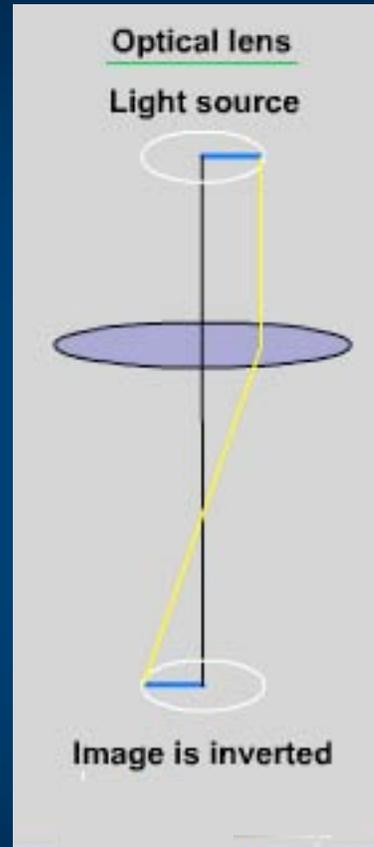


Lenses and Magnification

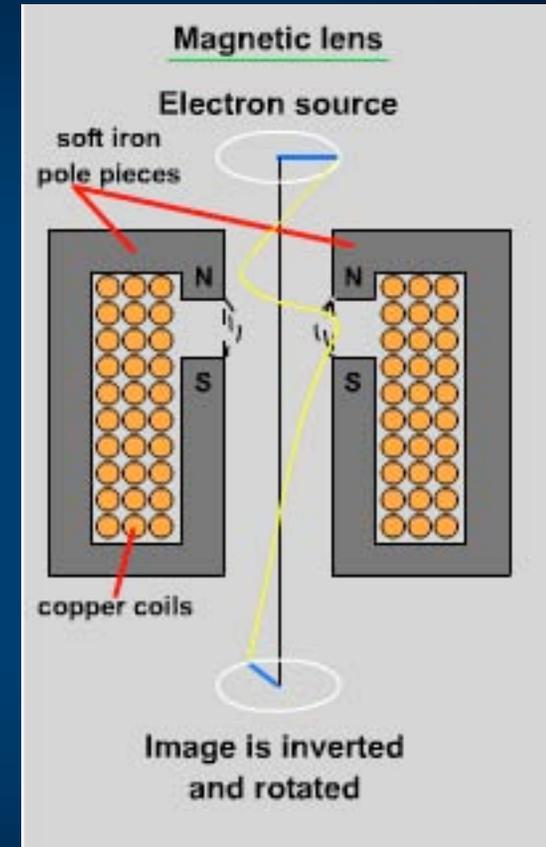
$$\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i}$$

$$M = -\frac{d_i}{d_o}$$

Thin Lens
Formulae



Focus achieved
using Refraction



Focus achieved
using Lorentz Force

Electron Lenses

Electrons are charged particles and are influenced by Electromagnetic Fields. Lenses in an TEM/STEM utilize either or combinations of Magnetic and Electrostatic Fields to direct the beams as desired.

Force (F) and displacements (X) on electrons by different types of fields yields a deflection in their trajectory. In a uniform field region the electrons drift at a characteristic radius (R).

Electrostatic

$$\vec{F}_E = q \vec{E}$$

$$X_E = \frac{1}{2} \frac{qEL^2}{m_0v^2}$$

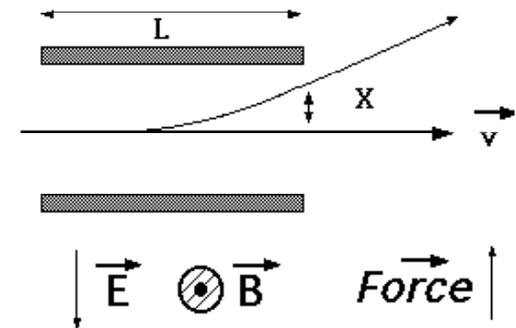
$$R_E = \frac{m_0v^2}{qE}$$

Electromagnetic

$$\vec{F}_B = q [\vec{v} \times \vec{B}]$$

$$X_B = \frac{1}{2} \frac{qBL^2}{m_0v}$$

$$R_B = \frac{m_0v}{qB}$$

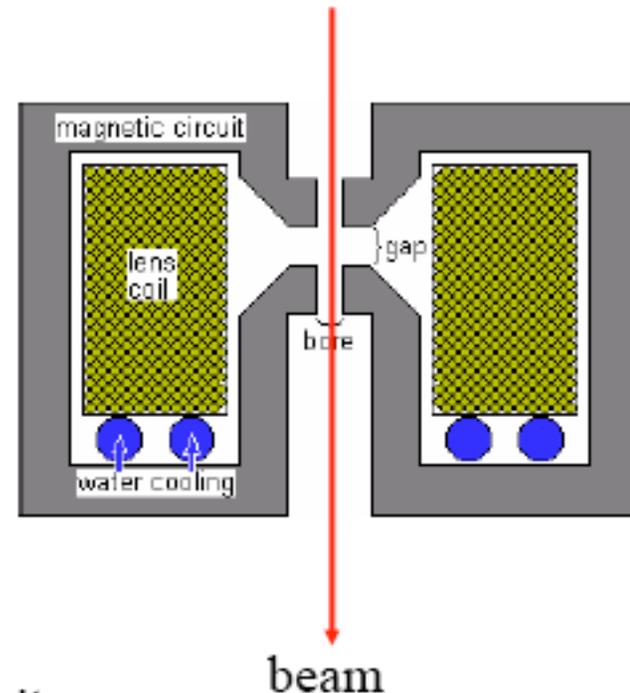


Lenses

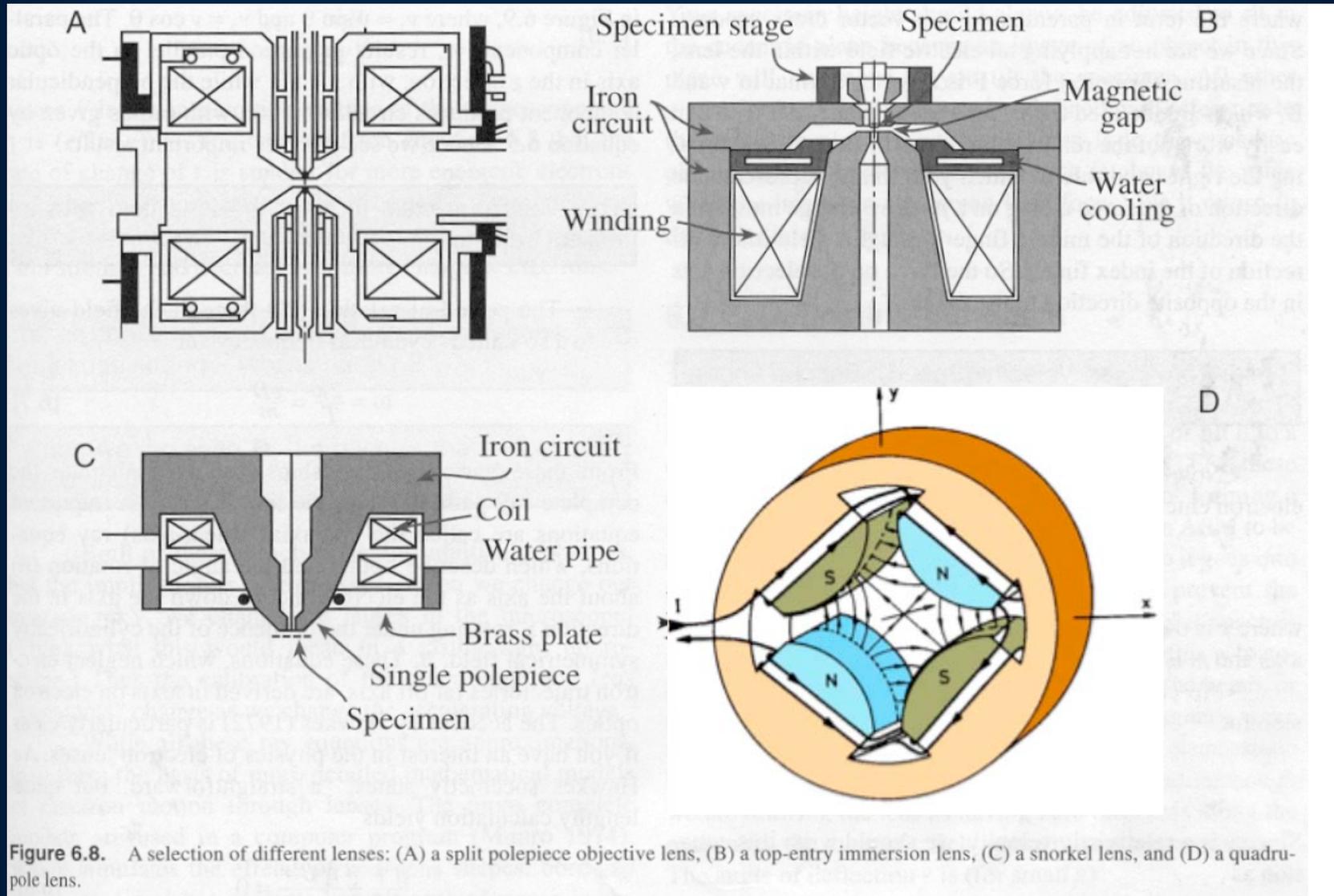
- the focal length is given by:

$$f = \frac{K \cdot U}{(N \cdot I)^2}$$

- K : constant
U : accelerating voltage
N : windings
I : lens current

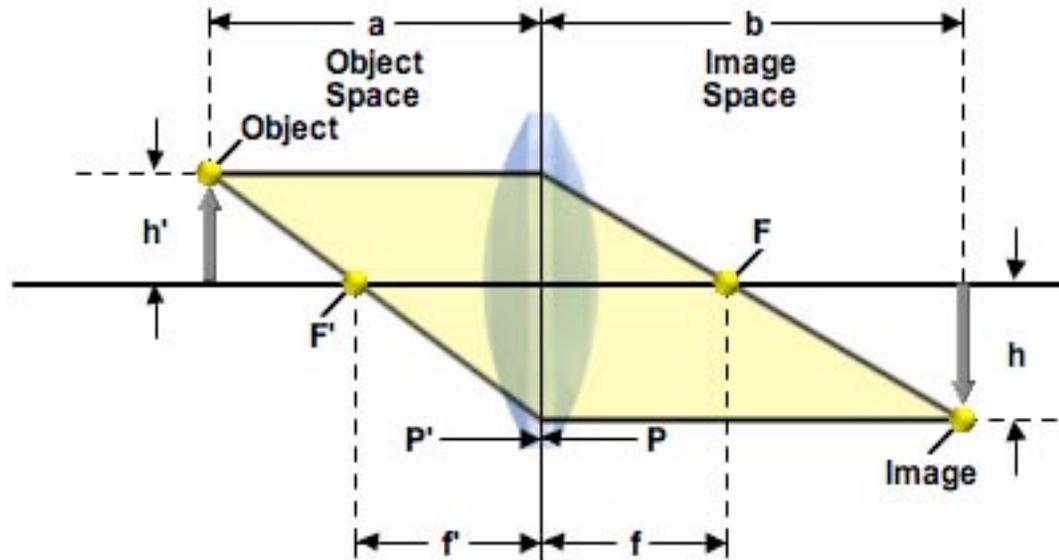


Types of Electron Lenses



Condenser Lenses ~ Type A, Objective Lenses ~ Type A B or C, Stigmators Type D

How Does a Lens Work as a Magnifier?



$$\frac{1}{f} = \frac{1}{a} + \frac{1}{b}$$

$$M = \frac{h}{h'} = -\frac{b}{a}$$

In a TEM the function of lens are to either demagnify the probe from the source point to the sample. This means that $b < a$ resulting in a smaller electron probe. Or to Magnify an Image $b > a$

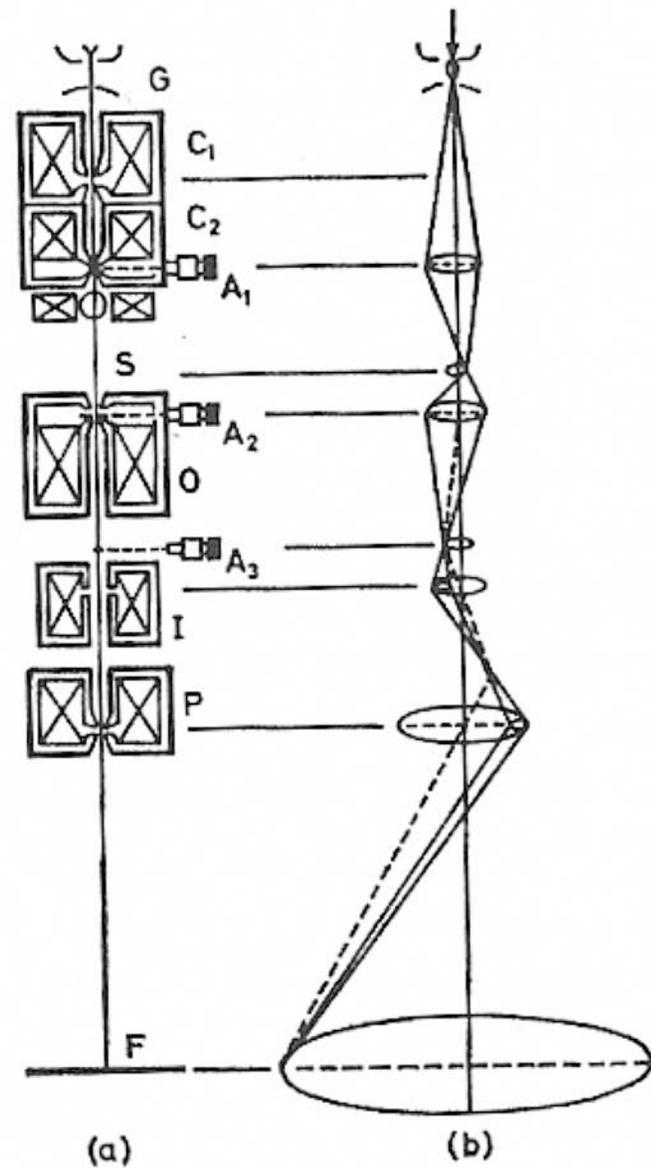
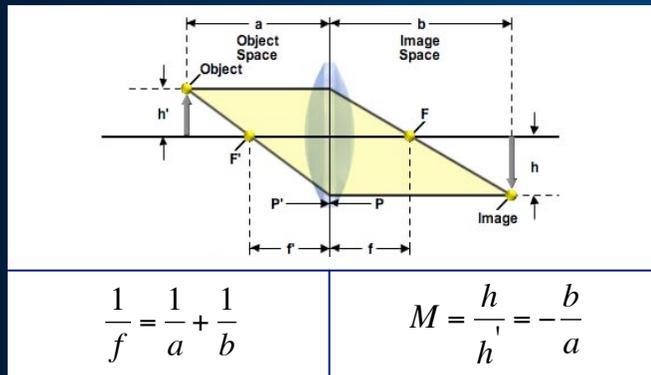
Magnification is achieved by

Stacking Lenses

$$M = M_1 * M_2 * M_3$$

How Accurate is M ?

What are the limiting Factors?



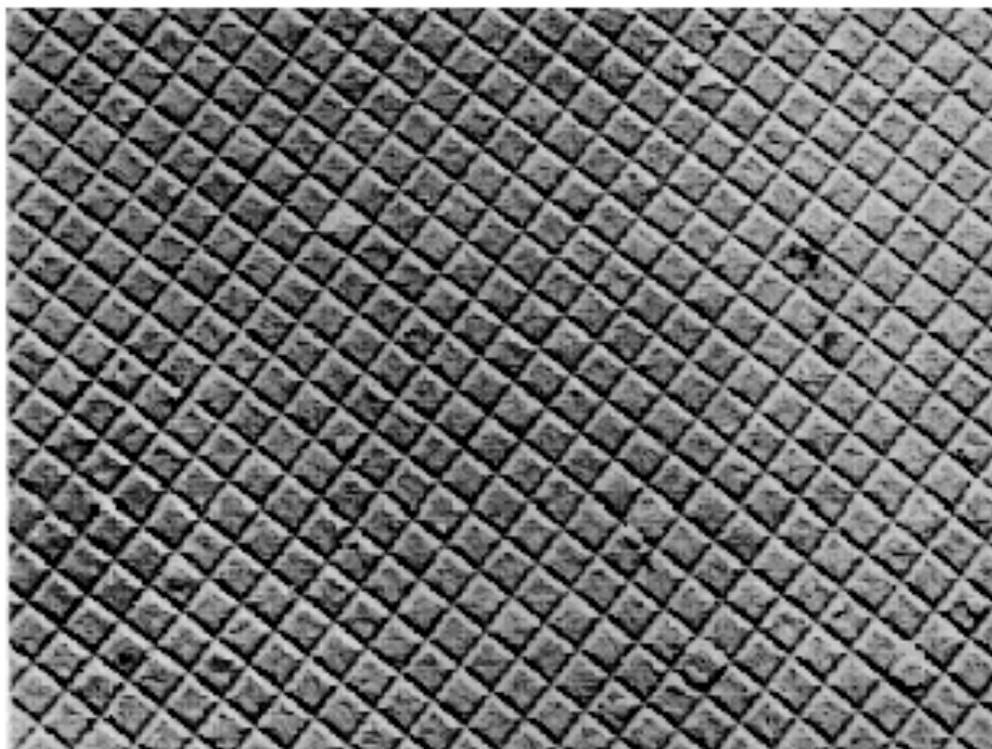
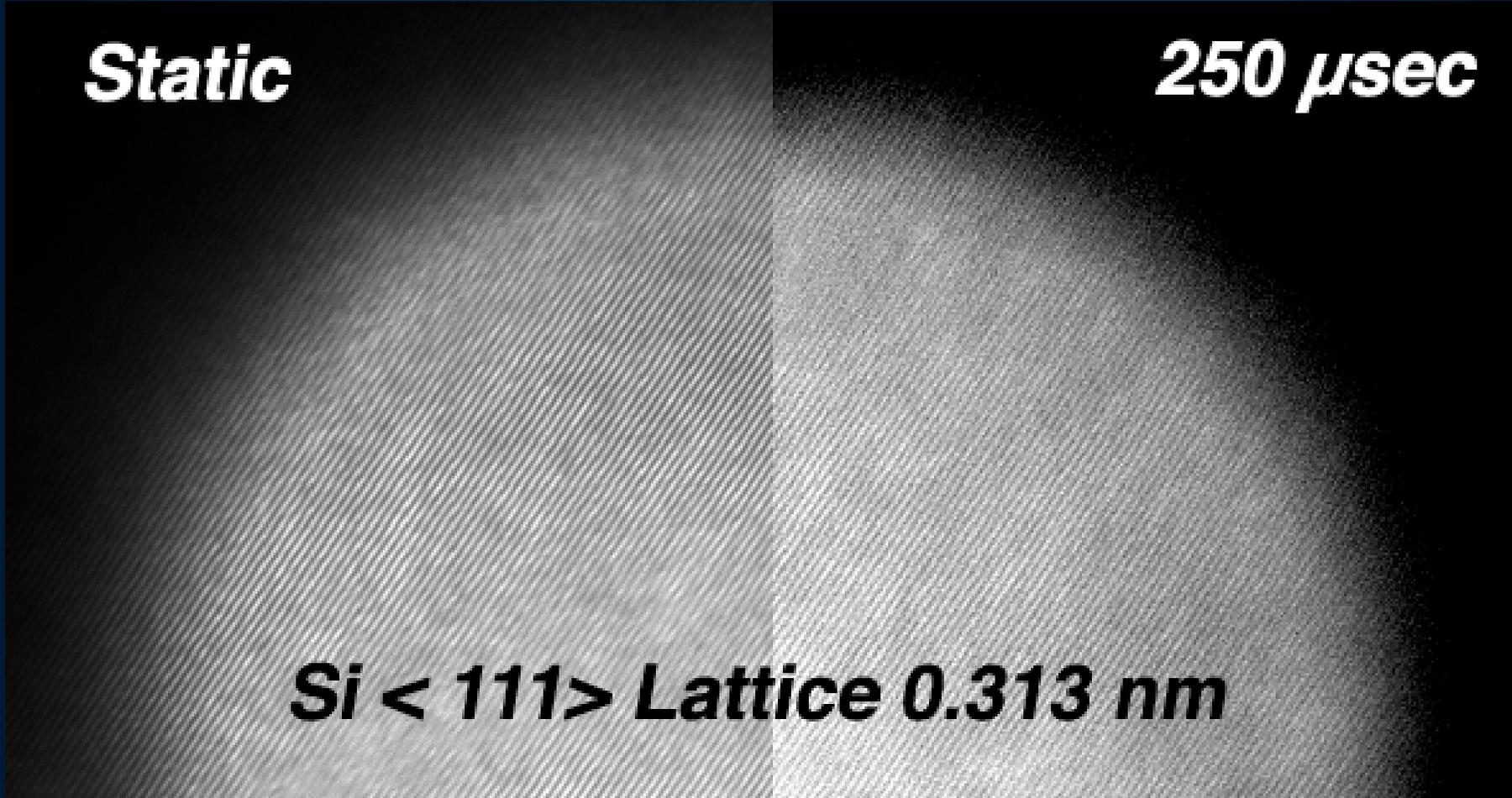


Fig. I.130. Replica of cross-ruled diffraction grating with 2160 lines/mm used as a calibration specimen. (From Agar, p.162)

Static

250 μ sec

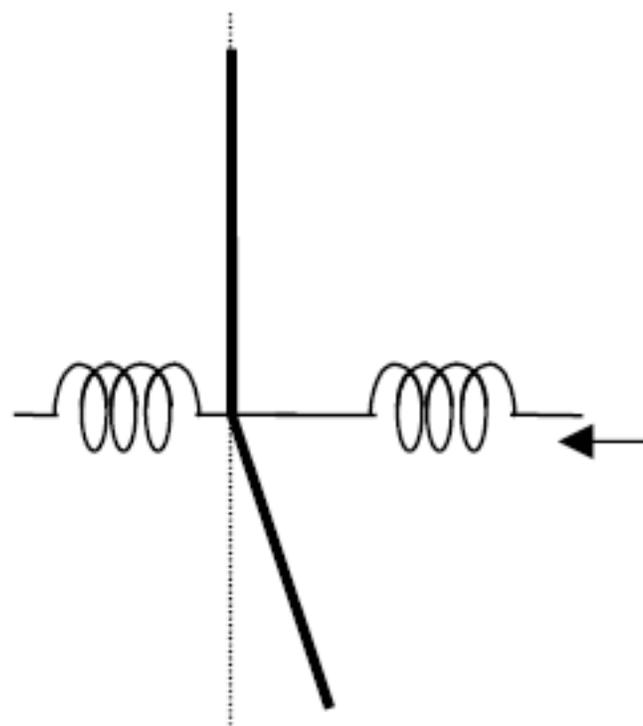
Si $\langle 111 \rangle$ Lattice 0.313 nm



Deflection Coils

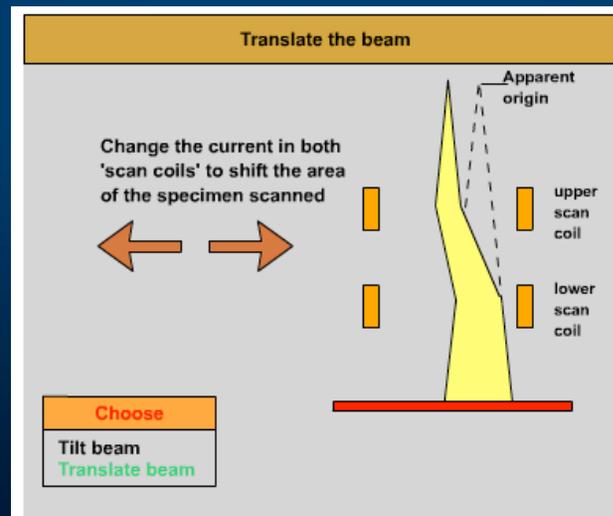
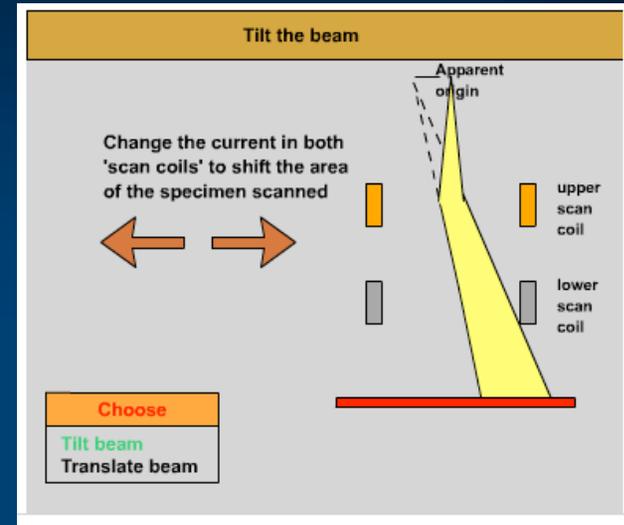
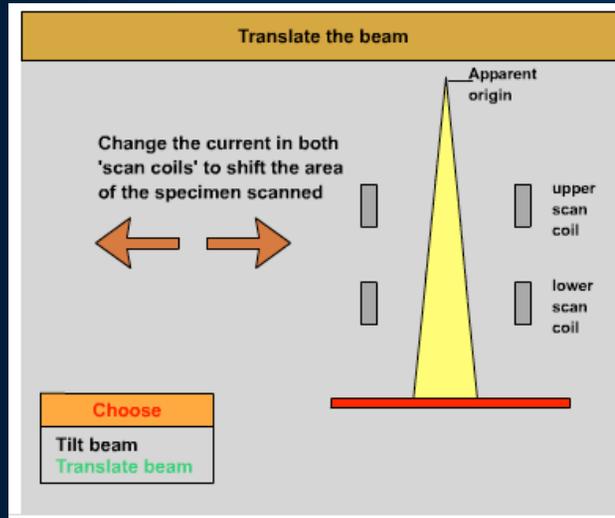
- Basic Principle

- Gun coils
- Beam coils
- Image coils
- Scanning coil
-
-

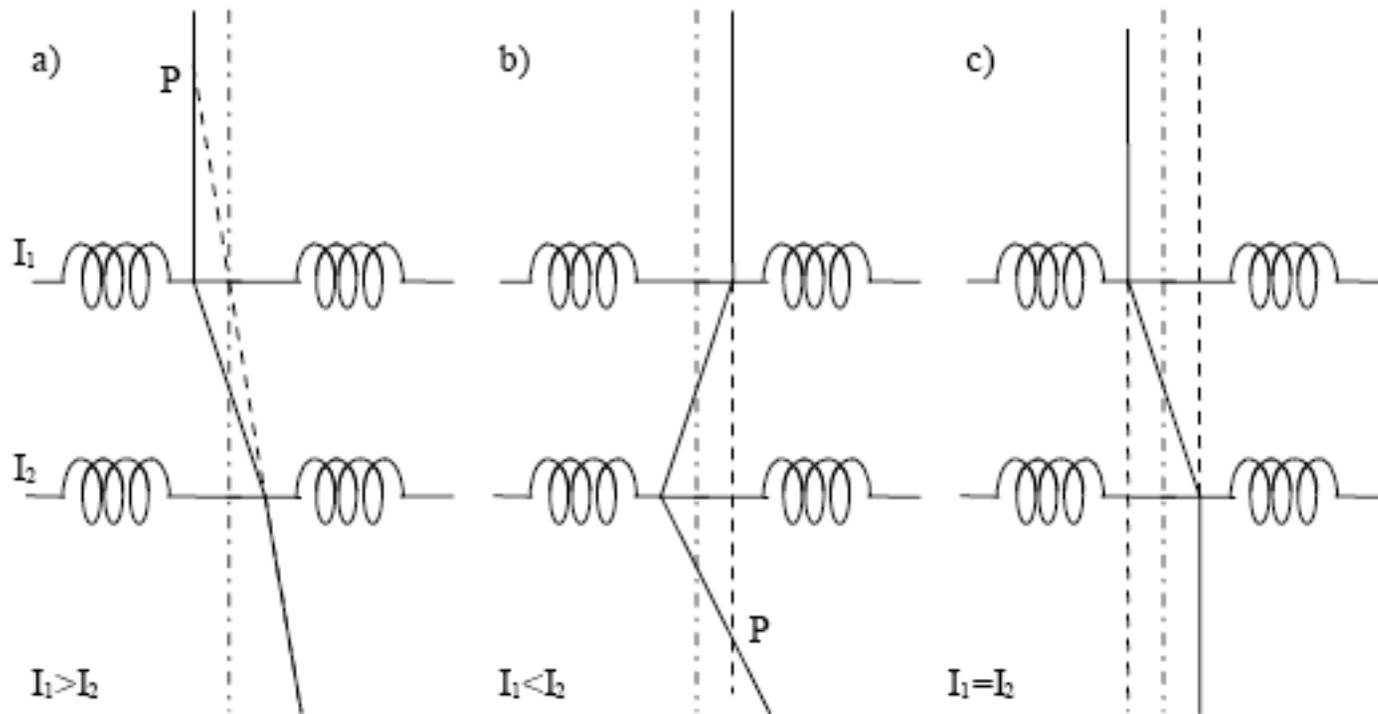


$$\vec{F}_n = q [\vec{v} \times \vec{B}] \quad X_n = \frac{1}{2} \frac{qBL^2}{m_0 v}$$

Alignment/Deflection Coils also use Lorentz Fields but they are not axially symmetric



Deflection Coils

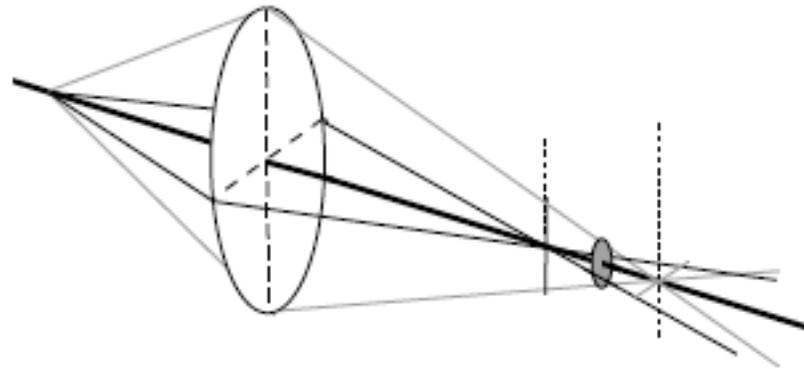


Tilting the Beam

Translating the Beam

Astigmatism

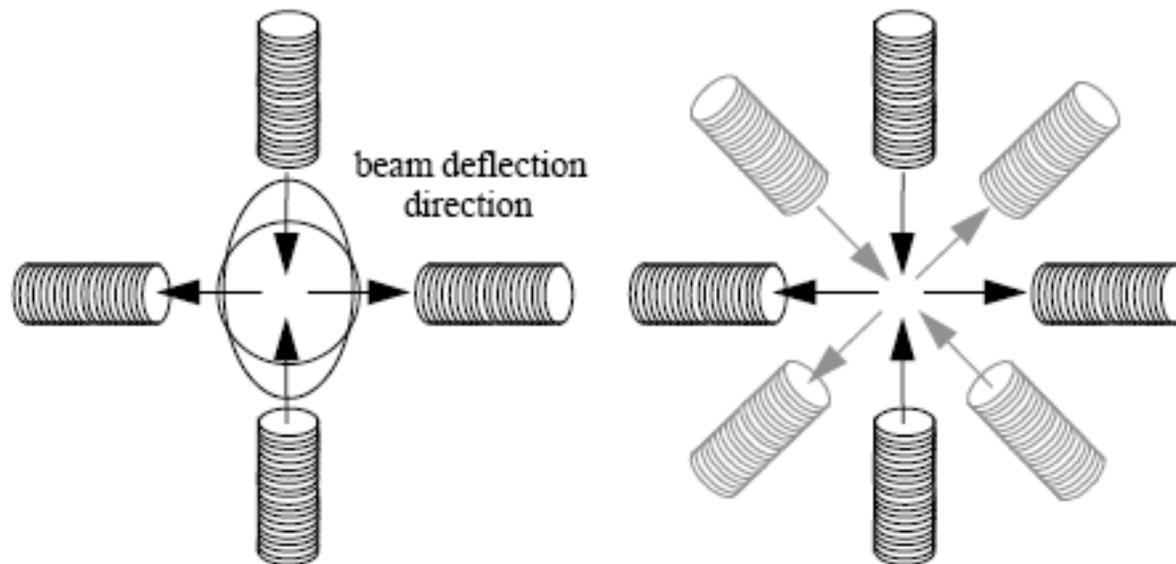
- Lens defect caused by magnetic field asymmetry

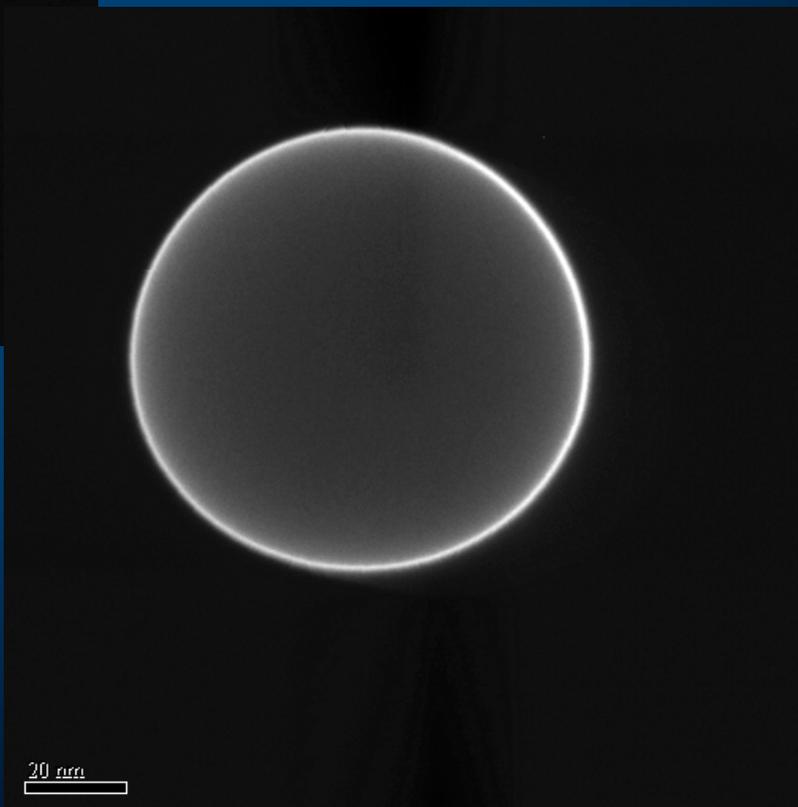
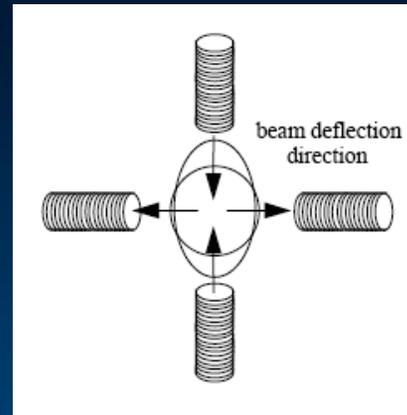
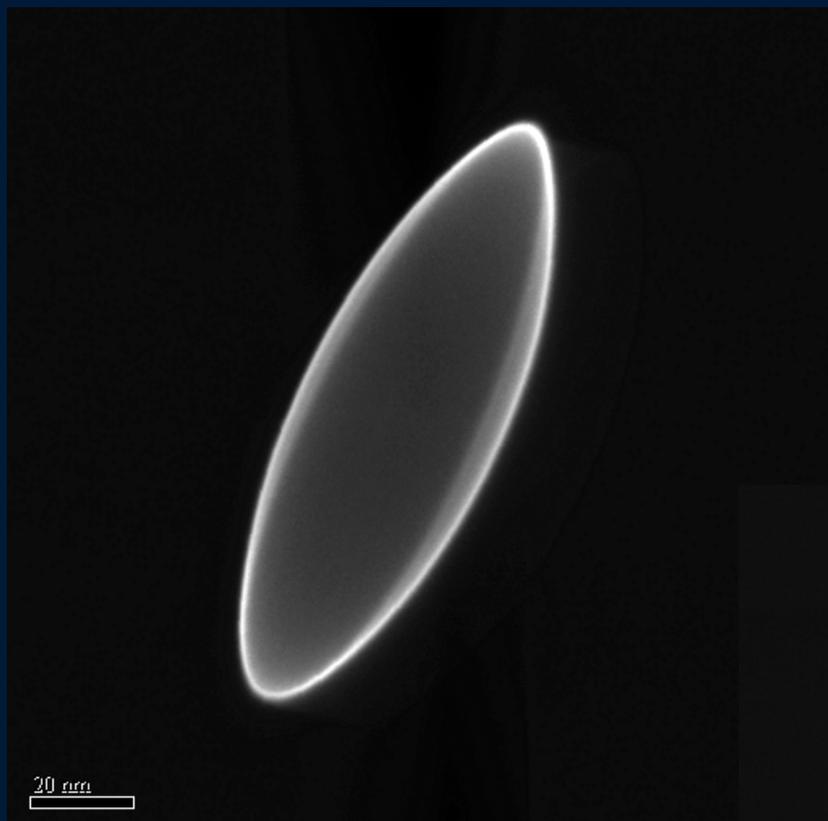


- can be corrected using stigmators!

Stigmators

- Working Principle





Probe Astigmatism

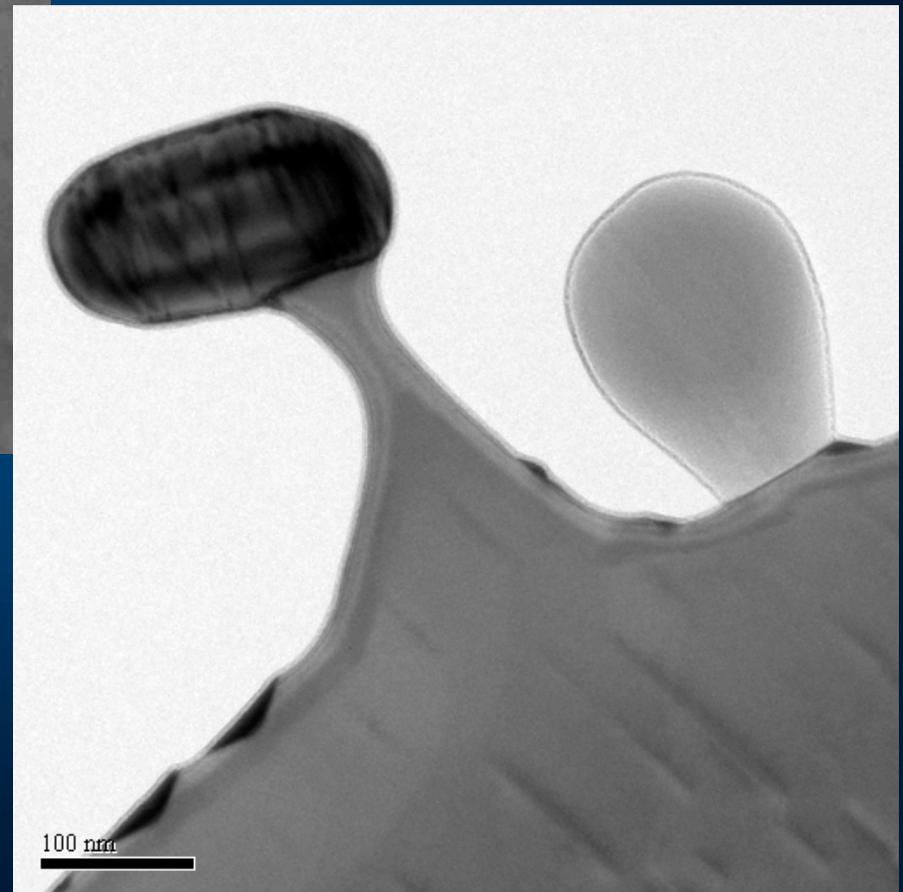
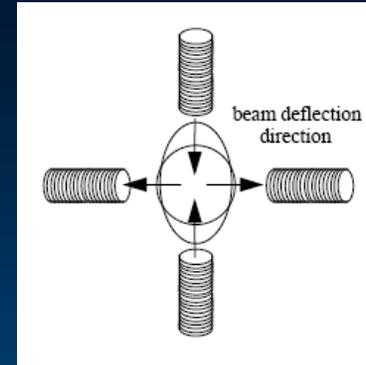
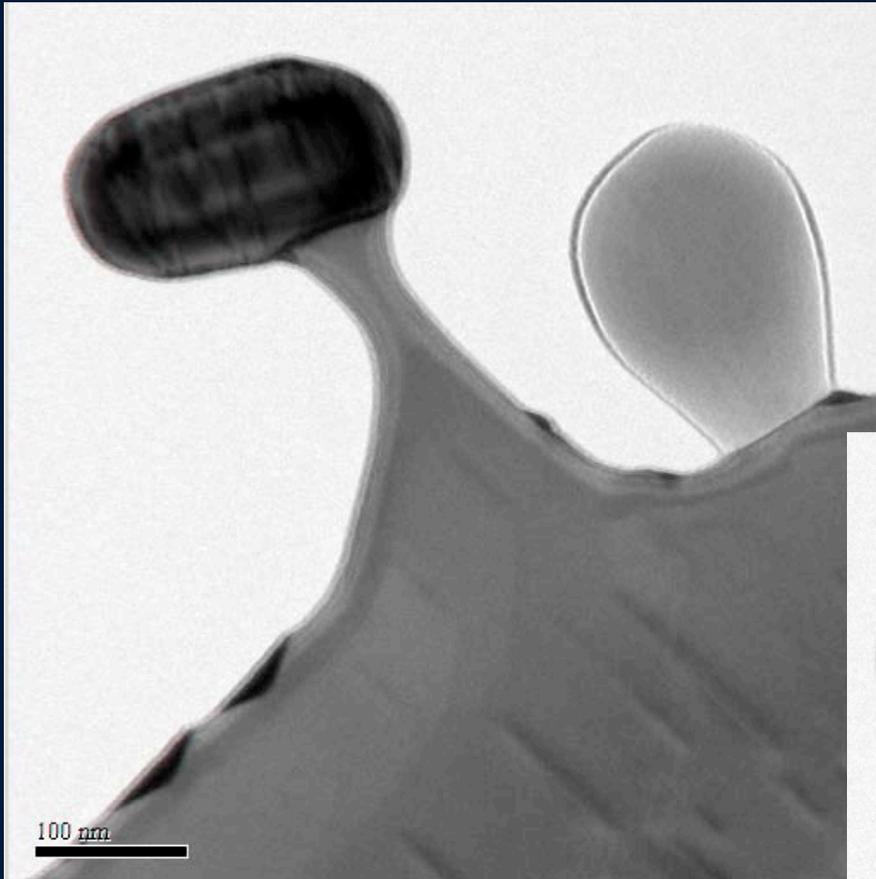


Image Astigmatism

Roles of the Lenses

Gun Lens

Helps form probe

Condenser Lens

Mainly controls:
Spot Size
hence total beam
current

Objective Lens

Mainly controls
Focus, 1st Magnification

Diffraction/Intermediate Lens

Controls Mode

Projector Lens

Magnification



Most TEM/STEM
have 7-8 Lenses

1 Gun Lens
2 Condensers
1 Objective
1-2 Intermediate
1-2 Projectors

Most instruments
have only
Electromagnetic
Round Lenses

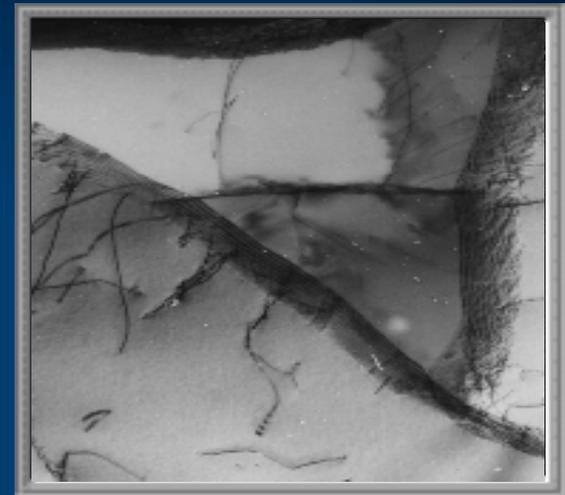
Note the locations
of the various
Apertures.

Optimum aperture
sizes are needed
for various
imaging functions.

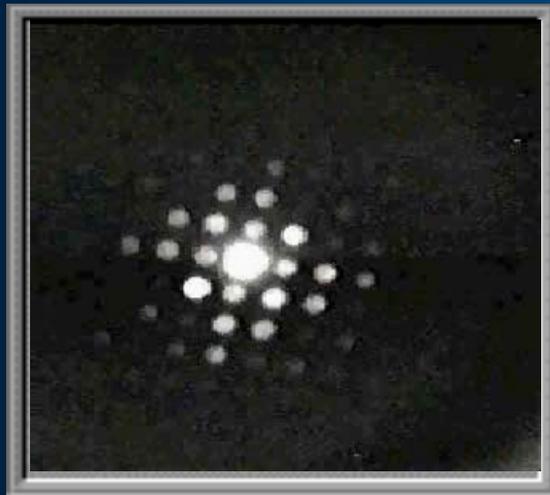
Transmission Electron Microscopy



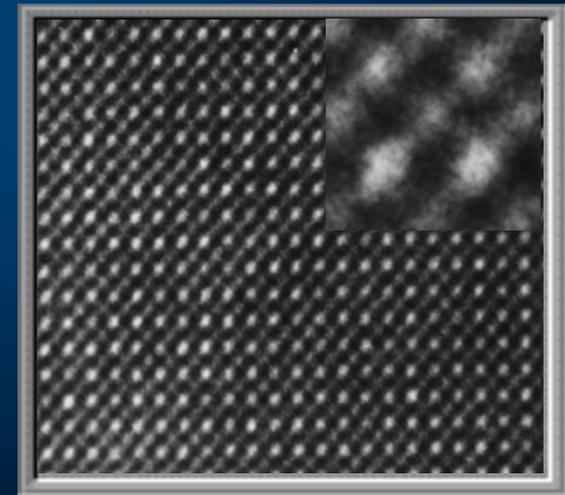
*Conventional
Imaging*



*High
Resolution
Imaging*



Diffraction



Roles of the Lenses

Gun Lens

Helps form probe

Condenser Lens

Mainly controls:
Spot Size
hence total beam
current



Most TEM/STEM
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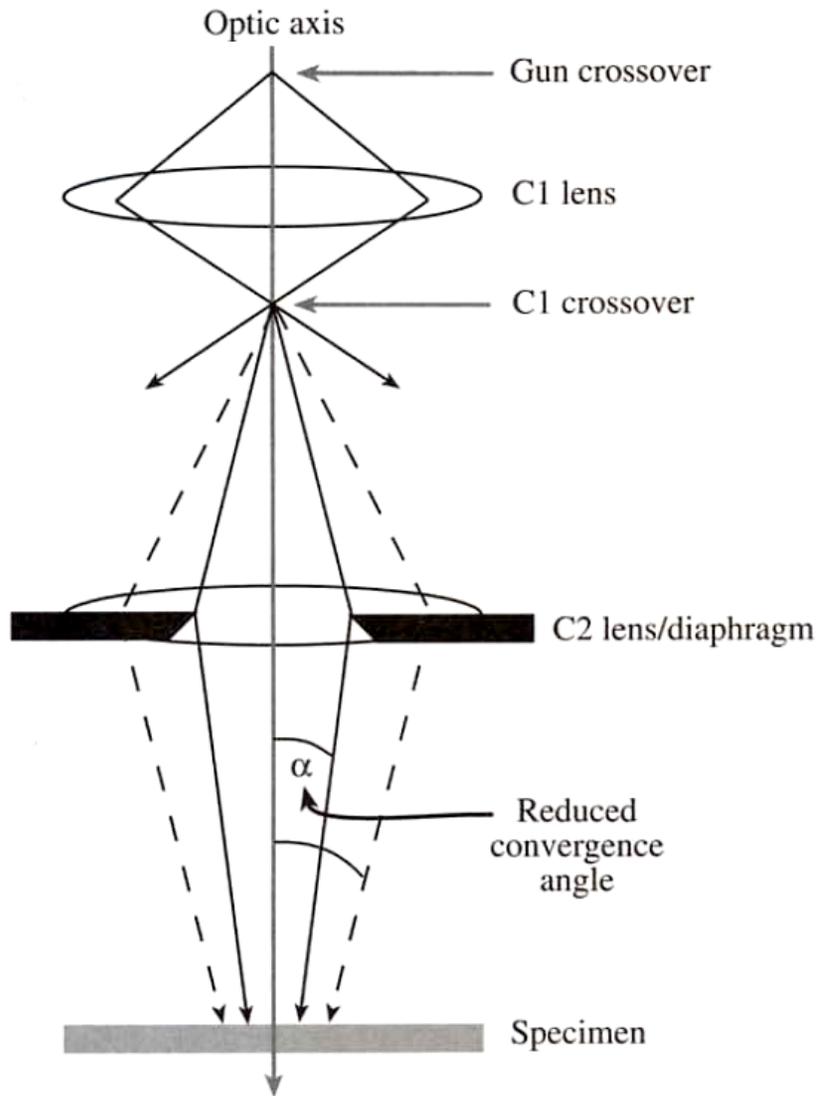


Figure 9.2. Effect of the C2 aperture on the beam coherence: a smaller aperture creates a more parallel, more coherent beam.

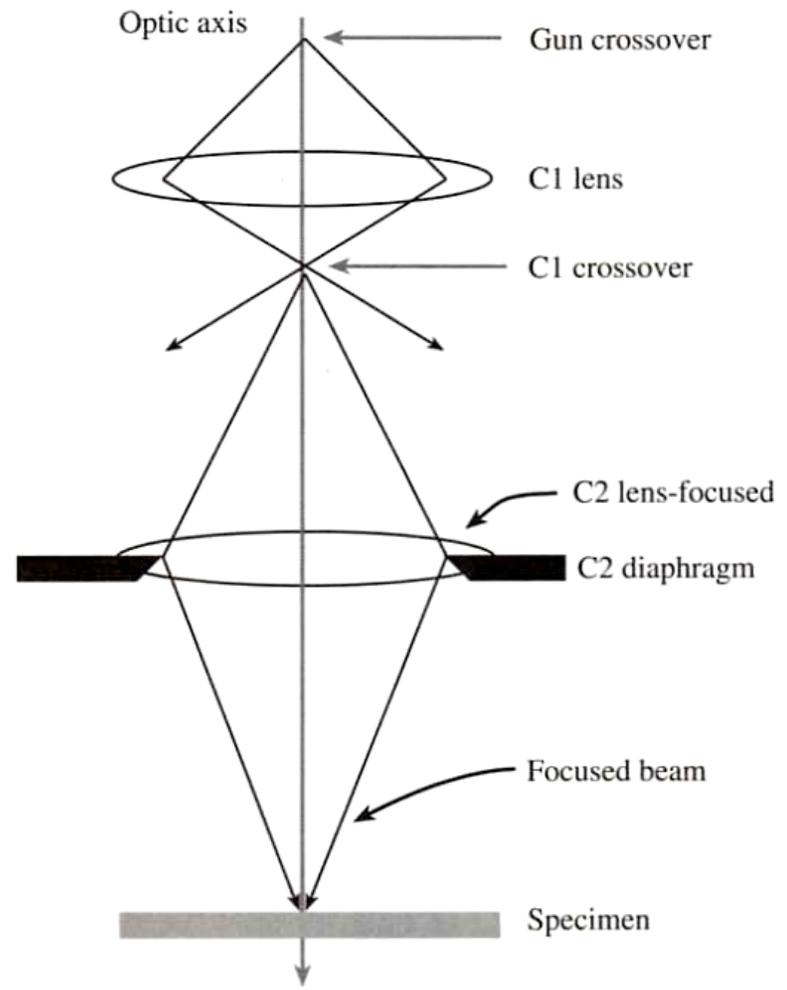


Figure 9.3. A focused C2 lens illuminates a small area of the specimen with a nonparallel beam.

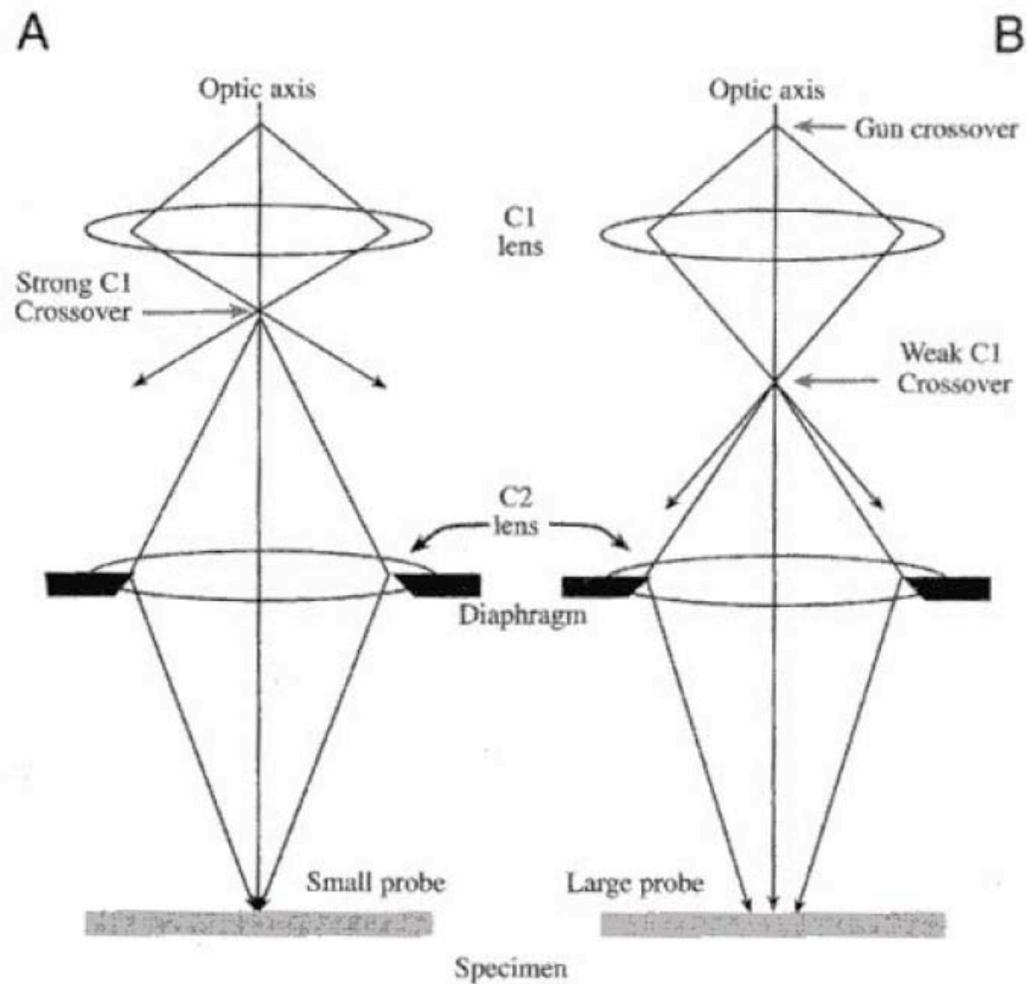


Figure 9.5. Effect of the C1 lens strength on probe size: a stronger C1 lens (A) results in greater demagnification by any subsequent lens (C2 or C3), giving a smaller electron beam at the specimen. A weaker lens (B) gives a broader probe.

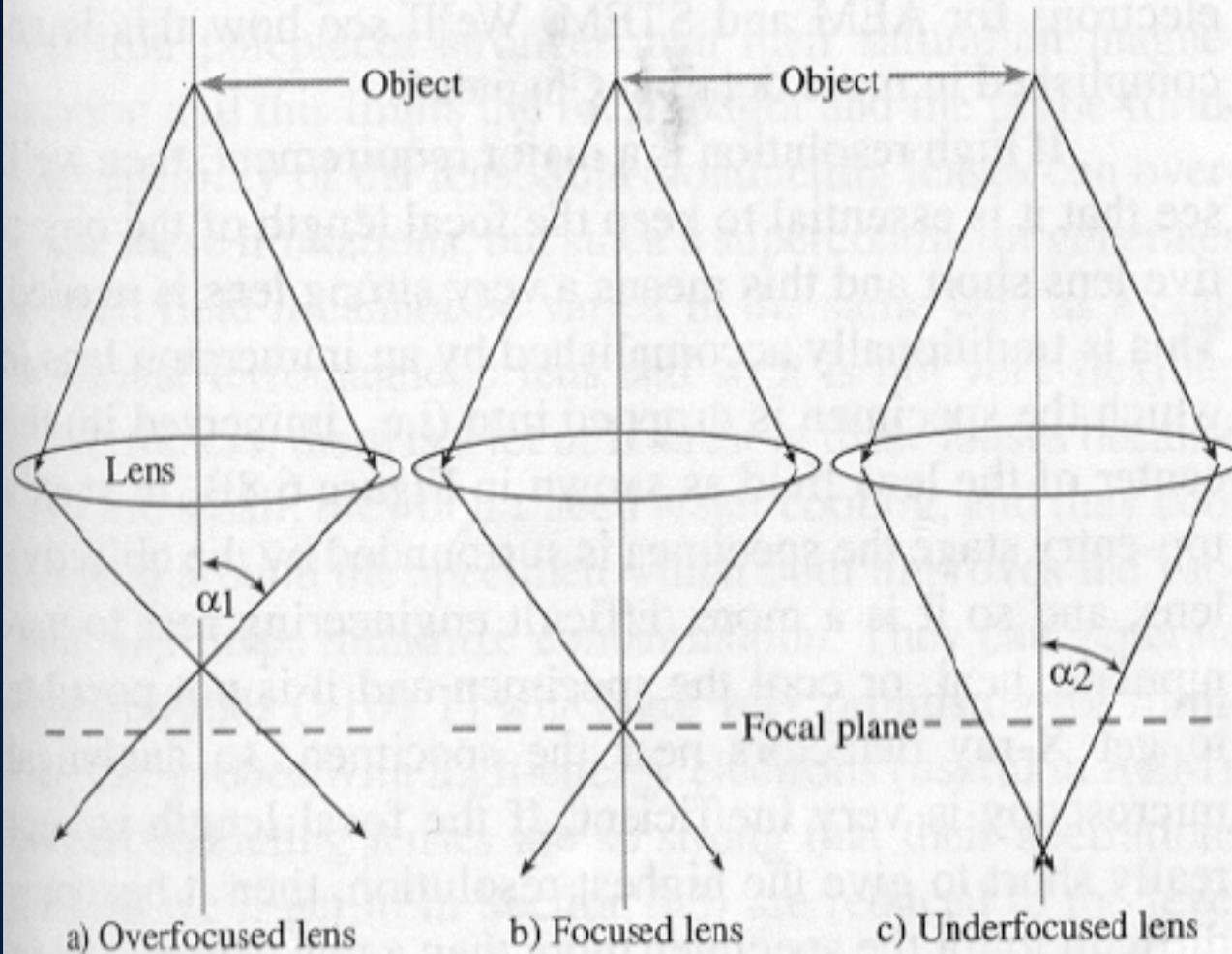
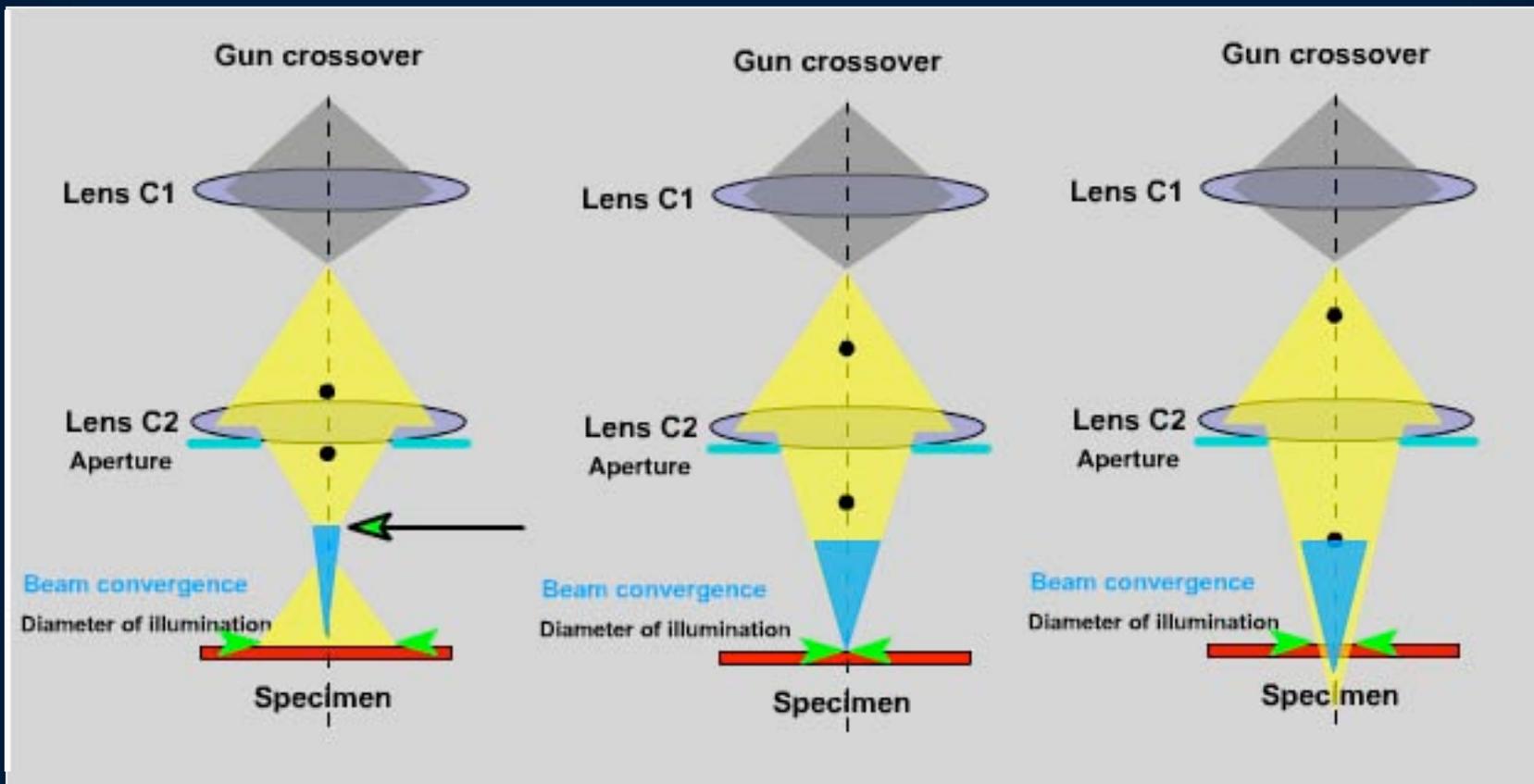


Figure 6.5. (a) Ray diagram illustrating the concepts of overfocus, in which a strong lens focuses the rays before the image plane, and (c) underfocus, where a weaker lens focuses after the image plane. It is clear from (c) that at a given underfocus the convergent rays are more parallel than the equivalent divergent rays at overfocus ($\alpha_2 < \alpha_1$).



Overfocused:
 beam convergence
 decreases substantially
 because electrons
 come from the
 crossover only

Focused:
 beam convergence is
 at a maximum

Underfocused:
 beam convergence
 decreases slightly

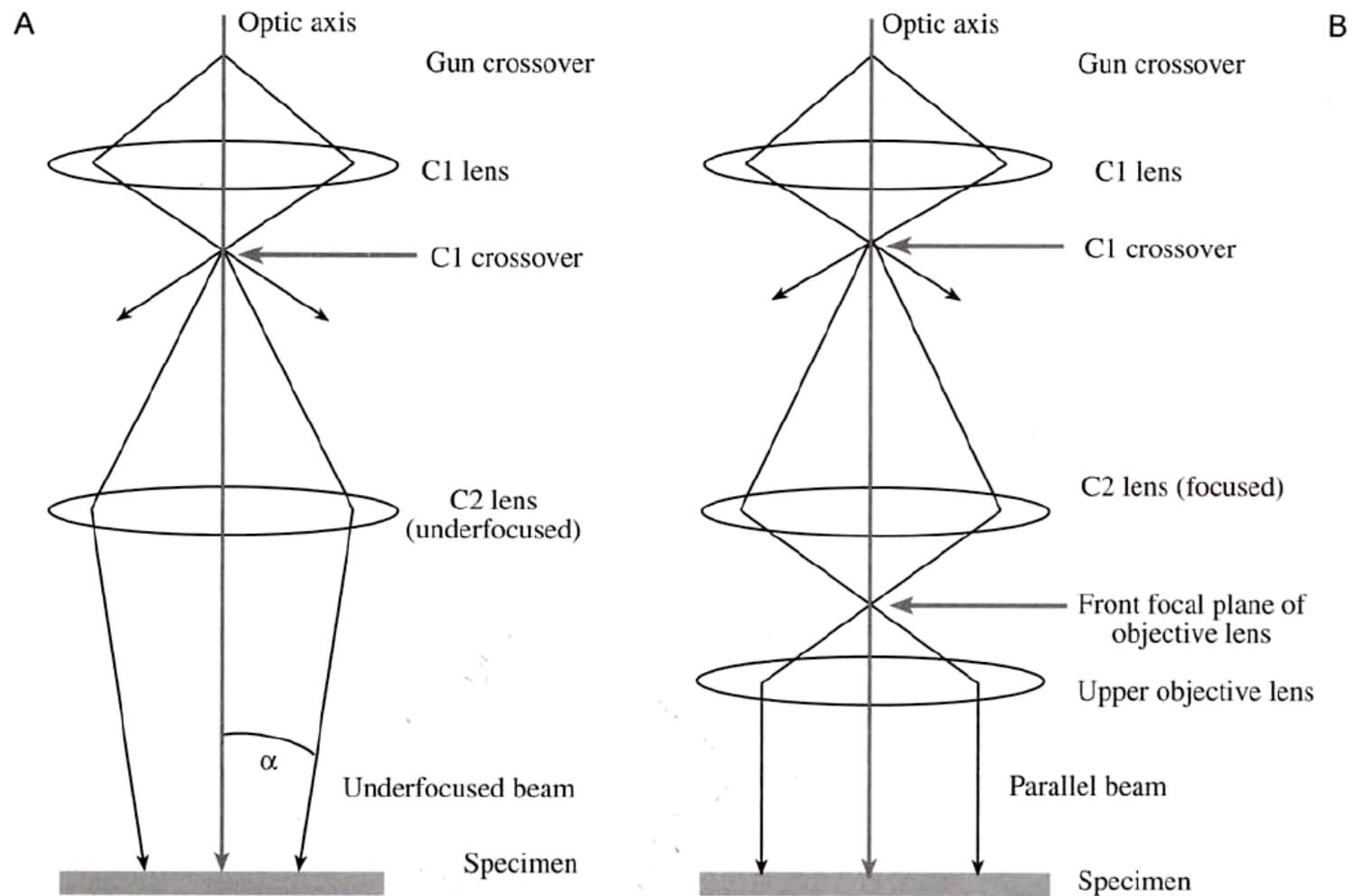
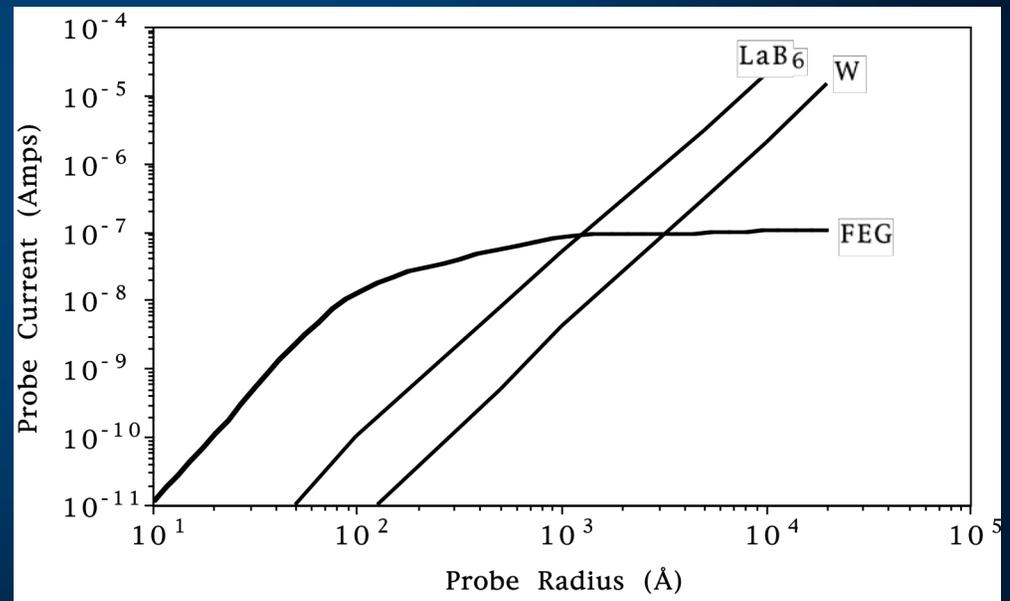
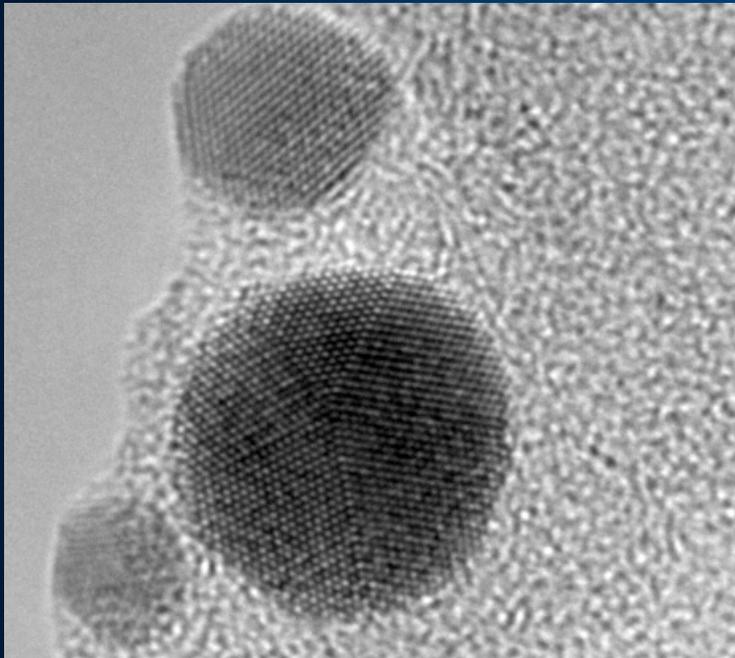


Figure 9.1. Parallel-beam operation in the TEM (A) using just the C1 and an underfocused C2 lens and (B) using the C1 and C2 lenses to image the source at the front focal plane of the upper objective lens.

With Modern Instruments
Spectroscopy can be done at the Sub-Nanometer Scale
Selection of Probe Forming Source is Important



Roles of the Lenses

Objective Lens

Mainly control
probe focus

Diffraction/Intermediate Lens

Controls Mode

Projector Lens

Magnification



Most TEM/STEM
have 7-8 Lenses

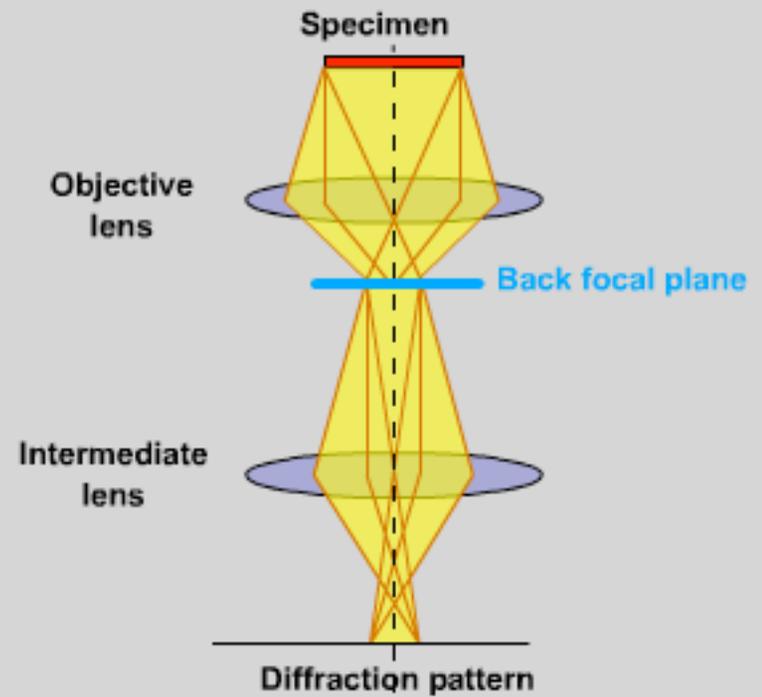
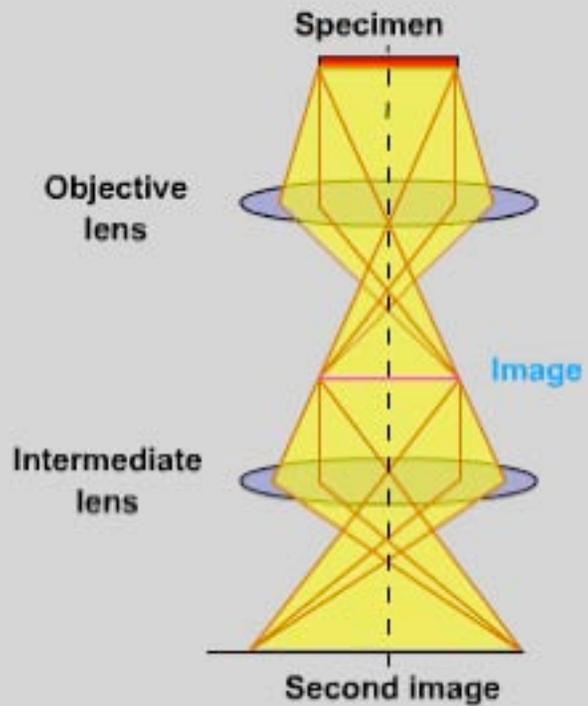
2 Condensers
1 Objective
1-2 Intermediate
2 Projectors

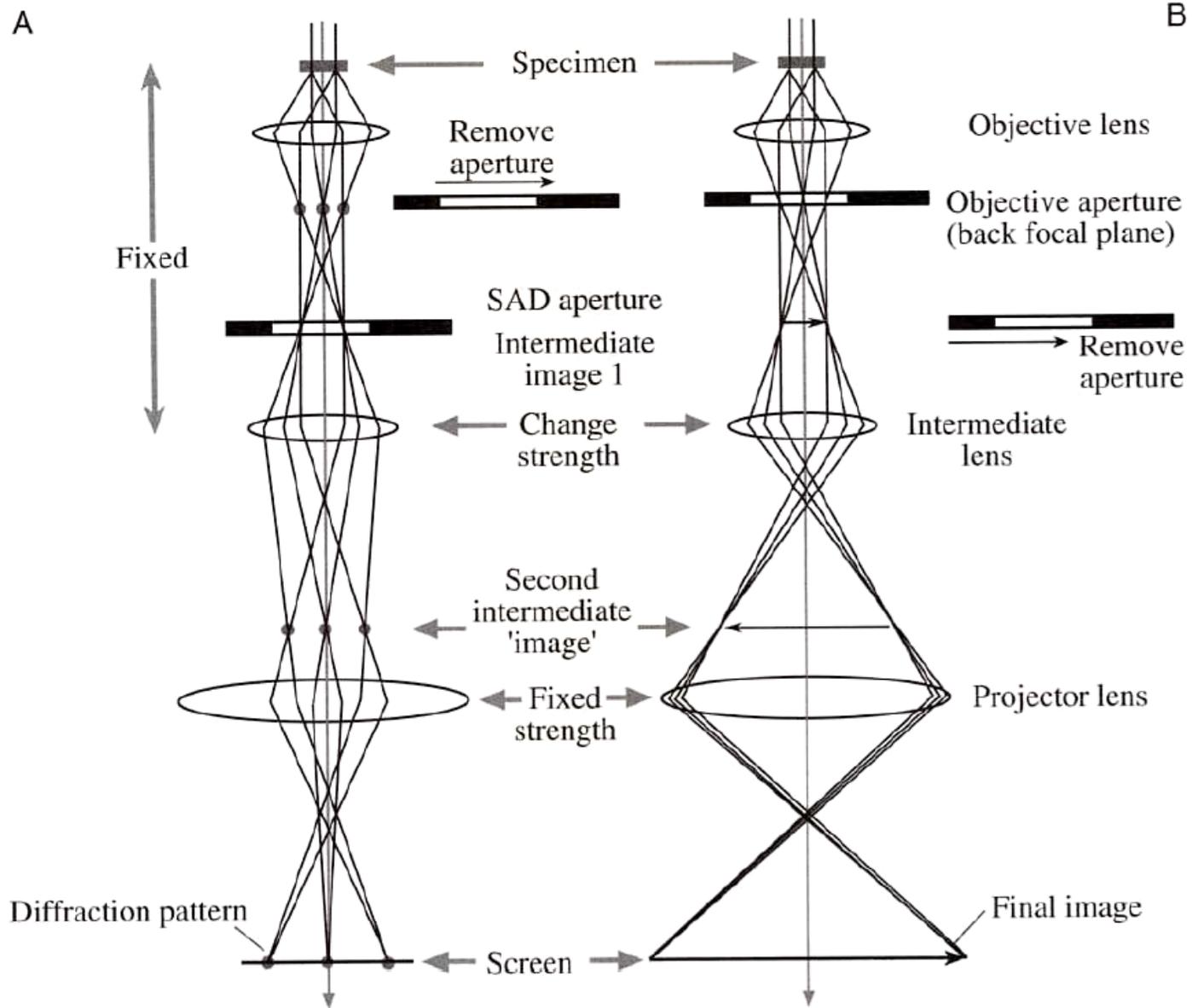
Most instruments
have only
Electromagnetic
Round Lenses

Note the locations
of the various
Apertures.

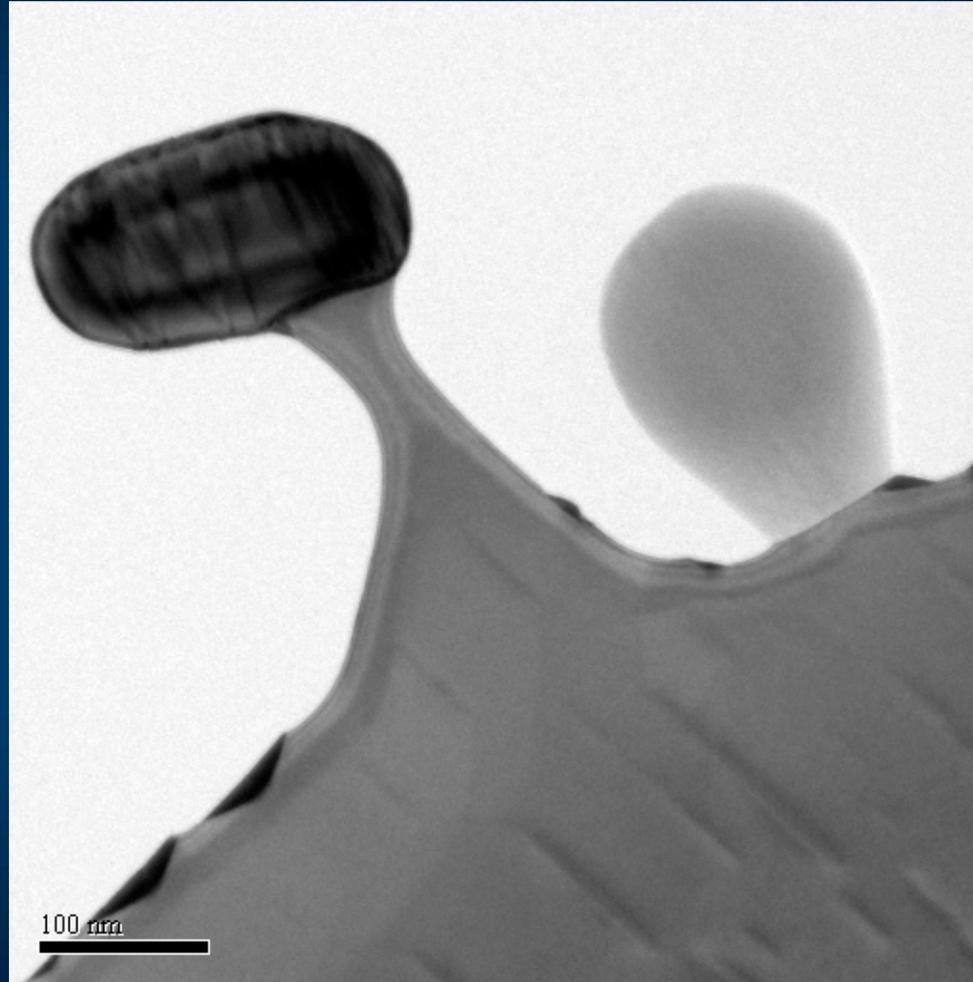
Optimum aperture
sizes are needed
for various
imaging functions.

Imaging vs Diffraction: Post Specimen Lenses determine the mode

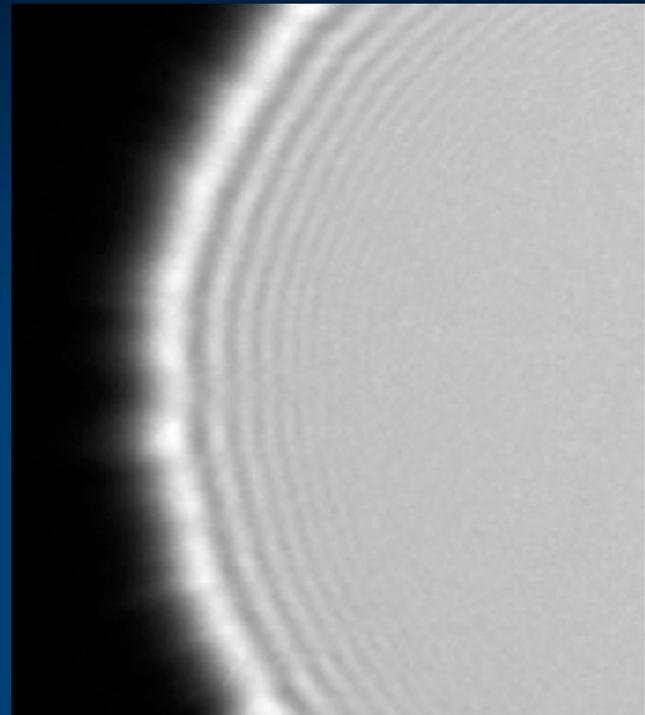
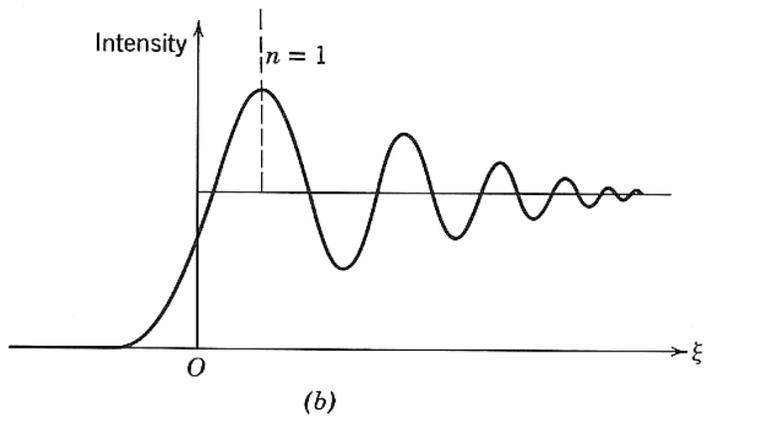
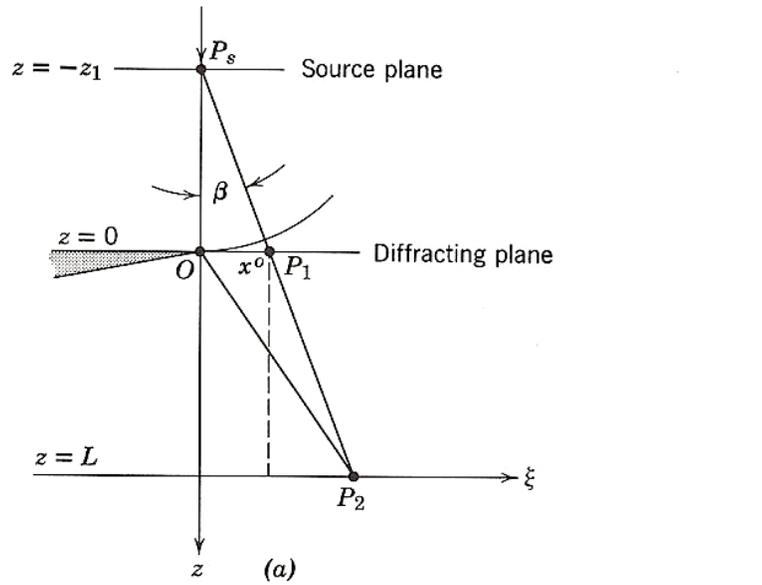




When is
the Image
in Focus?



Fresnel Fringes - Diffraction (Interference) from an Edge



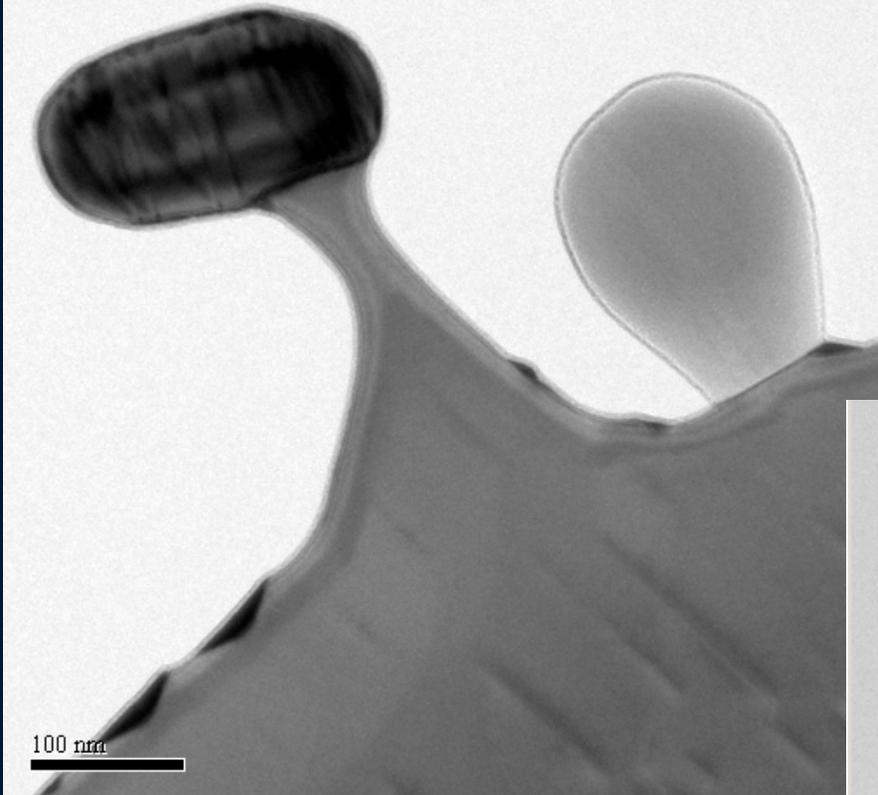
$$\nabla^2 \Psi(r) + \frac{8\pi^2 m e}{h^2} [E + V(r)] \Psi(r) = 0$$

$$\Psi_1(r, z) = \frac{\exp(2\pi i k r)}{r} \quad \Psi(r, z) = \sum \Psi_i(r, z)$$

$$I = \Psi(r, z) \Psi^*(r, z)$$

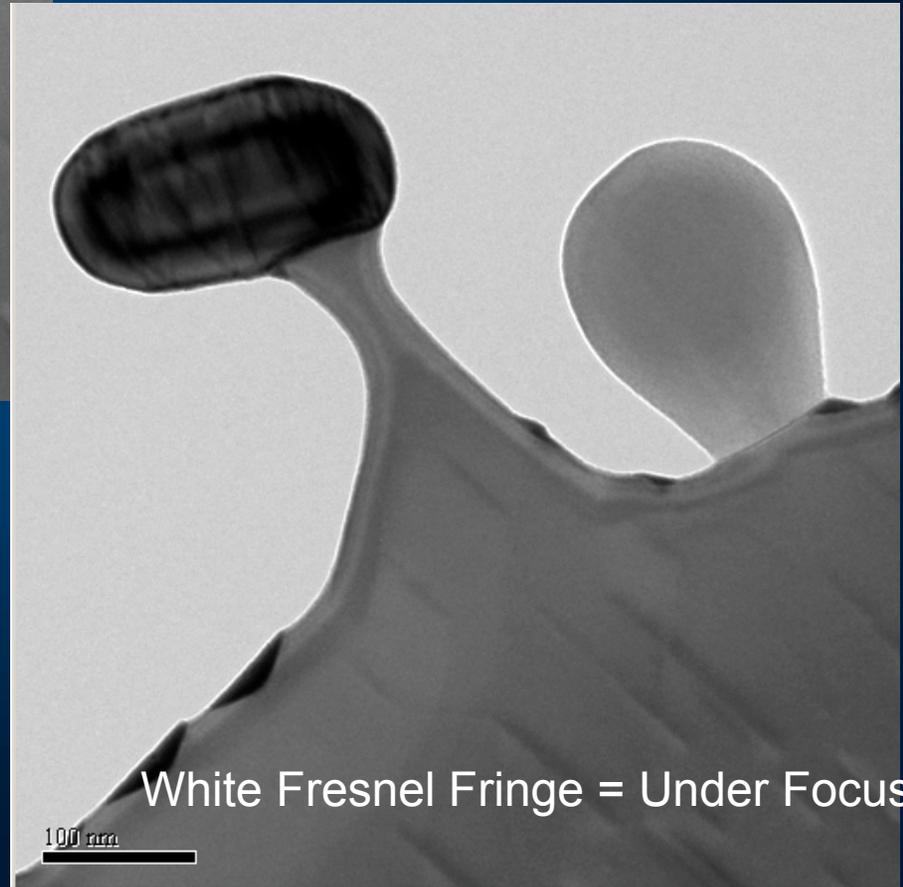
$$\xi_{\max} \simeq [4f(2n - 1)\lambda]^{1/2}$$

Black Fresnel Fringe = Over Focus



B O \longleftrightarrow W U

White Fresnel Fringe = Under Focus



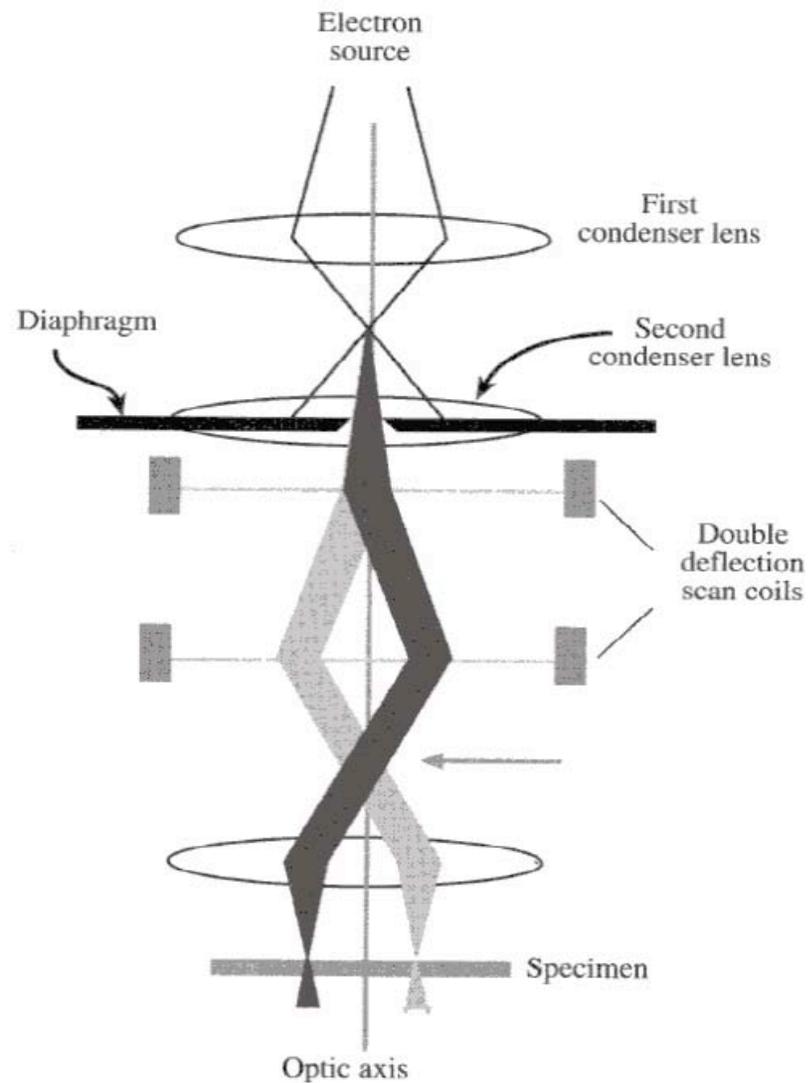
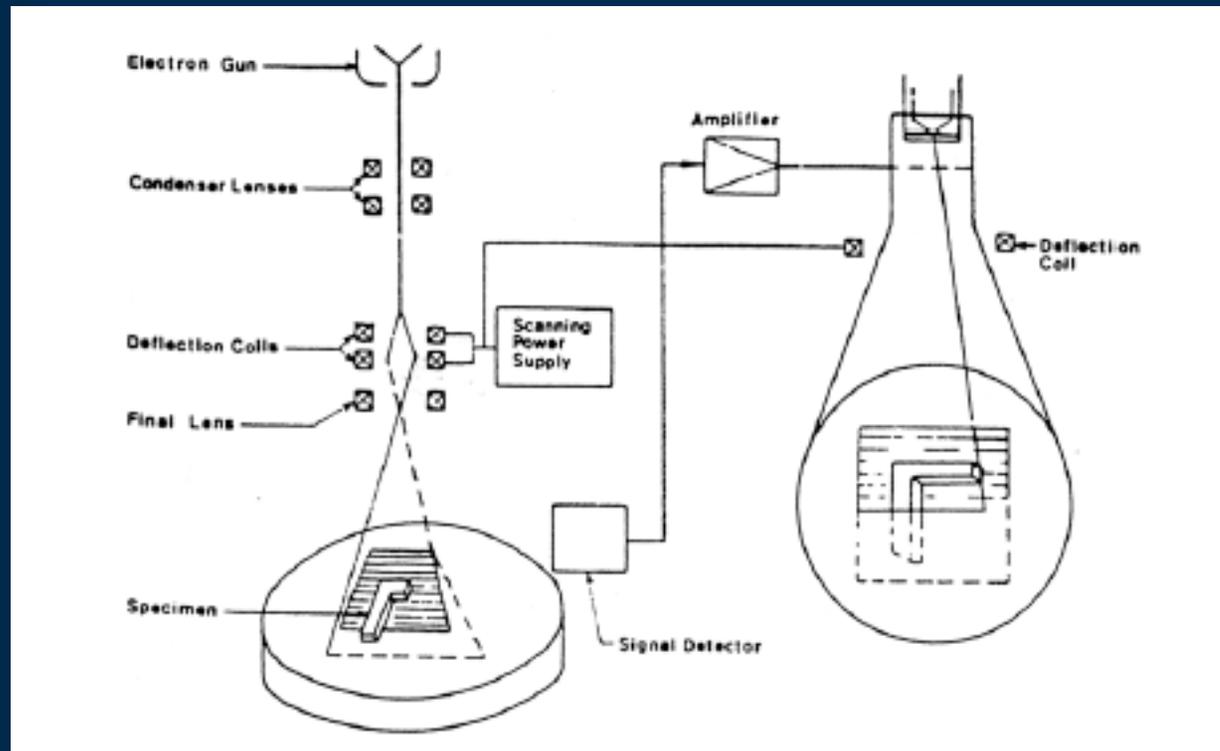


Figure 9.15. Scanning the convergent probe for STEM image formation using two pairs of scan coils between the C2 lens (usually switched off) and the upper objective polepiece. The probe remains parallel to the optic axis as it scans.

The scanning process is the mechanism which allows us to use small probes to form images of large areas.



$$\text{Magnification} = \text{CRT Display Size} / \text{Area Swept by Beam on Sample}$$

Electron Detectors

- TEM
 - phosphor screen, Film, CCD, Image Plate...
- SEM
 - SE detector, BE detector....
- STEM
 - BF detector, DF detector,

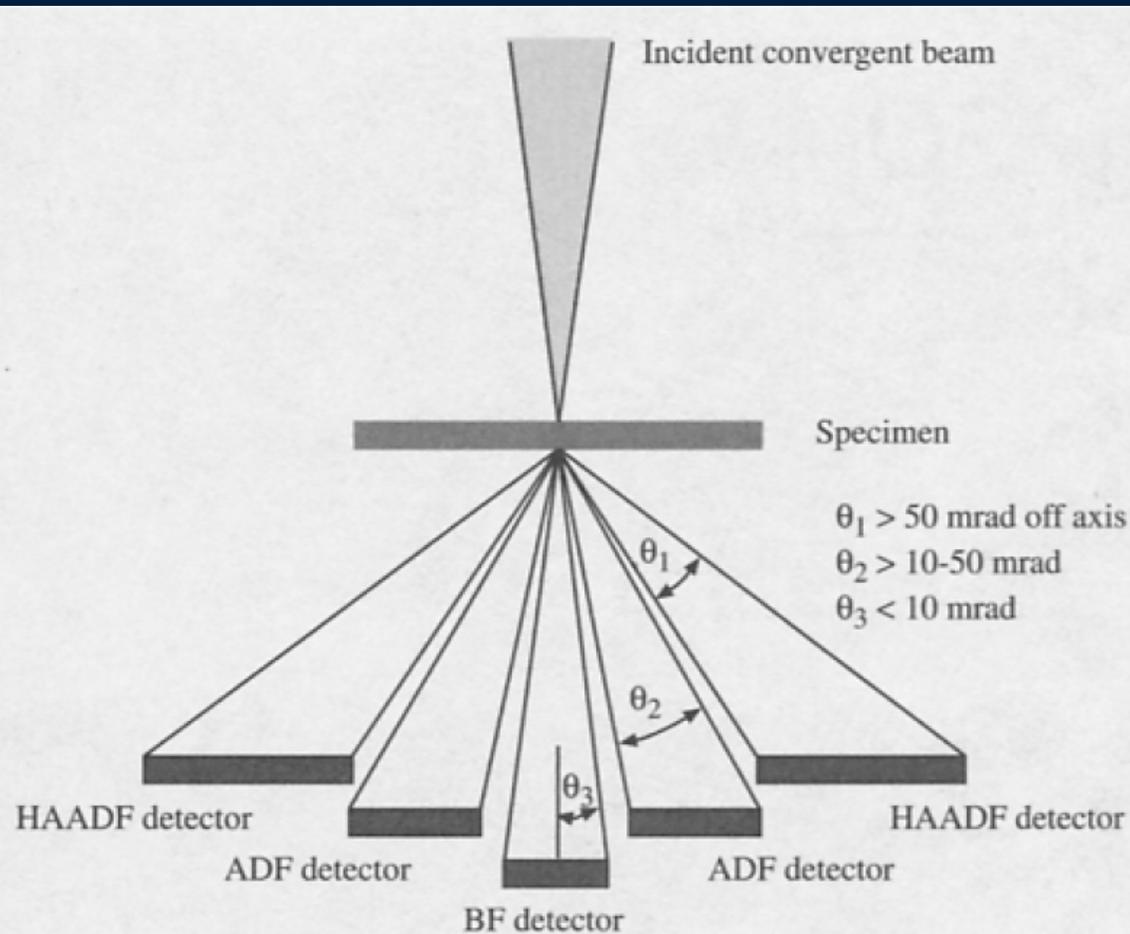
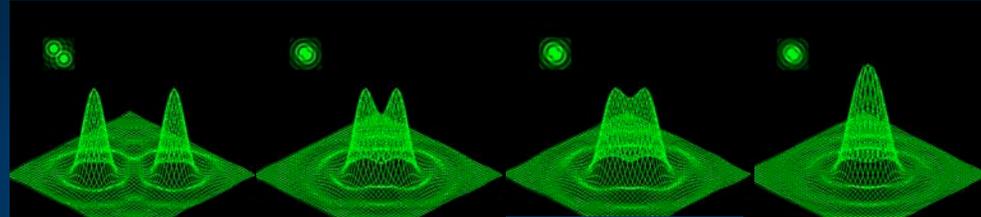


Figure 22.13. Schematic of the HAADF detector set-up for Z-contrast imaging in a STEM. The conventional ADF and BF detectors are also shown along with the range of electron scattering angles gathered by each detector.

What Limits Resolution?



Abbe (Diffraction) Limit:

Defines the minimum resolvable distance between the image of two point objects using a perfect lens.

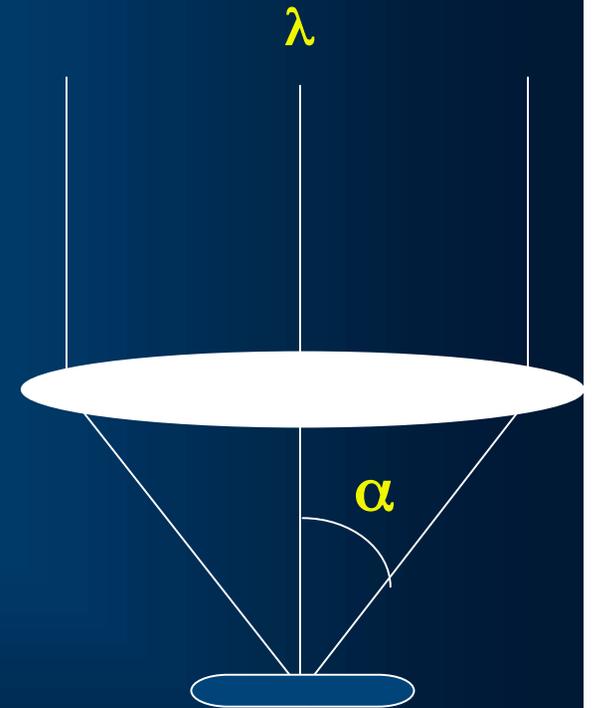
In any magnifying system a point object (i.e. zero dimension) cannot be imaged as a point but is imaged as a distribution of intensity having a finite width.

$$\text{Resolution of an imaging system} = \rho = \frac{0.61\lambda}{\eta \sin(\alpha)}$$

λ = wavelength of the imaging radiation

η = index of refraction of the lens

α = illumination semi-angle



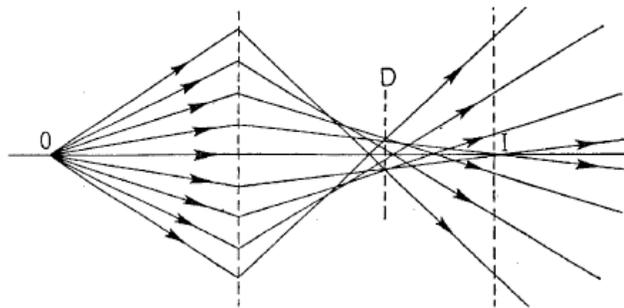
This ASSUMES a “Perfect Lens”

Ex: 100 kV electrons $\alpha \sim 100 \text{ mR} \Rightarrow \rho = 0.23 \text{ \AA}$

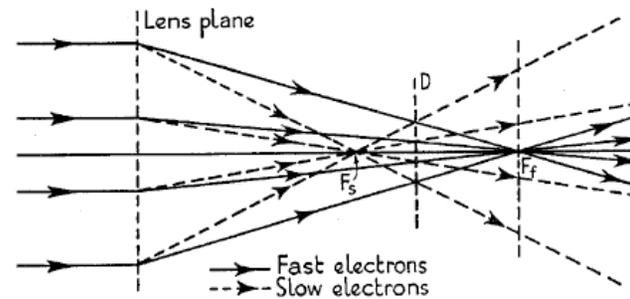
What limits our ability to perfectly focus?

Aberrations

- Spherical



- Chromatic



$$r_{sph} = C_s \beta^3$$

$$r_{chr} = C_c \frac{\Delta E}{E} \beta$$

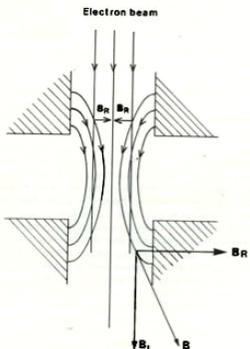
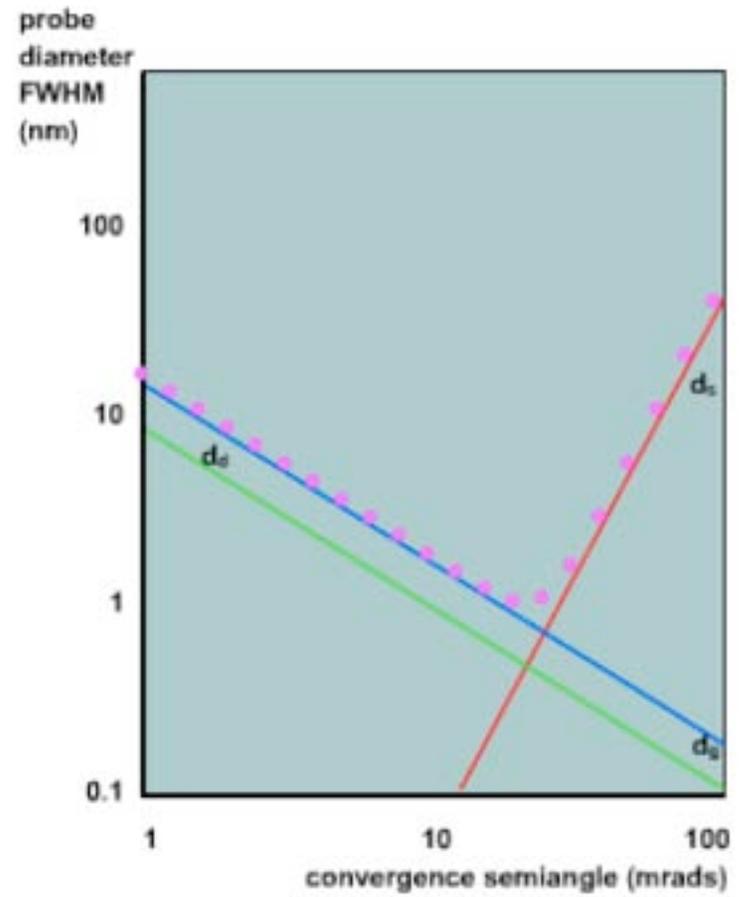
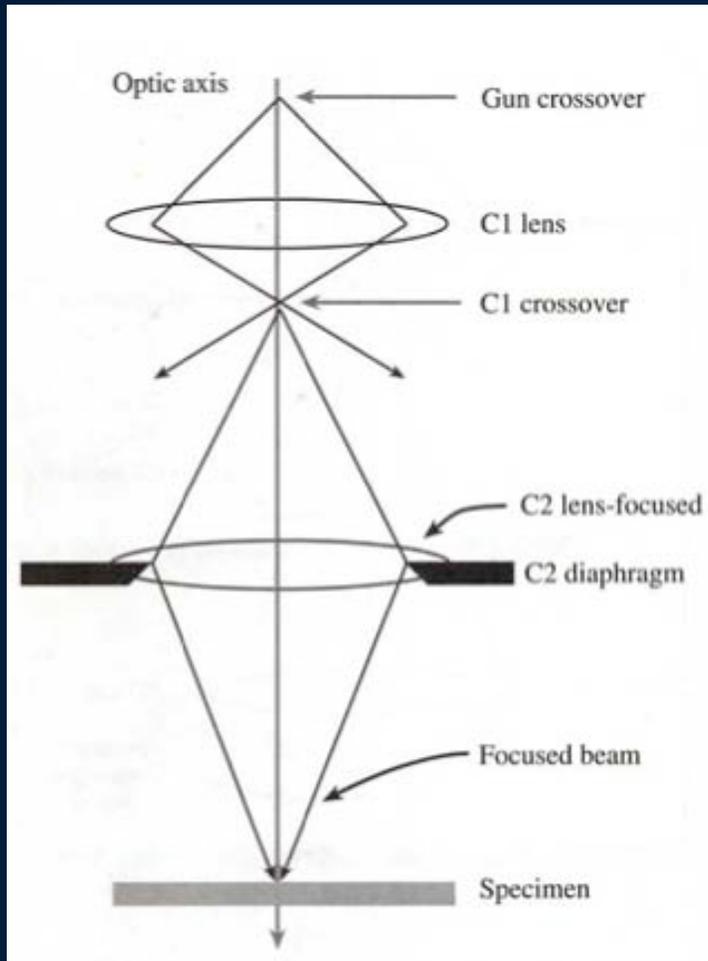


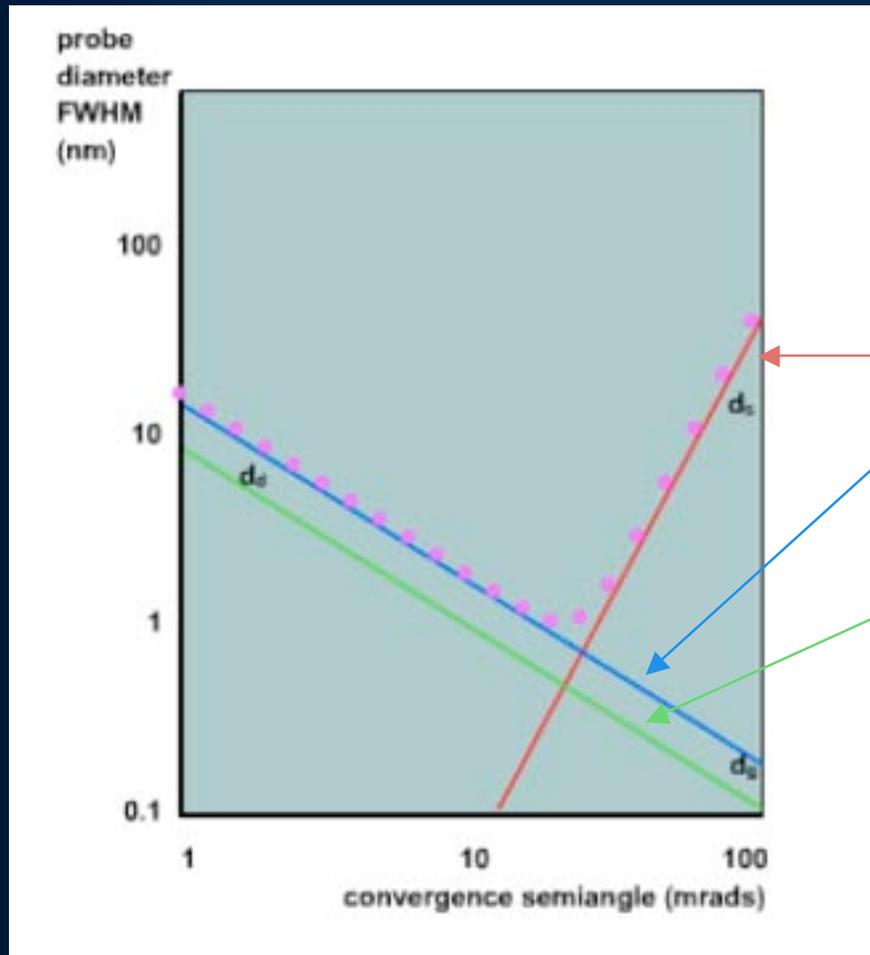
Fig. 1.2 Schematic diagram of the action of a cylindrical magnetic lens on the path of non-axial electrons. B_r is the radial component and B_z the longitudinal component of the field.

Lens Aberrations

Prespecimen Aberrations



Aberrations and Probe Size Related Parameters



$$d_{\epsilon} = \frac{2}{\pi} \sqrt{\frac{i}{\beta}} \frac{1}{\alpha}$$

$$d_s = 0.5 C_s \alpha^3$$

$$d_d = 1.22 \frac{\lambda}{\alpha}$$

The total beam diameter is found by adding these three effects in quadrature i.e.

$$d_t = \sqrt{d_s^2 + d_{\epsilon}^2 + d_d^2}$$

Aberration Correction also increases *usable* probe current

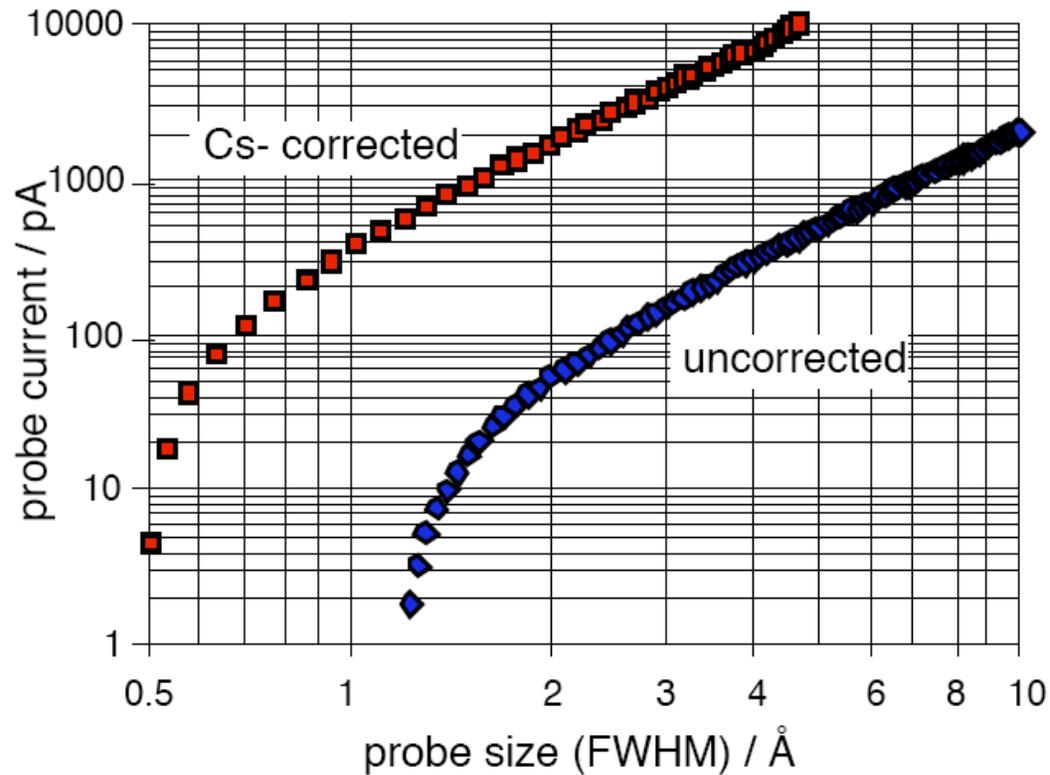
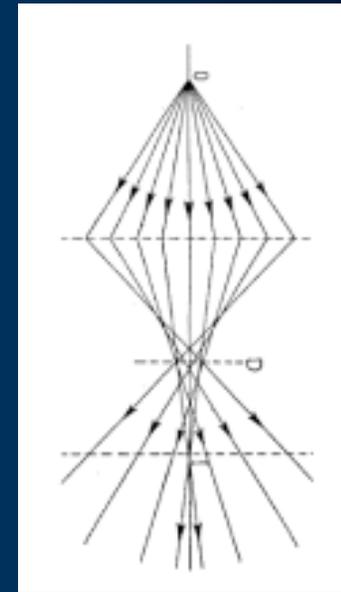
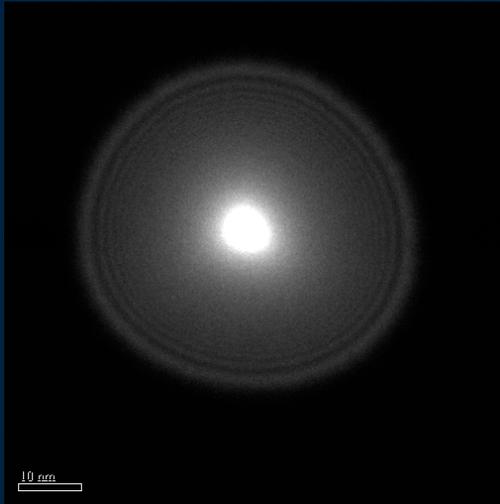


Fig. 1. Probe current vs. probe size. C_s -corrected: 200 keV, C_3/C_5 corrected, $C_{7,8} = 10$ cm, cold field emission gun. Uncorrected: $C_s = 0.5$ mm, Schottky gun.



Can we see aberrations ? Yes if you look for them.



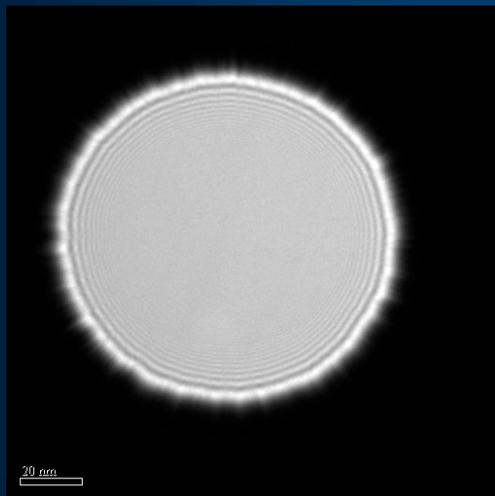
150 μm



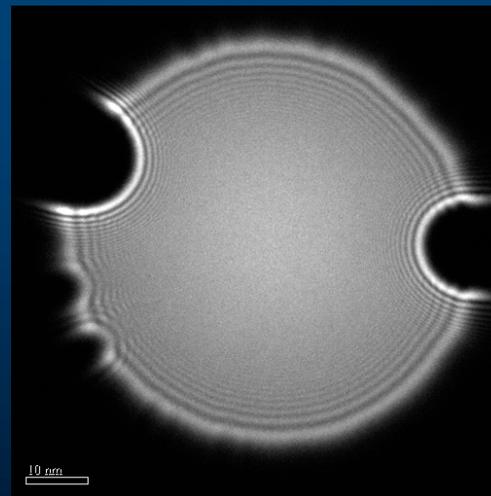
70 μm



30 μm



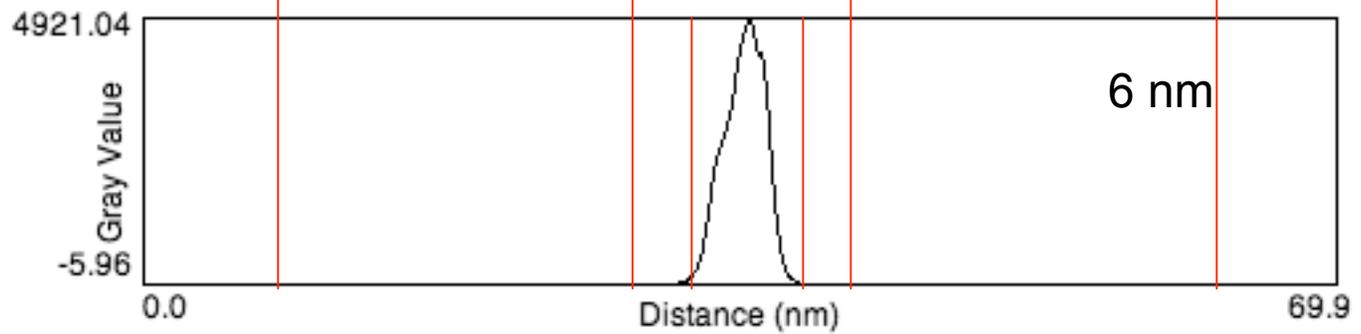
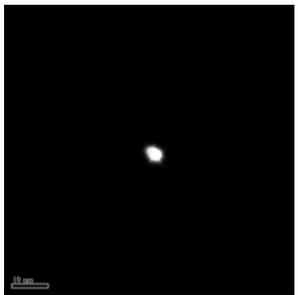
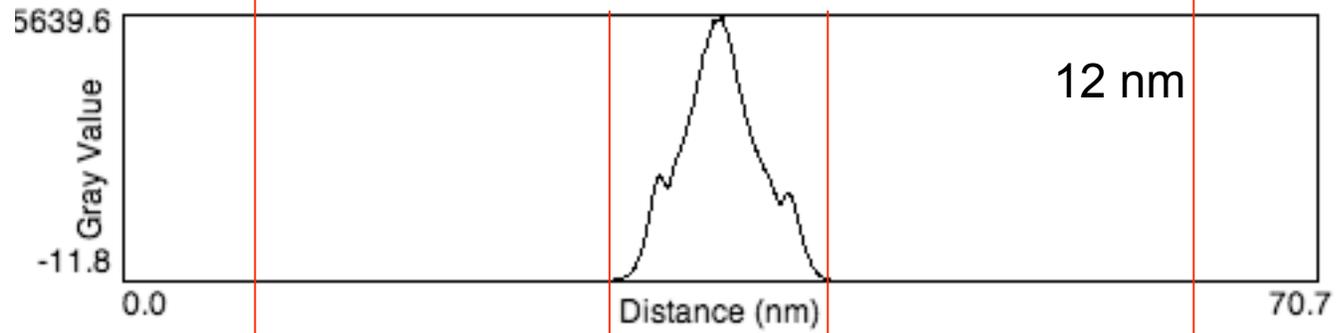
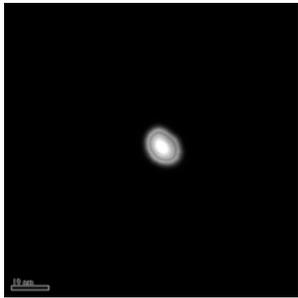
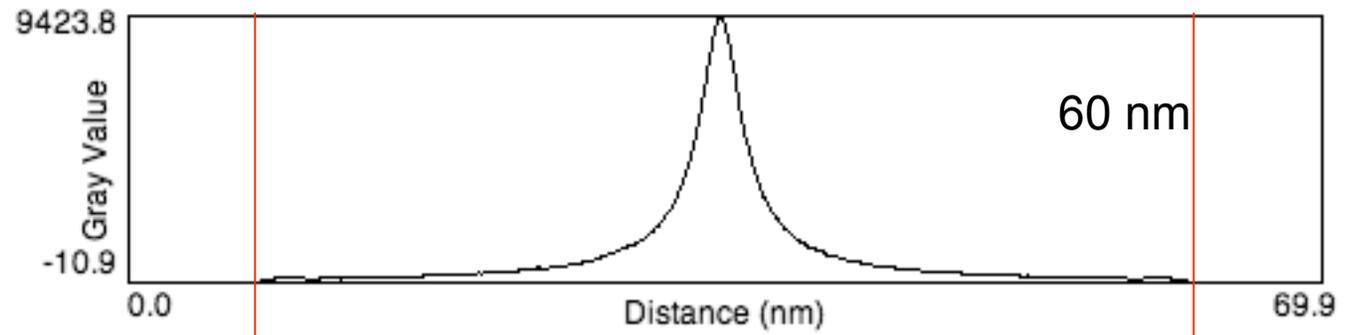
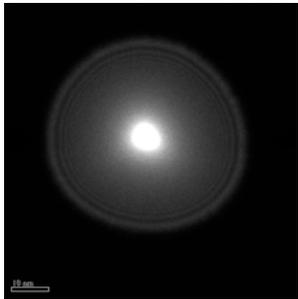
70 μm Clean



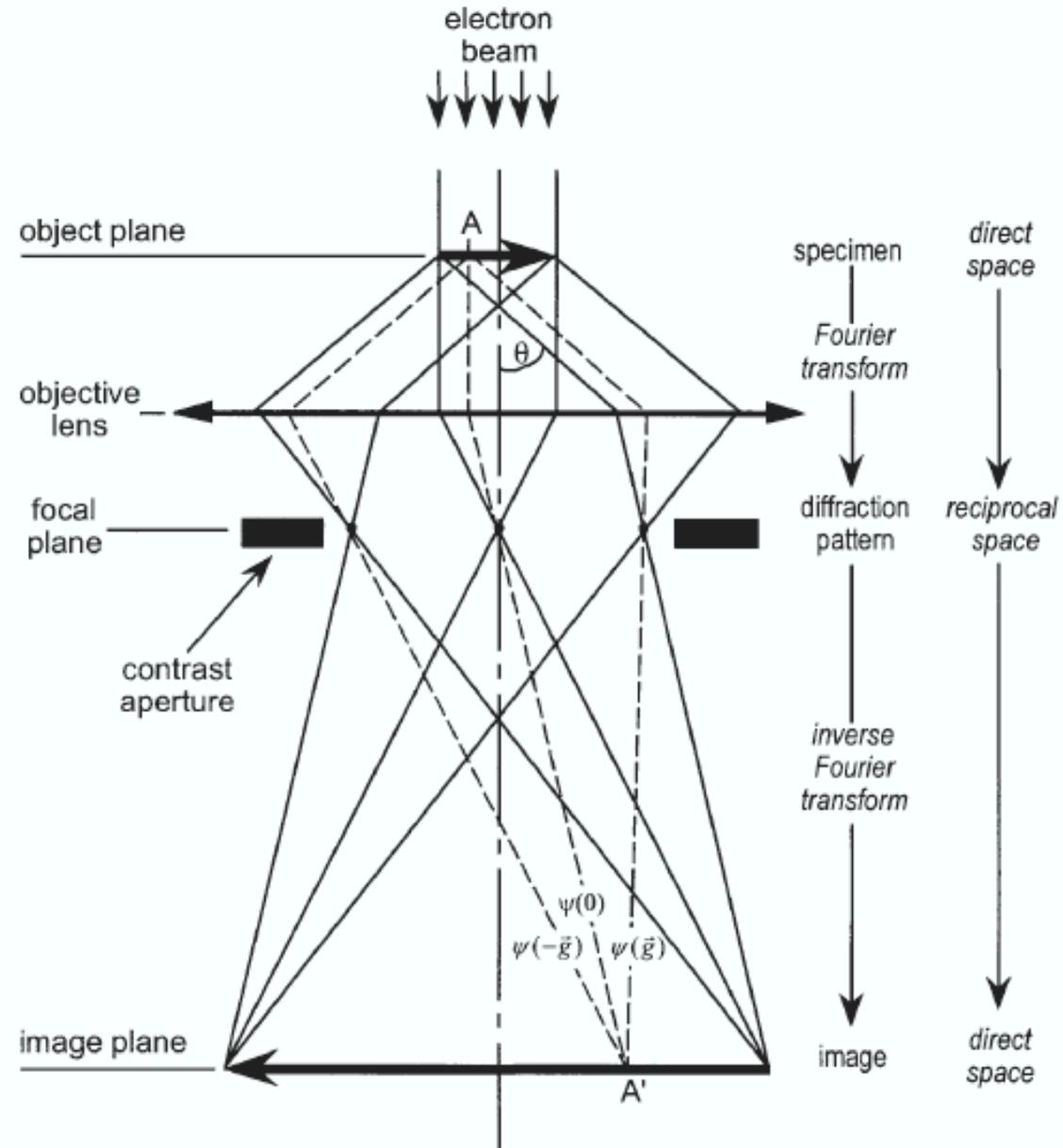
100 μm Dirty



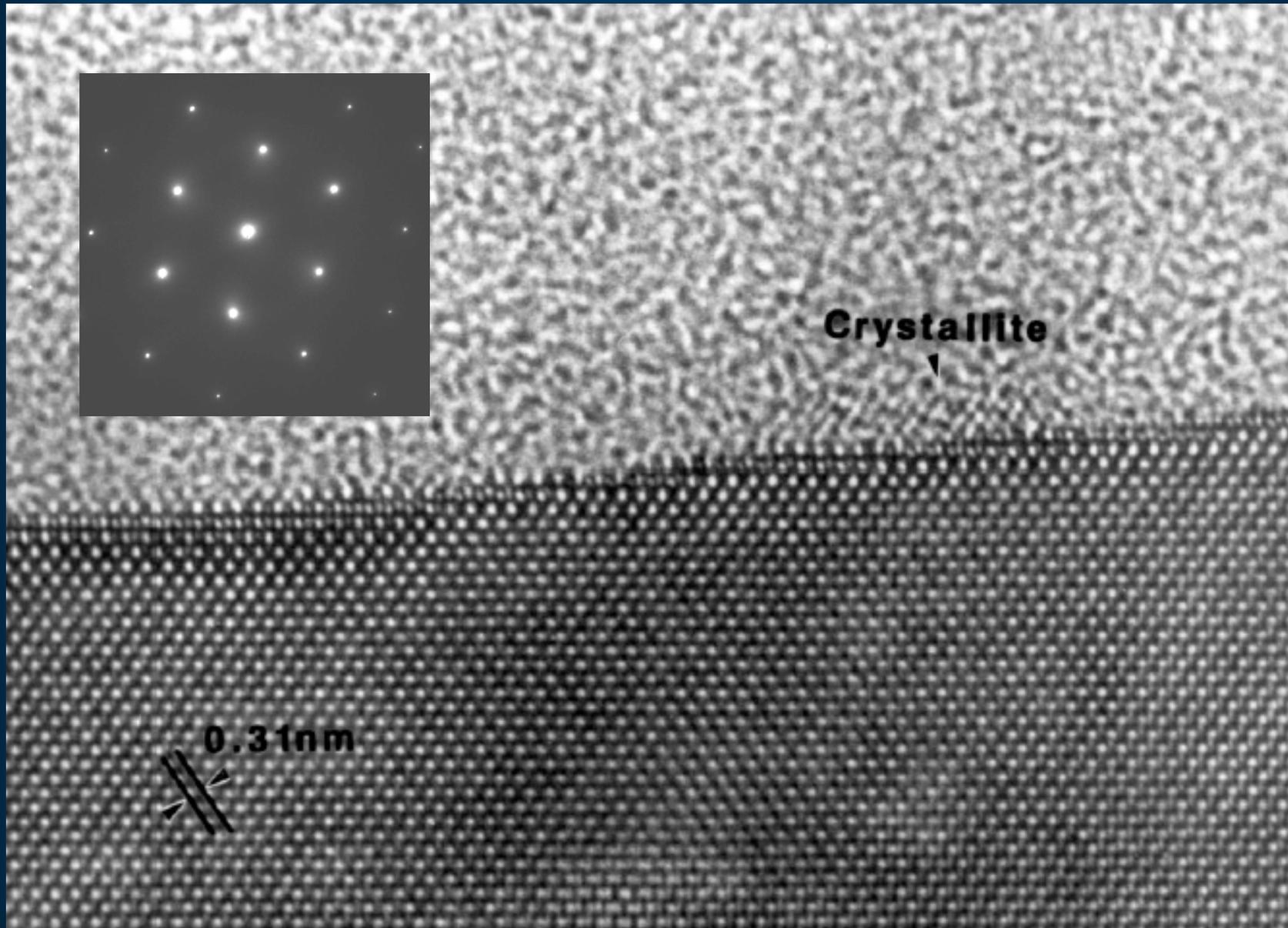
100 μm Dirty



Post Specimen Aberrations

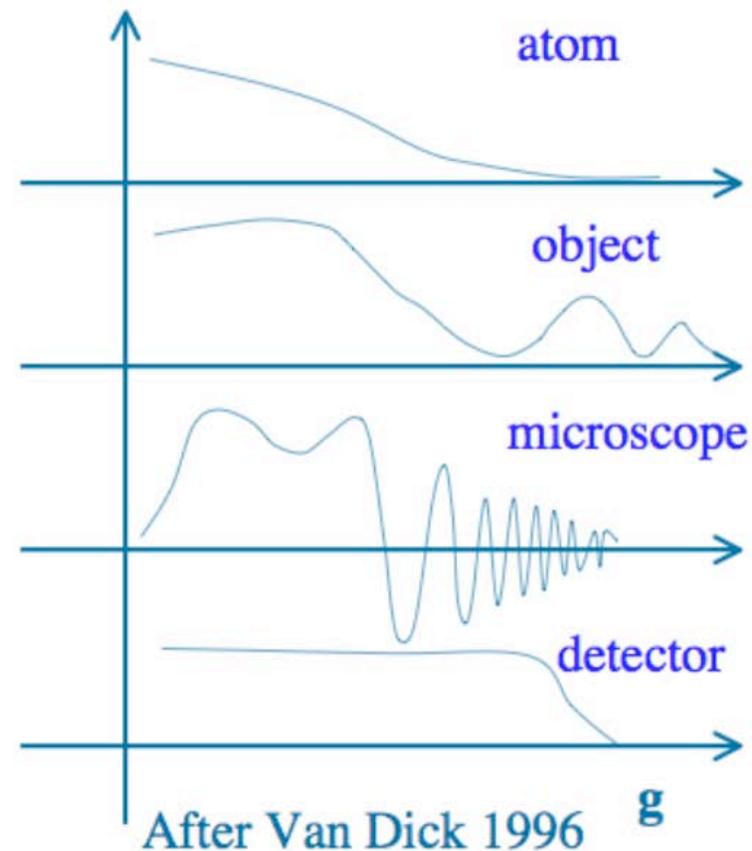


TEM-High Spatial Resolution Imaging



Resolution limiting factors

- The atom:
 - the Fourier transform of the atomic electrostatic potential is the scattering factor
- The 3D object:
 - 3D electron object interaction into a 2D imaging system, especially for thick samples
- The electron microscope
- The recording device



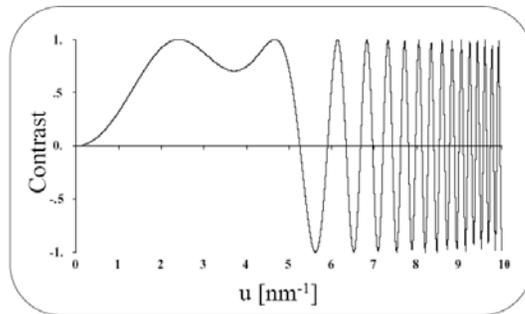
Lens System & Microscope Resolution

- Microscope resolution is governed by: (for TEM)
 - wavelength of electrons
 - C_s of objective lens
 - other lenses are less crucial (α/M)

$$\delta = 0.66 \times C_s^{1/4} \lambda^{3/4}$$

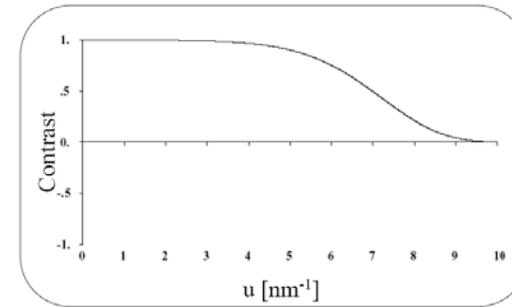
Aberrations and Image Resolution

$$H(\mathbf{u}) \sim \sin(\pi \cdot \Delta f \cdot u^2 + \frac{1}{2} \cdot C_s \cdot \pi \cdot \lambda^3 \cdot u^4)$$

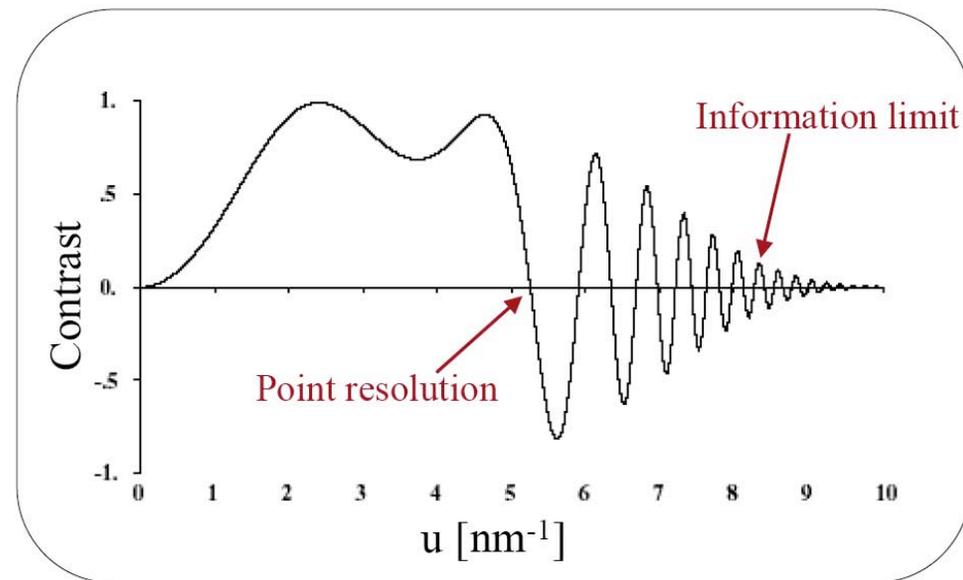


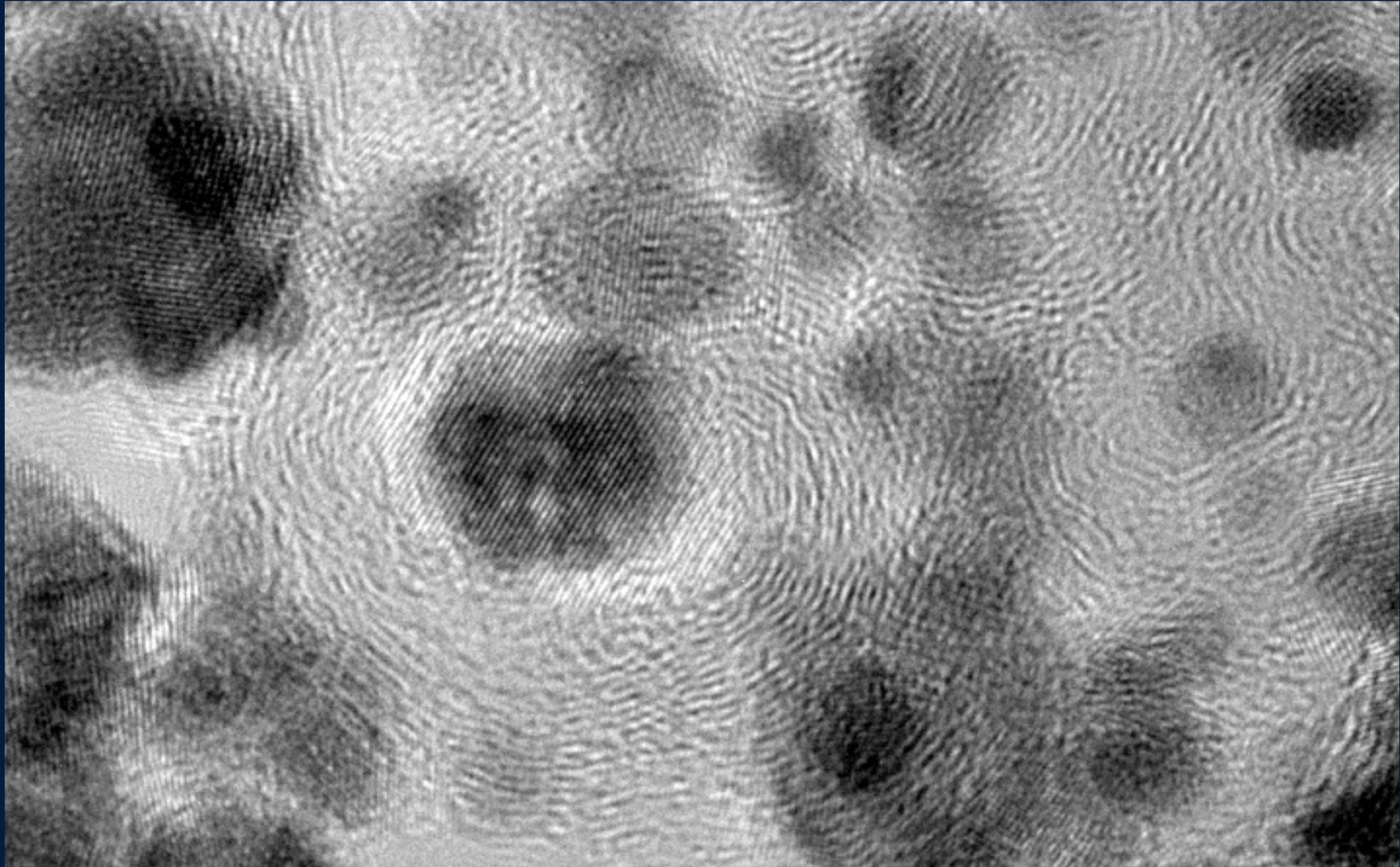
- Depends on spherical aberration (C_s) and defocus (Δf).

Bounding envelope



- Depends on chromatic aberration (C_c), coherence of electrons and stability of sample.

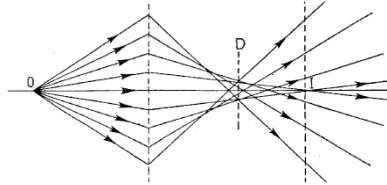




What are the limitations in EM ?

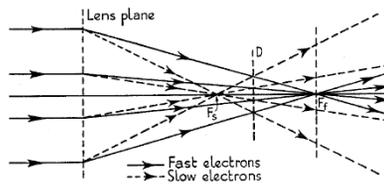
Aberrations

- Spherical



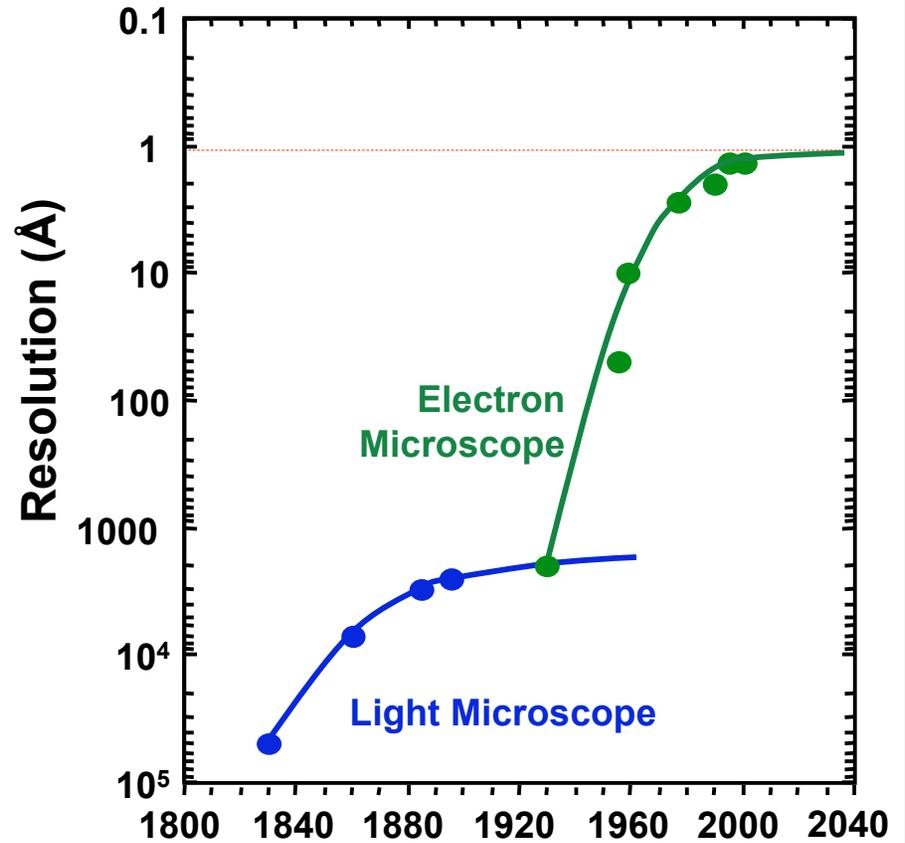
$$r_{sph} = C_s \beta^3$$

- Chromatic

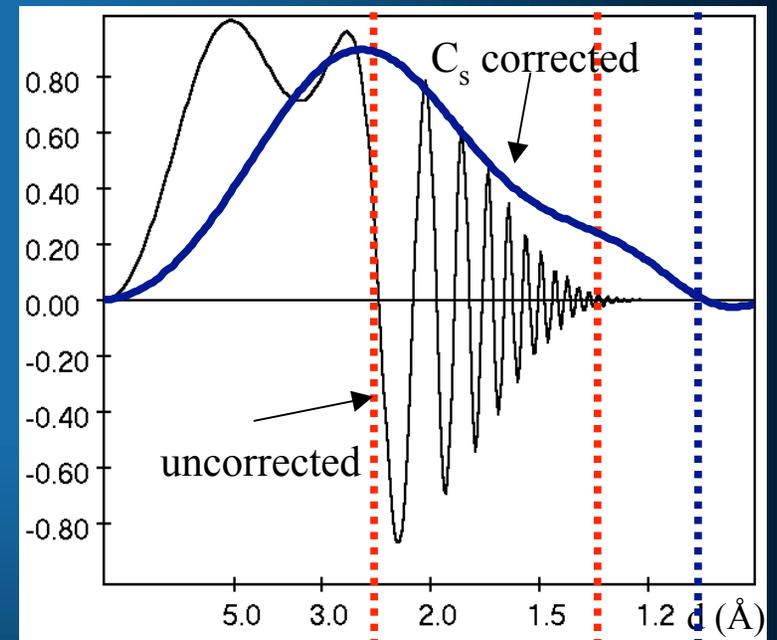
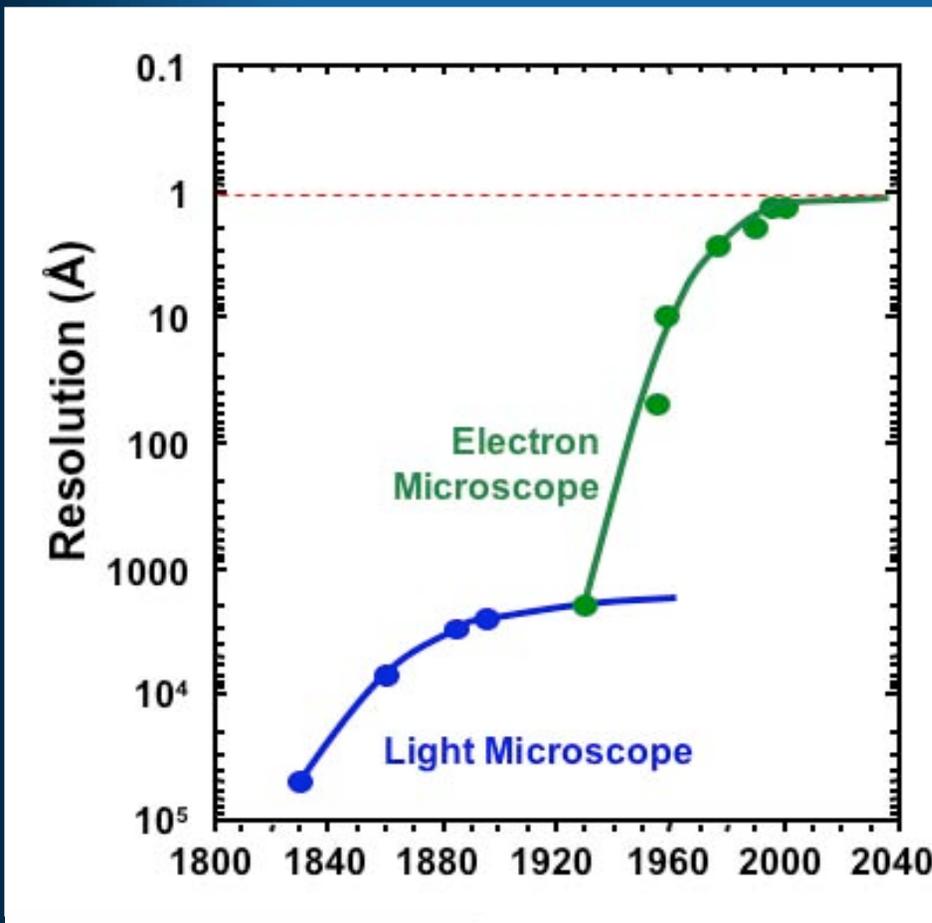


$$r_{chr} = C_c \frac{\Delta E}{E} \beta$$

The source and solution to “resolution limitations” has been known for nearly 50 years



TEAM Project Phase 1 : Ultra High Resolution Imaging
Requirements: <0.05 nm, 0.1 na , 0.1 eV



point res.

First Generation Corrected Instruments

Aberration Free Imaging

Influence of Contrast Delocalization

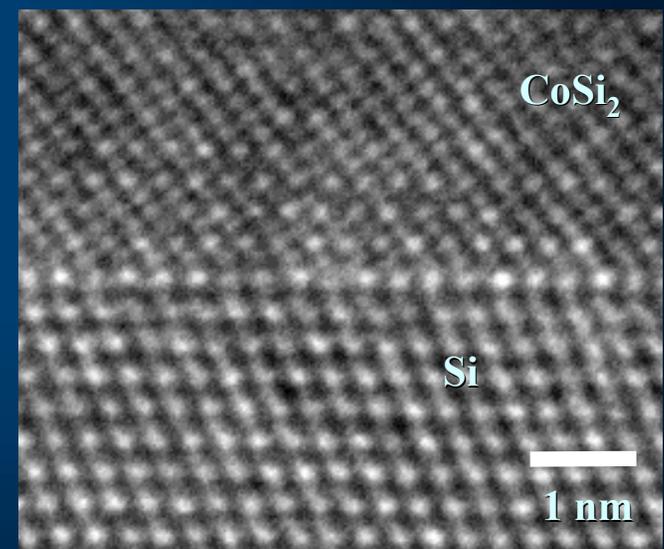
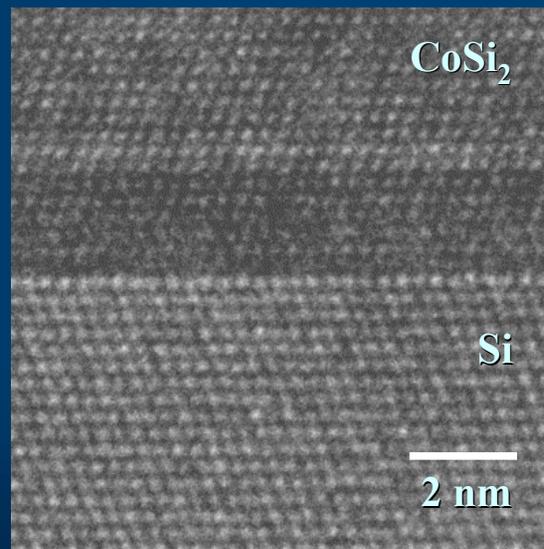
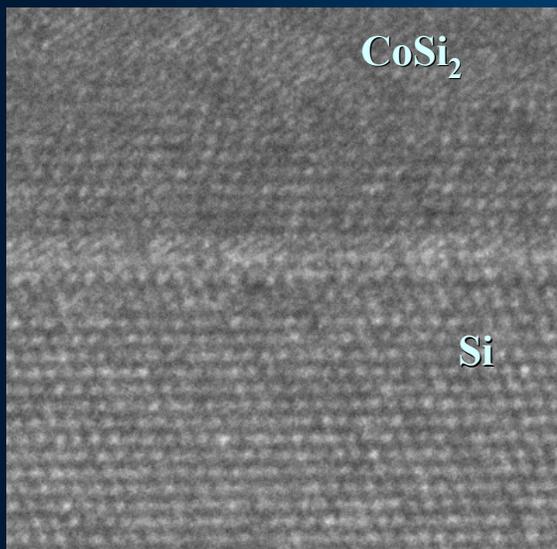
Uncorrected : $C_s = 1.2 \text{ mm}$

Corrected :
 $C_s = 0.05 \text{ mm}$

$\Delta f = -257 \text{ nm}; R = 1.4 \text{ nm}$

$\Delta f = -68 \text{ nm}; R = 4.4 \text{ nm}$

$\Delta f = -12 \text{ nm}; R = 0.1 \text{ nm}$



focus of least confusion

Scherzer defocus

Scherzer defocus (AFI)

$$\text{Delocalization} : R = | C_5 \lambda^5 g^5 + C_3 \lambda^3 g^3 + \lambda C_1 g |_{max}$$

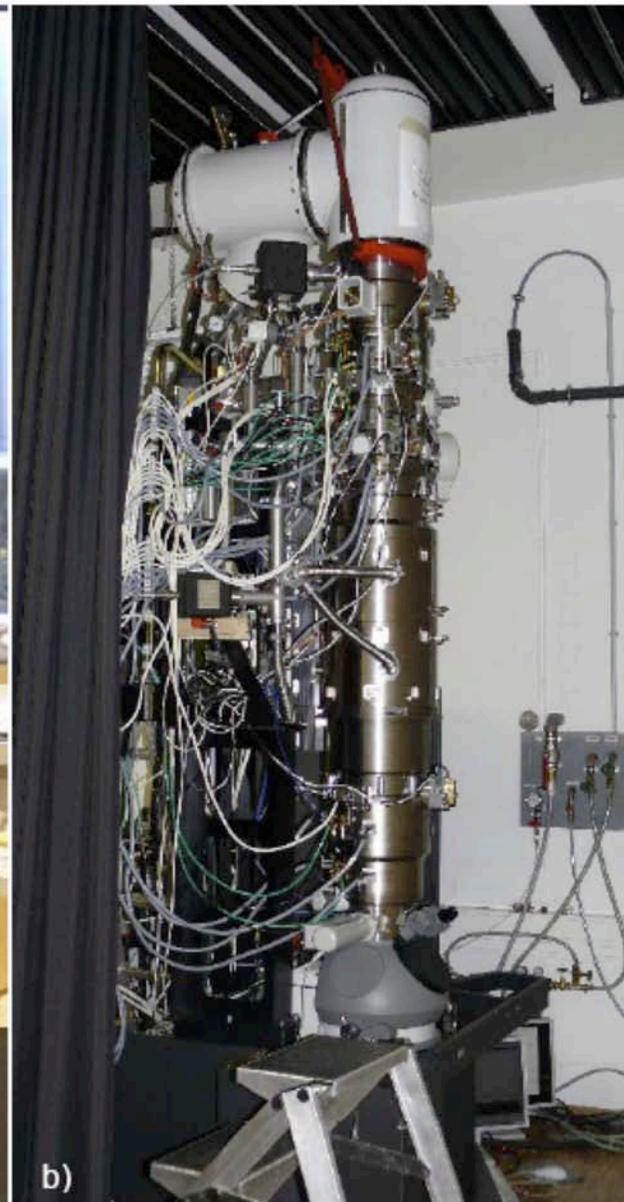


Fig. 1: a) The Cc/Cs-corrector (C-COR) after construction showing the total length (83 cm) without filter boxes and vacuum lines and b) the Titan with the C-COR incorporated.

THE TEAM PROJECT

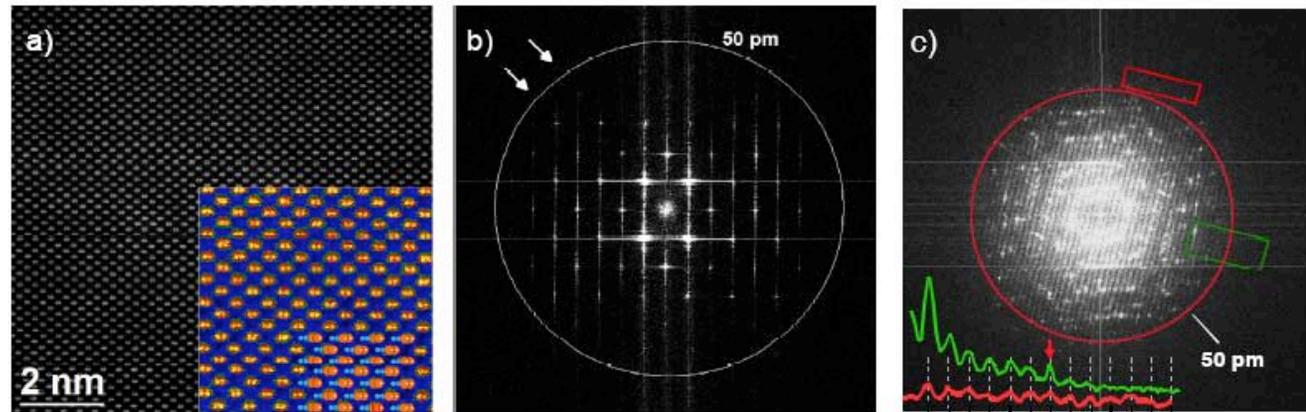
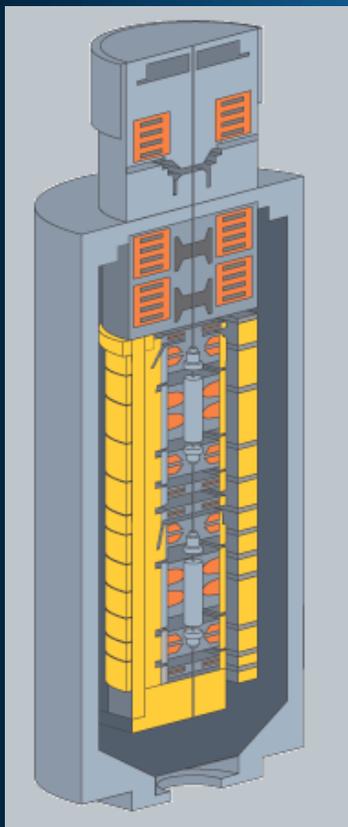


Figure 1. Performance of TEAM 0.5 microscope in STEM and TEM. Aberration-corrected high-resolution STEM image of GaN in [211] orientation (a), showing the 0.63\AA distance between Ga dumbbells clearly resolved (see inset model). The corresponding diffraction pattern in (b) shows Fourier components beyond the 50 pm marker indicated by the circle. The Fourier diffraction pattern from high resolution TEM images in (c) shows Young's fringes extending beyond the 50 pm mark indicated by the circle.

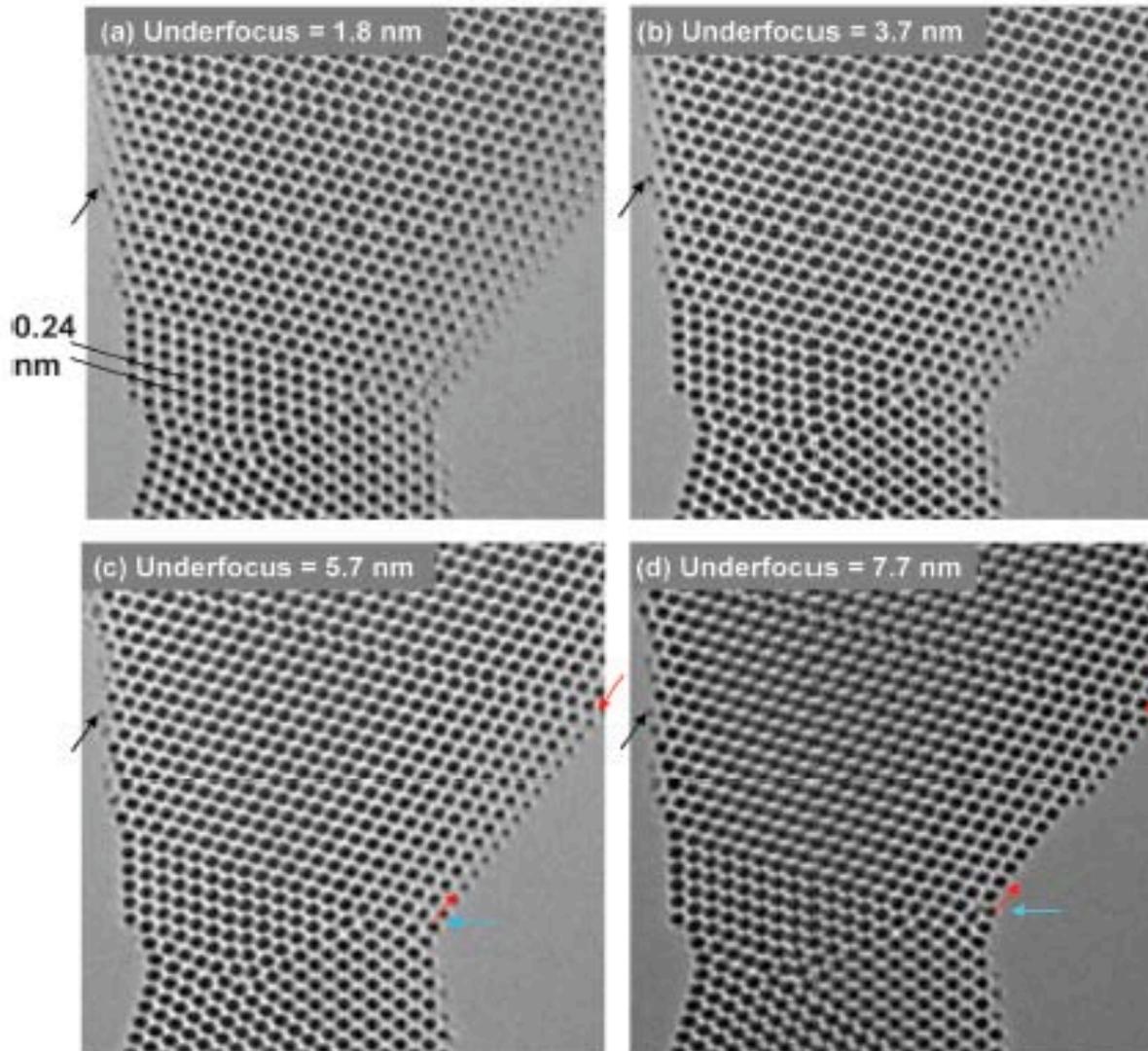
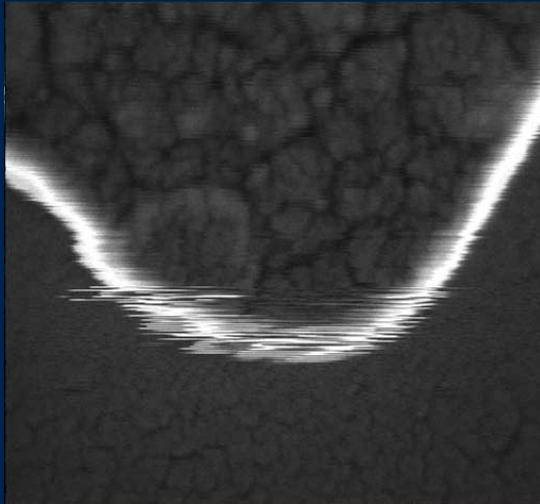
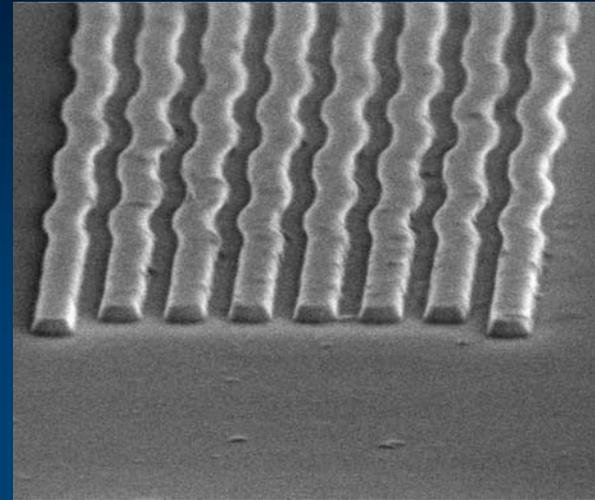


Figure 6. Four sequentially recorded TEM lattice images of gold [110] nanobridge connecting two grains that are rotated relative to each other by 90° around [110] axis. The four images shown are part of a 15-member focal series, recorded in time intervals of 1.5 s. Black arrows: (a, b) 2-atom column and (c, d) single atom. Red arrows: thirteen 2-atom columns, some of which disappear in d. Turquoise arrows: Rearrangement of atom columns at the intersection of a dissociated grain boundary with the surface. The focus difference on both sides of the bridge is negligible because the film was grown onto a flat single crystal substrate.

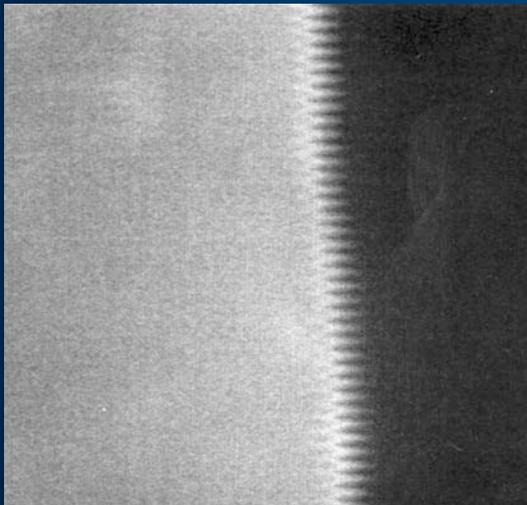
Examples of Environmental "Artifacts"



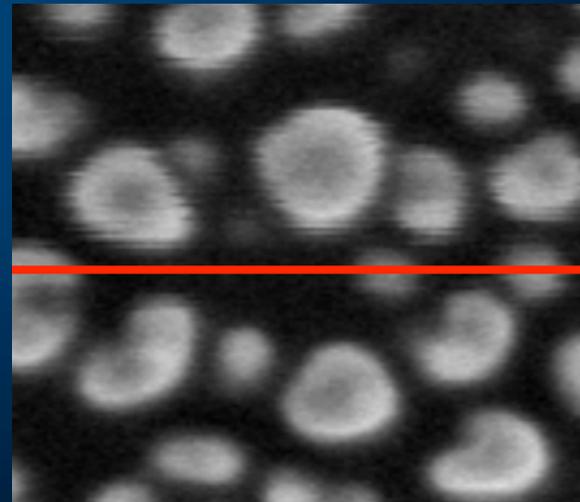
Aperiodic - Vibrational



User-Mechanical

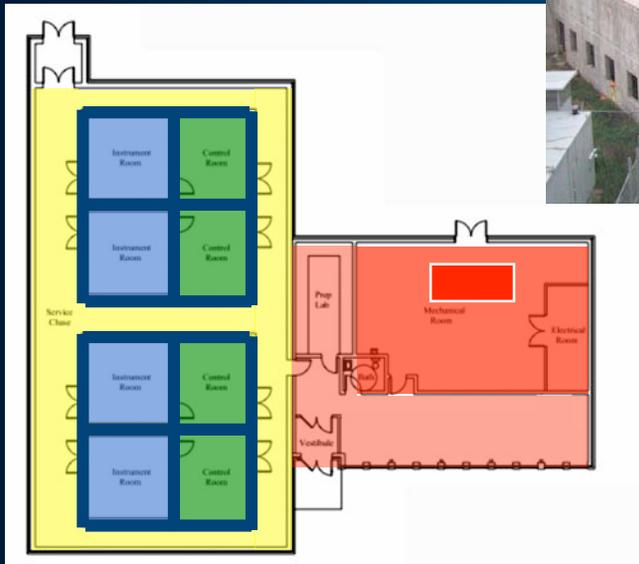


Periodic - EM Fields



User-Acoustic

Sub-Ångstrom Microscopy and Microanalysis Laboratory



Temp: $\pm 0.1 F$

EMF: $< 0.01mG$

Acoustics: $< 40 dB$

Air Flow: $< 1 cm/min$

Vibrations: $< 0.25 \mu m Pk$

Environmental Conditions

Best -> Worse